## CHAPTER 6 Calculator Notes for the TI－Nspire and TI－Nspire CAS

## Note 6A：Entering and Editing Matrices

You will use the Calculator application to enter and edit matrices．

## Entering a Matrix

Press（in）and choose Calculator．To access the $(m \times n)$ matrix template， press ctrl $\begin{gathered}\text { ridet } \\ x \rightarrow 7\end{gathered}$ ．Highlight the small block，which pictures a $3 \times 3$ matrix， and press＊＊＊）．Enter the number of rows and columns and press enier．The handheld displays an empty matrix．Move to each element in the matrix and type the appropriate value in each cell．

To store the matrix as a variable，press until you exit the matrix，press
（ctri）siar var ，type the name of the matrix，and press 气eñer．

## Editing a Matrix

To edit a matrix，highlight it and press 气eñer．The matrix will appear in the entry line．Move to the elements you would like to edit and type new values． Then press 气थñer．

| 1.1 | RAD AUTO REAL |
| :---: | :---: |
| $\left[\begin{array}{ccc}1 & 2 & 3 \\ -2 & 8 & -7 \\ 0 & -5 & 1\end{array}\right] \rightarrow$ mata | $\left[\begin{array}{ccc}1 & 2 & 3 \\ -2 & 8 & -7 \\ 0 & -5 & 1\end{array}\right] \hat{\square}$ |
| $\left[\begin{array}{ccc}1 & 1 & -5 \\ 0 & -4 & -7 \\ 4 & 1 & -1\end{array}\right] \rightarrow$ matb | $\left[\begin{array}{ccc}1 & 1 & -5 \\ 0 & -4 & -7 \\ 4 & 1 & -1\end{array}\right]$ |
| $\left[\begin{array}{ccc}1 & 0 & -1 \\ 0 & 1 & 0\end{array}\right] \rightarrow$ matc |  |
|  | 2／99 |


| $\left[\begin{array}{ccc}\hline 1.1 & & \text { RAD AUTO REAL } \\ \hline\left[\begin{array}{ccc}1 & 2 & 3 \\ -2 & 8 & -7 \\ 0 & -5 & 1\end{array}\right] \rightarrow \text { mata } & \square \\ \hline\left[\begin{array}{ccc}1 & 1 & -5 \\ 0 & -4 & -7 \\ 4 & 1 & -1\end{array}\right] \rightarrow \text { matb } & {\left[\begin{array}{ccc}1 & 2 & 3 \\ -2 & 8 & -7 \\ 0 & -5 & 1\end{array}\right]} \\ \hline\left[\begin{array}{ccc}1 & 0 & -1 \\ 0 & 1 & 0\end{array}\right] \rightarrow \text { matc } & {\left[\begin{array}{ccc}1 & 1 & -5 \\ 0 & -4 & -7 \\ 4 & 1 & -1\end{array}\right]} \\ \hline\end{array} \quad\left[\begin{array}{ccc}1 & 0 & -1 \\ 0 & 1 & 0\end{array}\right]\right.$ |
| :--- | :--- |



## Note 6B：Matrix Operations

You can perform operations on matrices just as with numbers．You can add or subtract matrices if they have the same dimensions．

（continued）

You can multiply two matrices if the number of columns in the first matrix matches the number of rows in the second matrix.

| 1.1 | RAD AUto REAL $\quad \square$ |
| :---: | :---: |
| mata-matb | $\left[\begin{array}{ccc}\frac{25}{2} & \frac{-9}{2} & \frac{-39}{2} \\ -30 & -41 & -39 \\ 4 & 21 & 34\end{array}\right] \hat{\nabla}$ |
| $\left[\begin{array}{ccc}1 & 2 & 3 \\ 0 & -1 & 0\end{array}\right]\left[\begin{array}{cc}1 & -1 \\ 0 & 5 \\ 2 & -7\end{array}\right]$ | $\left[\begin{array}{cc}7 & -12 \\ 0 & -5\end{array}\right]$ |
| 1 - |  |
|  | 8/99 |

You can multiply any matrix by a constant.


You can raise a square matrix to a power.

| 1.1 | RAD AUTO REAL $\square$ |
| :---: | :---: |
| atc | $\left[\begin{array}{lll}2 & 0 & \mathbf{z} \\ 0 & 2 & 0\end{array}\right] \hat{n}$ |
| matb ${ }^{3}$ | $\left[\begin{array}{ccc}-47 & 6 & 158 \\ 112 & -29 & 42 \\ -104 & -22 & 33\end{array}\right]$ |
| $\left[\begin{array}{cc}-5 & 1 \\ 7 & 3\end{array}\right]^{2}$ | $\left[\begin{array}{cc}32 & -2 \\ -14 & 16\end{array}\right]$ |
|  | 12/99 |

The result of a matrix operation can be stored in a matrix with a variable name or used in the next calculation. This allows you to work recursively with matrices.

| 1.1 | RAD AUTO REAL |
| :--- | ---: |
| $\left[\begin{array}{cc}3 & 5 \\ 7 & -2\end{array}\right] \cdot\left[\begin{array}{cc}1 & -6 \\ -3 & 5\end{array}\right]$ | $\left[\begin{array}{cc}-12 & 7 \\ 13 & -52\end{array}\right]$ |
| Ans $\cdot\left[\begin{array}{cc}1 & -6 \\ -3 & 5\end{array}\right]$ |  |
|  |  |
|  |  |
|  |  |
|  |  |


| 1.1 | RAD AUTO REAL |
| :--- | ---: |
| $\left[\begin{array}{cc}3 & 5 \\ 7 & -2\end{array}\right] \cdot\left[\begin{array}{cc}1 & -6 \\ -3 & 5\end{array}\right]$ | $\left[\begin{array}{cc}-12 & 7 \\ 13 & -52\end{array}\right]$ |
| $\left[\begin{array}{cc}-12 & 7 \\ 13 & -52\end{array}\right] \cdot\left[\begin{array}{cc}1 & -6 \\ -3 & 5\end{array}\right]$ | $\left[\begin{array}{cc}-33 & 107 \\ 169 & -338\end{array}\right]$ |
| $\left[\begin{array}{cc}-33 & 107 \\ 169 & -338\end{array}\right] \cdot\left[\begin{array}{cc}1 & -6 \\ -3 & 5\end{array}\right]$ | $\left[\begin{array}{cc}-354 & 733 \\ 1183 & -2704\end{array}\right]$ |

## Errors

If you get an Error: Dimension error message, then the dimensions of the matrices do not satisfy the operation's criteria.
An Error: Variable is not defined message probably indicates that you have named a matrix that has not been defined.

## Note 6C: Plotting a Polygon

To plot a polygon stored as a matrix, you need to convert the matrix into two lists, one representing the $x$-coordinates and the other representing the $y$-coordinates. To graph a closed figure, you must repeat the first point as the last point. For example, the matrix $\left[\begin{array}{rrrrr}1 & -2 & -3 & 2 & 1 \\ 2 & 1 & -1 & -2 & 2\end{array}\right]$ represents the quadrilateral with vertices $(1,2),(-2,1),(-3,-1)$, and $(2,-2)$.

First, you will create two submatrices that each contain just one row of the original polygon matrix. Then you will convert each submatrix into a list. So, to plot the polygon represented by a matrix, follow these steps:
a. Enter the matrix and store it as matrix poly.

b. Save each row of the matrix in a submatrix. To create a submatrix, press (menu) and choose Matrix \& Vector $\mid$ Create | Submatrix. Input the name of the original matrix, the starting row number of the submatrix, the starting column number, the ending row number, and the ending column number of the submatrix.
Type poly, 1, 1, 1,5) to represent row 1 , column 1 , to row 1 , column 5, and press Senter.

| 1.1 DE | DEG AUTO REAL |
| :---: | :---: |
| $\left[\begin{array}{ccccc}1 & -2 & -3 & 2 & 1 \\ 2 & 1 & -1 & -2 & 2\end{array}\right] \rightarrow$ poly | $\left[\begin{array}{ccccc}1 & -2 & -3 & 2 & 1 \\ 2 & 1 & -1 & -2 & 2\end{array}\right]$ |
| subMat(poly, 1,1,1,5) | $\left\|\begin{array}{\|lllll\|}1 & -2 & -3 & 2 & 1\end{array}\right\|$ |
| mat list() |  |
|  | 1/2 |

c. Store the resulting matrix as a list by pressing menu and choosing Statistics $\mid$ List Operations | Convert Matrix to List. Press $\boldsymbol{\sim}$ enier ) to copy the matrix from above to the current line. Press atrl) and type the name of the list, xcoord, and press 气enerer.

(continued)
d. Repeat the process for the $y$-coordinates, but change the row and column references to $2,1,2,5$. Store this matrix as the list ycoord.


Make a scatter plot of (xcoord, ycoord) in a Graphs \& Geometry page. Move to the attribute icon in the entry line and press ****。 Press $-*_{*}^{*}$ to connect the vertices of the polygon.
Set an appropriate window and display the graph. Press ctrr (G) to hide the entry line.


You can also use matrices to transform polygons. You can nest commands and copy and edit commands and expressions to make the process easier.


## Note 6D: Inverse Matrices

To find the inverse of a square matrix, type in the matrix or its variable


| 1.1 | RAD AUTO REAL |
| :--- | ---: |
| $\left[\begin{array}{ll}1 & 2 \\ 4 & 5\end{array}\right]^{-1}$ | $\left[\begin{array}{cc}\frac{-5}{3} & \frac{2}{3} \\ \frac{4}{3} & \frac{-1}{3}\end{array}\right]$ |
| $m^{-1}$ | $\left[\begin{array}{cc}2 & -2 \\ -4 & 0\end{array}\right]$ |
| 1 |  |

If you get an Error: Dimension error message, the matrix is not square; if you get an Error: Singular matrix message, one row of the matrix is a multiple of another row. In either case, the matrix has no inverse.

## Note 6E: Matrix Row Operations

The handheld can perform four operations on the rows of a matrix. To continue working with a matrix, store the matrix as a variable, or work with it recursively by pressing otris
To exchange two rows of a matrix, press (menu) and choose Matrix \& Vector | Row Operations | Swap Rows. Then type the matrix or its name and the two row numbers you would like to exchange.

| 1.1 RAD AUTO | RAD AUTO REAL |
| :---: | :---: |
| $\left[\begin{array}{ccc}2 & 1 & 5 \\ 5 & 3 & 13\end{array}\right] \rightarrow$ matrixa | $\left[\begin{array}{ccc}2 & 1 & 5 \\ 5 & 3 & 13\end{array}\right]$ |
| rowSwap (matrixa, 1,2) $\rightarrow$ matrixa | $\left[\begin{array}{ccc}5 & 3 & 13 \\ 2 & 1 & 5\end{array}\right]$ |
|  |  |

To add the entries of one row to those of another row, press menu and choose Matrix \& Vector|Row Operations | Row Add. For example, you add the entries of row 1 to those of row 2 and store them in row 2 with the command rowAdd (matrixa, 1, 2).

| 1.1 |  |
| :--- | :--- |
| $\left[\begin{array}{ccc}2 & 1 & 5 \\ 5 & 3 & 13\end{array}\right] \rightarrow$ matrixa | $\left[\begin{array}{ccc}2 & 1 & 5 \\ 5 & 3 & 13\end{array}\right]$ |
| rowSwap $($ matrixa, 1,2$) \rightarrow$ matrixa | $\left[\begin{array}{ccc}5 & 3 & 13 \\ 2 & 1 & 5\end{array}\right]$ |
| rowAdd (matrixa,1,2) $\rightarrow$ matrixa | $\left[\begin{array}{ccc}5 & 3 & 13 \\ 12 & 7 & 31\end{array}\right]$ |
| 1 |  |

To multiply the entries in a row by a value, press (menu and choose Matrix \& Vector |Row Operations |Multiply Row. For example, you multiply the entries of row 1 by 5 and store the products in row 1 with the command mRow(5, matrixa, 1).

| 1.1 | RAD AUTO REAL |
| :---: | :---: |
| $\text { rowSwap }(\text { matrixa, } 1,2) \rightarrow \text { matrixa }\left[\begin{array}{lll} 5 & 3 & 13 \\ 2 & 1 & 5 \end{array}\right]$ |  |
|  |  |
| rowA | $\rightarrow$ matrixa $\left[\begin{array}{c}5 \\ 12 \\ 12\end{array}\right.$ |
| $\text { mRow }\left(5, \text { matrixa, } 1 \text { ) } \rightarrow \text { matrixa }\left[\begin{array}{ccc} 25 & 15 & 65 \\ 12 & 7 & 31 \end{array}\right]\right.$ |  |
| 4/99 |  |

To multiply the entries of one row by a value and add the products to another row, press menu) and choose Matrix \& Vector $\mid$ Row Operations |Multiply Row \& Add. For example, you multiply the entries of row 1 by 5 , add the products to row 2 , and store them in row 2 with the command mRowAdd(5, matrixa, 1, 2).

| 1.1 | RAD AUTO REAL | $\square$ |
| :---: | :---: | :---: |
| row | $\rightarrow$ mabrixa $\left[\begin{array}{cc}5 & 5 \\ 12 & 7\end{array}\right.$ |  |
| mRow | matrixa $\left[\begin{array}{cc}25 & 15 \\ 12 & 7\end{array}\right.$ |  |
| $\begin{array}{r} \text { mRowAdd }(5, \text { matrixa, } 1,2) \rightarrow \text { matrixa } \\ \qquad\left[\begin{array}{ccc} 25 & 15 & 65 \\ 137 & 82 & 356 \end{array}\right] \end{array}$ |  |  |
| 5/99 |  |  |

These commands don't change the original matrix, they create a new matrix. You'll probably want to end each command by storing the new matrix with a new name. If you don't need to keep the original matrix, you can store the new matrix with the original name, as was done in each of the examples.

## Note 6F: Reduced Row-Echelon Form

To convert an augmented matrix to reduced row-echelon form, type rref( or press (menu) and choose Matrix \& Vector | Reduced Row-Echelon Form. Type the matrix or its name, and press 气enter. For example, the following system of equations could be solved by using reduced row-echelon form to get $x=2, y=3$, and $z=4$.
$\left\{\begin{array}{l}x-y+2 z=7 \\ x+2 y-3 z=-4 \\ 2 x+2 y-z=6\end{array}\right.$


## Note 6G: Graphing Inequalities

Press (n) and choose Graphs \& Geometry. Move to the entry line and press $\stackrel{\text { clear }}{\leftrightarrows}$ to delete the " $=$ " symbol. Next, type the inequality symbol.
To create " $\leq$ " or " $\geq$ " press ctrl $<$ or ctrr $>$. As soon as the inequality sign is typed, $f_{1}(x)$ changes to $y$. Type the rest of the expression and press eñer to graph the inequality.


