# HP 12c Financial Calculator - Internal Rate of Return

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## Cash flow and IRR calculations

Cash flow analysis is an extension of the basic TVM concepts applied to compound interest problems when payments occur in regular periods and do not have the same value. Any financial investment can be represented as an initial investment of money and a series of later cash flows that occur in regular periods of time. Each flow of money can be positive (received) or negative (paid out) and considered as a cash flow. Common cash flow problems usually involve the calculation of the Internal Rate of Return (IRR) or the Net Present Value (NPV).

The NPV expresses the amount of money resulting from the summation of the initial investment ( $CF_0$ ) and the present value of each anticipated cash flow ( $CF_i$ ) calculated to the time of the initial investment. The IRR is the discounted rate applied to all future cash flows that cause NPV = 0.

The expression that calculates the Internal Rate of Return is:

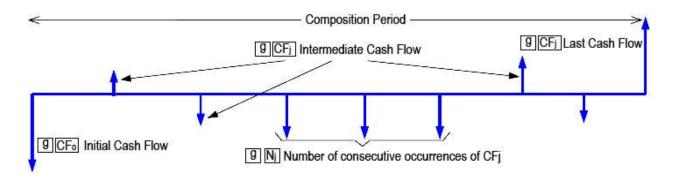
Figure: Expression calculating Internal Rate of Return

$$0 = CF_0 + \sum_{j=1}^{k} CF_j \times \left[ \frac{1 - (1 + IRR)^{-nj}}{IRR} \right] \times (1 + IRR)^{-nj}$$

# Cash flow diagrams

The cash flow diagram in Figure 1 illustrates one of the many possible situations that can be handled by the HP 12c.

Figure: Cash flow diagram



# The HP 12c cash flow approach

In the HP 12c each cash flow amount is stored in its corresponding register in memory. For each cash flow amount there is a related register to store the number of consecutive occurrences of this amount. This approach is shown below:

Figure: Diagram showing different cash flow amounts can be stored

	Registers	Cash flow	Ni	
R₀ [	1500	CF₀ [	181	No
R₀ R₁		CF <sub>1</sub>		N <sub>1</sub>
<sub>-</sub>		T F	***	7
R <sub>6</sub>		_ CF6 _		N <sub>6</sub>
R <sub>6</sub> R <sub>7</sub>		CF <sub>7</sub>		N <sub>7</sub>
Б Г	1157	Der E		Пм
T.8		CF <sub>18</sub>		N <sub>18</sub>
R.9		CF <sub>19</sub>		N <sub>19</sub>
R. <sub>8</sub> [ R. <sub>9</sub> [ FV [		CF <sub>20</sub>		N <sub>20</sub>

The HP 12c memory organization allows up to 20 different cash flow amounts plus the initial investment to be stored and handled according to the diagram in Figure 2. If any cash flow amount repeats consecutively, then it can be stored as a grouped cash flow  $CF_i$  and its corresponding  $N_i$  holds the number of occurrences, up to 99. TVM register 'n' is used as an index to control CF operations.

The keys to enter cash flow data are:

Keystroke	Description
g CFo	Stores the number in the display in R₀ and sets 'n' to zero.

Keystroke	Description	
g CF <sub>J</sub>	Adds 1 unit to current 'n' contents (j) and then stores the number in the display in $R_{\rm i}$ .	
g N <sub>i</sub>	Stores the number in the display in N; 'n' contents (j) are not changed.	
NOTE: The number in the display must be a positive integer from 1 to 99, otherwise		
	lable register has already been used, <b>9 CF</b> J adds 1 unit to current 'n' stores the number in the display in TVM register FV. Any attempt to add a bunt with <b>9 CF</b> J after FV has already been used or when 'n' contents	

# Practice solving IRR problems

refer to a register that is not available causes

in the display and no operation is performed.

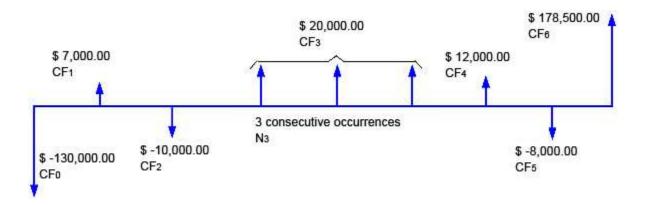
## Example 1

The cash flow diagram below represents a possible investment and you were chosen to determine if it is feasible. The success of this investment dictates your future in the company, so the analysis must be precise and error free. What is the correct keystroke sequence to fill the HP 12c registers with all data?

Error

to be shown

Figure: Values entered in the cash flow diagram



#### Solution

Clearing all registers is not necessary to start cash flow analysis because only the registers updated with cash flow data are used.

Keystroke	Display
13000 CHS g CFo 7000 g CFi 1000 CHS g CFi	Figure : Entering the first set of values  - 10,0000.00

The next cash flow amount occurs three times in a sequence, so it can be entered as a grouped cash flow.

Keystroke	Display
20000 g CFi 3 g Ni	Figure: Entering the next set of values  3.00

The remaining data is entered with the following keystroke sequence:

Keystroke	Display
12000 g CF <sub>1</sub> 8000 CHS g CF <sub>1</sub> 178500 g CF <sub>1</sub>	Figure : Entering the remaining set of values

#### Answer

The keystrokes presented above indicate the correct entries.

#### Example 2

The cash flow diagram had all of its information used to compose the cash flow data in the HP 12c memory. Show how to check that they were entered correctly.

#### Solution

Now that all data is entered, checking for its correctness is possible in two ways. The most common way is the sequential check and the keystroke sequence for this checking is as follows:

Keystroke	Display
RCL n	Figure : Displaying the number of the last register <b>6.00</b>

This is the number of the last register used to store the cash flow data. It will be needed later.

Keystroke	Display
RCL 9 CF	Figure : Displaying the amount of CF <sub>6</sub>

This is the amount of CF<sub>6</sub>. The sequential checking works backwards, and each time **RCL g CF**<sub>1</sub> is pressed, 'n' is decreased by one unit. Now check CF<sub>5</sub>, CF<sub>4</sub> and when checking CF<sub>3</sub> verify N<sub>3</sub> as well.

Keystroke	Display
RCL g CFI RCL g CFI RCL g Ni	Figure : Checking the cash flow data entered  3.0 0

This is the  $N_3$  value. Whenever  $N_i$  needs to be checked, it must be recalled first. Now check the  $CF_3$  value:

Keystroke	Display
RCL 9 CF	Figure : Checking the CF <sub>3</sub> value

Continue checking CF<sub>2</sub>, CF<sub>1</sub> and stop when CF<sub>0</sub> is shown in the display.

Keystroke	Display
RCL 9 CF	Figure: Displaying the value of CF <sub>0</sub> - 130,000.00

Recall 'n' contents to the display:

Keystroke	Display	
RCL n	Figure : Recalling the contents  - 1.0 0	

#### **Answer**

The entries are correct.

## Example 3

The investment is considered attractive if it shows at least 8% of internal rate of return. Calculate the IRR.

#### Solution

To perform either IRR or NPV calculations, 'n' must have its contents restored to the correct value:

Keystroke	Display
6 n f IRR	(flashing)  Figure : Calculating the Internal Rate of Return  9.3 7

#### Answer

Yes, the investment is attractive based on its 9.37% internal rate of return.

# How to modify cash flow entries

If it happens that a cash flow entry was wrongly entered, modifying its amount is not difficult and there is no need to enter all data again. In fact there are two ways for doing this.

## Example 4

Update the amount of CF<sub>2</sub> for \$-9,500.00 and compute the new IRR after this change.

#### Solution 1

Type in the correct amount and store it in R<sub>2</sub>:

Keystroke	Display
9 5 0 0 CHS STO 2 f IRR	Figure: Updating the amount of CF <sub>2</sub>

#### Solution 2

Set 'n' register to (j-1), type in the correct amount, press **9 CF1**, then restore 'n' prior to compute IRR:

Keystroke	Display
1 n 9 5 0 0 CHS g CF <sub>J</sub> 6 n f IRR	Figure : Calculating the Internal Rate of Return  9.42

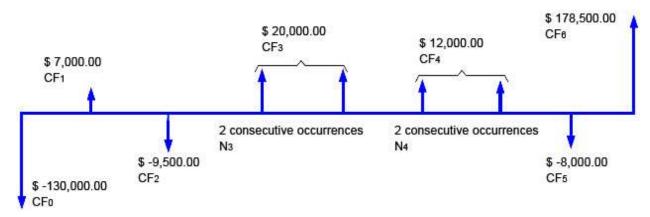
#### Answer

The investment is still attractive based on revised IRR of 9.42%.

To modify a wrongly entered N<sub>i</sub>, it is necessary to change the value stored in the register 'n'.

## Example 5

Now change both  $N_3$  and  $N_4$  to 2 and calculate the IRR again. The cash flow diagram now looks like this:



#### Solution

For each correction, set 'n' to match 'j,' type in the correct  $N_i$  and press  $N_i$ . After all corrections, set 'n' to its original value and press  $N_i$ .

Keystroke	Display
3 n 2 g N <sub>j</sub> 4 n 2 g N <sub>j</sub> 6 n f IRR	Figure : Calculating the new Internal Rate of Return

#### **Answer**

The newly computed IRR is 8.77%.