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## General Series Formulas

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## List of 21 General Series Formulas

## General Series

## Fibonacci Sequence [

1) Nth Term of Fibonaccci Sequence
fx $\mathrm{F}_{\mathrm{n}}=\mathrm{F}_{\mathrm{n}-1}+\mathrm{F}_{\mathrm{n}-2}$
ex $21=13+8$
2) Nth Term of Fibonaccci Sequence using Golden Ratio
$\mathrm{fx}_{\mathrm{F}}^{\mathrm{F}}=\frac{[\mathrm{phi}]^{\mathrm{n}_{\mathrm{Fib}}}-(1-[\mathrm{phi}])^{\mathrm{n}_{\mathrm{Fib}}}}{\sqrt{5}}$
ex $21=\frac{[\mathrm{phi}]^{8}-(1-[\mathrm{phi}])^{8}}{\sqrt{5}}$
3) Sum of First N Even Index Fibonacci Numbers 凹
$f x \quad S_{n(\text { Fib }) \text { Even }}=F_{2 n+1}-1$
ex $1596=1597-1$
4) Sum of First N Fibonacci Numbers
$f \mathrm{f} \mathrm{S}_{\mathrm{n}(\mathrm{Fib})}=\mathrm{F}_{\mathrm{n}+2}-1$
ex $54=55-1$
5) Sum of First N Odd Index Fibonacci Numbers
$f \mathrm{f} \quad \mathrm{S}_{\mathrm{n}(\mathrm{Fib}) \text { Odd }}=1 \cdot \mathrm{~F}_{2 \mathrm{n}}$
ex $987=1.987$

## Sum of 4th Powers

6) Sum of 10th Powers of First N Natural Numbers

$$
\mathrm{S}_{\mathrm{n} 10}=\frac{\mathrm{n} \cdot(\mathrm{n}+1) \cdot(2 \cdot \mathrm{n}+1) \cdot\left(\mathrm{n}^{2}+\mathrm{n}-1\right) \cdot\left(3 \cdot \mathrm{n}^{6}+9 \cdot \mathrm{n}^{5}+2 \cdot \mathrm{n}^{4}-11 \cdot \mathrm{n}^{3}+3 \cdot \mathrm{n}^{2}+10\right.}{66}
$$

ex
$60074=\frac{3 \cdot(3+1) \cdot(2 \cdot 3+1) \cdot\left((3)^{2}+3-1\right) \cdot\left(3 \cdot(3)^{6}+9 \cdot(3)^{5}+2 \cdot(3)^{4}-11 \cdot(3)^{3}+3 \cdot(3)^{2}+10 \cdot 3-\right.}{66}$
7) Sum of 4th Powers of First N Natural Numbers
$f x S_{n 4}=\frac{\mathrm{n} \cdot(\mathrm{n}+1) \cdot(2 \cdot \mathrm{n}+1) \cdot\left(3 \cdot \mathrm{n}^{2}+3 \cdot \mathrm{n}-1\right)}{30}$
Open Calculator
ex $98=$

$$
\frac{3 \cdot(3+1) \cdot(2 \cdot 3+1) \cdot\left(3 \cdot(3)^{2}+3 \cdot 3-1\right)}{30}
$$

8) Sum of 5th Powers of First $N$ Natural Numbers
$f \mathrm{x} \mathrm{S}_{\mathrm{n} 5}=\frac{\mathrm{n}^{2} \cdot\left(2 \cdot \mathrm{n}^{2}+2 \cdot \mathrm{n}-1\right) \cdot(\mathrm{n}+1)^{2}}{12}$
$\frac{(3)^{2} \cdot\left(2 \cdot(3)^{2}+2 \cdot 3-1\right) \cdot(3+1)^{2}}{12}$
9) Sum of 6th Powers of First $N$ Natural Numbers
$f x S_{n 6}=\frac{\mathrm{n} \cdot(\mathrm{n}+1) \cdot(2 \cdot \mathrm{n}+1) \cdot\left(3 \cdot \mathrm{n}^{4}+6 \cdot \mathrm{n}^{3}-3 \cdot \mathrm{n}+1\right)}{42}$
ex $794=\frac{3 \cdot(3+1) \cdot(2 \cdot 3+1) \cdot\left(3 \cdot(3)^{4}+6 \cdot(3)^{3}-3 \cdot 3+1\right)}{42}$
10) Sum of 7th Powers of First N Natural Numbers
$\mathrm{fx} \mathrm{S}_{\mathrm{n} 7}=\frac{\mathrm{n}^{2} \cdot\left(3 \cdot \mathrm{n}^{4}+6 \cdot \mathrm{n}^{3}-\mathrm{n}^{2}-4 \cdot \mathrm{n}+2\right) \cdot(\mathrm{n}+1)^{2}}{24}$
$2316=$ $\frac{(3)^{2} \cdot\left(3 \cdot(3)^{4}+6 \cdot(3)^{3}-(3)^{2}-4 \cdot 3+2\right) \cdot(3+1)^{2}}{24}$
11) Sum of 8th Powers of First $N$ Natural Numbers
$\mathrm{S}_{\mathrm{n} 8}=\frac{\mathrm{n} \cdot(\mathrm{n}+1) \cdot(2 \cdot \mathrm{n}+1) \cdot\left(5 \cdot \mathrm{n}^{6}+15 \cdot \mathrm{n}^{5}+5 \cdot \mathrm{n}^{4}-15 \cdot \mathrm{n}^{3}-\mathrm{n}^{2}+9 \cdot \mathrm{n}-3\right)}{90}$
$\operatorname{ex} 6818=\frac{3 \cdot(3+1) \cdot(2 \cdot 3+1) \cdot\left(5 \cdot(3)^{6}+15 \cdot(3)^{5}+5 \cdot(3)^{4}-15 \cdot(3)^{3}-(3)^{2}+9 \cdot 3-3\right)}{90}$
12) Sum of 9th Powers of First $N$ Natural Numbers $\leftrightarrows$
$f x \mathrm{~S}_{\mathrm{n} 9}=\frac{\mathrm{n}^{2} \cdot\left(\mathrm{n}^{2}+\mathrm{n}-1\right) \cdot\left(2 \cdot \mathrm{n}^{4}+4 \cdot \mathrm{n}^{3}-\mathrm{n}^{2}-3 \cdot \mathrm{n}+3\right) \cdot(\mathrm{n}+1)^{2}}{20}$
$\operatorname{ex} 20196=\frac{(3)^{2} \cdot\left((3)^{2}+3-1\right) \cdot\left(2 \cdot(3)^{4}+4 \cdot(3)^{3}-(3)^{2}-3 \cdot 3+3\right) \cdot(3+1)^{2}}{20}$

## Sum of Cubes

13) Sum of Cubes of First $N$ Even Numbers
fx $\mathrm{S}_{\mathrm{n} 3(\text { Even })}=2 \cdot\left(\mathrm{n} \cdot(\mathrm{n}+1)^{2}\right.$
ex $288=2 \cdot(3 \cdot(3+1))^{2}$
14) Sum of Cubes of First N Natural Numbers
$f \mathrm{f} \mathrm{S}_{\mathrm{n} 3}=\frac{(\mathrm{n} \cdot(\mathrm{n}+1))^{2}}{4}$
ex $36=\frac{(3 \cdot(3+1))^{2}}{4}$
15) Sum of Cubes of First N Odd Numbers
$f \times \mathrm{S}_{\mathrm{n} 3(\text { Odd })}=(\mathrm{n})^{2} \cdot\left(2 \cdot(\mathrm{n})^{2}-1\right)$
ex $153=(3)^{2} \cdot\left(2 \cdot(3)^{2}-1\right)$

## Sum of Squares

16) Sum of Squares of First $N$ Even Natural Numbers
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$f \mathrm{x} \mathrm{S}_{\mathrm{n} 2(\text { Even })}=\frac{2 \cdot \mathrm{n} \cdot(\mathrm{n}+1) \cdot((2 \cdot \mathrm{n})+1)}{3}$
$\mathrm{ex} 56=\frac{2 \cdot 3 \cdot(3+1) \cdot((2 \cdot 3)+1)}{3}$
17) Sum of Squares of First $N$ Natural Numbers
$f \mathrm{x} \mathrm{S}_{\mathrm{n} 2}=\frac{\mathrm{n} \cdot(\mathrm{n}+1) \cdot((2 \cdot \mathrm{n})+1)}{6}$
ex $14=\frac{3 \cdot(3+1) \cdot((2 \cdot 3)+1)}{6}$
18) Sum of Squares of First N Odd Natural Numbers
fx $\mathrm{S}_{\mathrm{n} 2(\mathrm{Odd})}=\frac{\mathrm{n} \cdot((2 \cdot \mathrm{n})+1) \cdot((2 \cdot \mathrm{n})-1)}{3}$
ex $35=\frac{3 \cdot((2 \cdot 3)+1) \cdot((2 \cdot 3)-1)}{3}$

## Sum of Terms

19) Sum of First N Even Natural Numbers
$f \mathrm{f} \mathrm{S}_{\mathrm{n}(\mathrm{Even})}=\mathrm{n} \cdot(\mathrm{n}+1)$
ex $12=3 \cdot(3+1)$
20) Sum of First $N$ Natural Numbers
f. $\mathrm{S}_{\mathrm{n}}=\frac{\mathrm{n} \cdot(\mathrm{n}+1)}{2}$
ex $6=\frac{3 \cdot(3+1)}{2}$
21) Sum of First N Odd Natural Numbers
fx $\mathrm{S}_{\mathrm{n}(\mathrm{Odd})}=\mathrm{n}^{2}$
ex $9=(3)^{2}$

## Variables Used

- $\mathbf{F}_{2 \mathrm{n}}$ 2Nth Term of Fibonacci Sequence
- $\mathrm{F}_{2 \mathrm{n}+1}(2 \mathrm{~N}+1)$ th Term of Fibonacci Sequence
- $\mathbf{F}_{\mathbf{n}}$ Nth Term of Fibonacci Sequence
- $\mathrm{F}_{\mathrm{n}+2}(\mathrm{~N}+2)$ th Term of Fibonacci Sequence
- $\mathrm{F}_{\mathrm{n}-1}(\mathrm{~N}-1)$ th Term of Fibonacci Sequence
- $\mathrm{F}_{\mathrm{n}-2}$ (N-2)th Term of Fibonacci Sequence
- $\mathbf{n}$ Value of N
- $\mathrm{n}_{\text {Fib }}$ Value of N of Fibonacci Sequence
- $\mathbf{S}_{\mathbf{n}}$ Sum of First $N$ Natural Numbers
- $\mathbf{S}_{\mathrm{n}(\text { Even })}$ Sum of First N Even Natural Numbers
- $\mathbf{S}_{\mathrm{n}(\mathrm{Fib})}$ Sum of First $N$ Fibonacci Numbers
- $\mathbf{S}_{\mathbf{n}(\text { Fib }) \text { Even }}$ Sum of First $N$ Even Index Fibonacci Numbers
- $\mathbf{S}_{\mathbf{n}(\text { Fib)Odd }}$ Sum of First $N$ Odd Index Fibonacci Numbers
- $\mathrm{S}_{\mathrm{n}(\mathrm{Odd})}$ Sum of First N Odd Natural Numbers
- $\mathbf{S}_{\mathbf{n} 10}$ Sum of 10th Powers of First $N$ Natural Numbers
- $\mathbf{S}_{\mathrm{n} 2}$ Sum of Squares of First N Natural Numbers
- $S_{n 2(E v e n)}$ Sum of Squares of First $N$ Even Natural Numbers
- $\mathbf{S}_{\mathrm{n} 2 \text { (Odd) }}$ Sum of Squares of First $N$ Odd Natural Numbers
- $\mathrm{S}_{\mathrm{n} 3}$ Sum of Cubes of First $N$ Natural Numbers
- $S_{n 3(E v e n)}$ Sum of Cubes of First $N$ Even Natural Numbers
- $\mathbf{S}_{\mathrm{n} 3 \text { (Odd) }}$ Sum of Cubes of First N Odd Natural Numbers
- $\mathbf{S}_{\mathrm{n} 4}$ Sum of 4th Powers of First $N$ Natural Numbers
- $\mathbf{S}_{\mathrm{n} 5}$ Sum of 5th Powers of First $N$ Natural Numbers
- $\mathbf{S}_{\mathrm{n} 6}$ Sum of 6th Powers of First $N$ Natural Numbers
- $\mathrm{S}_{\mathrm{n} 7}$ Sum of 7th Powers of First $N$ Natural Numbers
- $\mathrm{S}_{\mathrm{n} 8}$ Sum of 8th Powers of First N Natural Numbers
- $\mathbf{S}_{\mathrm{n} 9}$ Sum of 9th Powers of First N Natural Numbers


## Constants, Functions, Measurements used

- Constant: [phi], 1.61803398874989484820458683436563811

Golden ratio

- Function: sqrt, sqrt(Number)

Square root function

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- Mean Formulas

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