TI-83/84 Guide for Introductory Statistics

Includes step-by-step instructions, practice exercises, and links to video tutorials. Covers all calculator features needed for AP[®] Statistics Exam

Instructions excerpted from Advanced High School Statistics, 2nd ed. available for FREE at openintro.org/ahss

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Summarizing data

Entering data

TI-83/84: ENTERING DATA

The first step in summarizing data or making a graph is to enter the data set into a list. Use STAT, Edit.

- 1. Press STAT.
- 2. Choose 1:Edit.
- 3. Enter data into L1 or another list.

Calculating summary statistics

TI-84: CALCULATING SUMMARY STATISTICS

Use the STAT, CALC, 1-Var Stats command to find summary statistics such as mean, standard deviation, and quartiles.

- 1. Enter the data as described previously.
- 2. Press STAT.
- 3. Right arrow to CALC.
- 4. Choose 1:1-Var Stats.
- 5. Enter L1 (i.e. 2ND 1) for List. If the data is in a list other than L1, type the name of that list.
- 6. Leave FreqList blank.
- 7. Choose Calculate and hit ENTER.

TI-83: Do steps 1-4, then type L1 (i.e. 2nd 1) or the list's name and hit ENTER.

Calculating the summary statistics will return the following information. It will be necessary to hit the down arrow to see all of the summary statistics.

 $\bar{\mathbf{x}}$ Mean $\Sigma \mathbf{x}$ Sum of all the data values $\Sigma \mathbf{x}^2$ Sum of all the squared data values $\mathbf{S} \mathbf{x}$ Sample standard deviation $\sigma \mathbf{x}$ Population standard deviation

Drawing a box plot

TI-83/84: DRAWING A BOX PLOT

- 1. Enter the data to be graphed as described previously.
- 2. Hit 2ND Y= (i.e. STAT PLOT).
- 3. Hit ENTER (to choose the first plot).
- 4. Hit ENTER to choose ON.
- 5. Down arrow and then right arrow three times to select box plot with outliers.
- 6. Down arrow again and make Xlist: L1 and Freq: 1.
- 7. Choose ZOOM and then 9:ZoomStat to get a good viewing window.

What to do if you cannot find L1 or another list

TI-83/84: WHAT TO DO IF YOU CANNOT FIND L1 OR ANOTHER LIST Restore lists L1-L6 using the following steps:

1. Press STAT.

- 2. Choose 5:SetUpEditor.
- 3. Hit ENTER.

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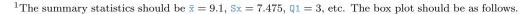
Practice exercises

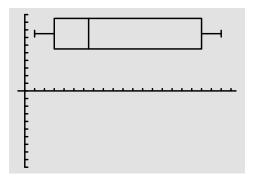
GUIDED PRACTICE 0.1

Enter the following 10 data points into a list on a calculator:

5, 8, 1, 19, 3, 1, 11, 18, 20, 5

Find the summary statistics and make a box plot of the data.¹





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Probability

Computing the binomial coefficient

TI-83/84: COMPUTING THE BINOMIAL COEFFICIENT, $\binom{n}{k}$

Use MATH, PRB, nCr to evaluate n choose r. Here r and k are different letters for the same quantity.

- 1. Type the value of n.
- 2. Select MATH.
- 3. Right arrow to PRB.
- 4. Choose 3:nCr.
- 5. Type the value of k.
- 6. Hit ENTER.

Example: 5 nCr 3 means 5 choose 3.

Computing the binomial formula

TI-84: COMPUTING THE BINOMIAL FORMULA, $P(X=k) = {n \choose k} p^k (1-p)^{n-k}$

Use 2ND VARS, binompdf to evaluate the probability of *exactly* k occurrences out of n independent trials of an event with probability p.

- 1. Select 2ND VARS (i.e. DISTR)
- 2. Choose A: binompdf (use the down arrow).
- 3. Let trials be n.
- 4. Let \mathbf{p} be p
- 5. Let \mathbf{x} value be k.
- 6. Select Paste and hit ENTER.

TI-83: Do steps 1-2, then enter n, p, and k separated by commas: binompdf(n, p, k). Then hit ENTER.

Computing a cumulative binomial probability

TI-84: COMPUTING $P(X \le k) = \binom{n}{0}p^0(1-p)^{n-0} + ... + \binom{n}{k}p^k(1-p)^{n-k}$

Use 2ND VARS, binomcdf to evaluate the cumulative probability of at most k occurrences out of n independent trials of an event with probability p.

- 1. Select 2ND VARS (i.e. DISTR)
- 2. Choose B: binomcdf (use the down arrow).
- 3. Let trials be n.
- 4. Let p be p
- 5. Let \mathbf{x} value be k.
- 6. Select Paste and hit ENTER.

TI-83: Do steps 1-2, then enter the values for n, p, and k separated by commas as follows: binomcdf(n, p, k). Then hit ENTER.

Practice exercises

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GUIDED PRACTICE 0.2 Find the number of ways of arranging 3 blue marbles and 2 red marbles.²

GUIDED PRACTICE 0.3

There are 13 marbles in a bag. 4 are blue and 9 are red. Randomly draw 5 marbles with replacement. Find the probability you get exactly 3 blue marbles.³

GUIDED PRACTICE 0.4

There are 13 marbles in a bag. 4 are blue and 9 are red. Randomly draw 5 marbles with replacement. Find the probability you get at most 3 blue marbles (i.e. less than or equal to 3 blue marbles).⁴

²Here n = 5 and k = 3. Doing 5 nCr 3 gives the number of combinations as 10.

³Here, n = 5, p = 4/13, and k = 3, so set trials = 5, p = 4/13 and x value = 3. The probability is 0.1396.

⁴Similarly, set trials = 5, p = 4/13 and x value = 3. The cumulative probability is 0.9662.

Distribution of random variables

Finding area under the normal curve

TI-84: FINDING AREA UNDER THE NORMAL CURVE

Use 2ND VARS, normalcdf to find an area/proportion/probability to the left or right of a Z-score or between two Z-scores.

- 1. Choose 2ND VARS (i.e. DISTR).
- 2. Choose 2:normalcdf.
- 3. Enter the Z-scores that correspond to the lower (left) and upper (right) bounds.
- 4. Leave μ as 0 and σ as 1.
- 5. Down arrow, choose Paste, and hit ENTER.

TI-83: Do steps 1-2, then enter the lower bound and upper bound separated by a comma, e.g. normalcdf(2, 5), and hit ENTER.

Find a Z-score that corresponds to a percentile

TI-84: FIND A Z-SCORE THAT CORRESPONDS TO A PERCENTILE

Use 2ND VARS, invNorm to find the Z-score that corresponds to a given percentile.

- 1. Choose 2ND VARS (i.e. DISTR).
- 2. Choose 3:invNorm.
- 3. Let Area be the percentile as a decimal (the area to the left of desired Z-score).
- 4. Leave μ as 0 and σ as 1.
- 5. Down arrow, choose Paste, and hit ENTER.

TI-83: Do steps 1-2, then enter the percentile as a decimal, e.g. invNorm(.40), then hit ENTER.

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Practice exercises

EXAMPLE 0.5

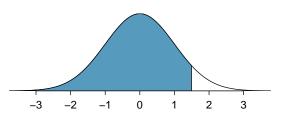
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Use a calculator to determine what percentile corresponds to a Z-score of 1.5.

Always first sketch a graph:⁵



To find an area under the normal curve using a calculator, first identify a lower bound and an upper bound. Theoretically, we want all of the area to the left of 1.5, so the left endpoint should be $-\infty$. However, the area under the curve is nearly negligible when Z is smaller than -4, so we will use -5 as the lower bound when not given a lower bound (any other negative number smaller than -5 will also work). Using a lower bound of -5 and an upper bound of 1.5, we get P(Z < 1.5) = 0.933.

GUIDED PRACTICE 0.6 Find the area under the normal curve to right of Z = 2.⁶

GUIDED PRACTICE 0.7

Find the area under the normal curve between -1.5 and 1.5. 7

EXAMPLE 0.8

Use a calculator to find the Z-score that corresponds to the 40th percentile.

Letting Area be 0.40, a calculator gives -0.253. This means that Z = -0.253 corresponds to the 40th percentile, that is, P(Z < -0.253) = 0.40.

GUIDED PRACTICE 0.9

Find the Z-score such that 20 percent of the area is to the right of that Z-score.⁸

⁵normalcdf gives the result without drawing the graph. To draw the graph, do 2nd VARS, DRAW, 1:ShadeNorm. However, beware of errors caused by other plots that might interfere with this plot.

 $^{^{6}}$ Now we want to shade to the right. Therefore our lower bound will be 2 and the upper bound will be 5 (or a number bigger than 5) to get P(Z > 2) = 0.023.

⁷Here we are given both the lower and the upper bound. Lower bound is -1.5 and upper bound is 1.5. The area under the normal curve between -1.5 and 1.5 = P(-1.5 < Z < 1.5) = 0.866.

EXAMPLE 0.10

In a large study of birth weight of newborns, the weights of 23,419 newborn boys were recorded.⁹ The distribution of weights was approximately normal with a mean of 7.44 lbs (3376 grams) and a standard deviation of 1.33 lbs (603 grams). The government classifies a newborn as having low birth weight if the weight is less than 5.5 pounds. What percent of these newborns had a low birth weight?

We find an area under the normal curve between -5 (or a number smaller than -5, e.g. -10) and a Z-score that we will calculate. There is no need to write calculator commands in a solution. Instead, continue to use standard statistical notation.

$$Z = \frac{5.5 - 7.44}{1.33}$$
$$= -1.49$$
$$P(Z < -1.49) = 0.068$$

Approximately 6.8% of the newborns were of low birth weight.

GUIDED PRACTICE 0.11 Approximately what percent of these babies weighed greater than 10 pounds?¹⁰

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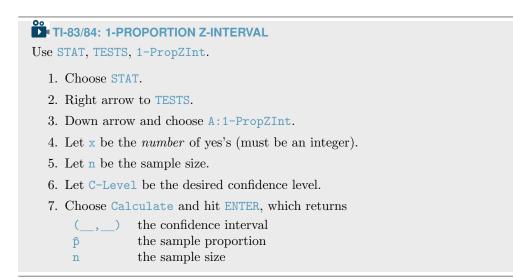
 $^{^{8}}$ If 20% of the area is the right, then 80% of the area is to the left. Letting area be 0.80, we get Z = 0.841.

⁹www.biomedcentral.com/1471-2393/8/5

 $^{{}^{10}}Z = \frac{10-7.44}{1.33} = 1.925$. Using a lower bound of 2 and an upper bound of 5, we get P(Z > 1.925) = 0.027. Approximately 2.7% of the newborns weighed over 10 pounds.

Inference for categorical data

1-proportion Z-interval and Z-test



TI-83/84: 1-PROPORTION Z-TEST

Use STAT, TESTS, 1-PropZTest.

- 1. Choose STAT.
- 2. Right arrow to TESTS.
- 3. Down arrow and choose 5:1-PropZTest.
- 4. Let p_0 be the null or hypothesized value of p.
- 5. Let \mathbf{x} be the *number* of yes's (must be an integer).
- 6. Let n be the sample size.
- 7. Choose \neq , <, or > to correspond to H_A.
- 8. Choose Calculate and hit ENTER, which returns
 - z Z-statistic
 - p p-value
 - \hat{p} the sample proportion
 - n the sample size

Practice exercises

GUIDED PRACTICE 0.12

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Using a calculator, evaluate the confidence interval from the example on intelligent life. Recall that we wanted to find a 95% confidence interval for the proportion of U.S. adults who think there is intelligent life on other planets. The sample percent was 68% and the sample size was 1,033.¹¹

GUIDED PRACTICE 0.13

Using a calculator, find the test statistic and p-value for the example on nuclear energy. Recall that we were looking for evidence that more than half of U.S. adults oppose nuclear energy. The sample percent was 54%, and the sample size was 1019.¹²

¹¹Navigate to 1-PropZInt on the calculator. To find x, the number of yes responses in the sample, we multiply the sample proportion by the sample size. Here $0.68 \times 1033 = 702.44$. We must round this to an integer, so we use x = 702. Also, n = 1033 and C-Level = 0.95. The 95% confidence interval is (0.651, 0.708).

¹²Navigate to 1-PropZTest on the calculator. Let $p_0 = 0.5$. To find x, do $0.54 \times 1019 = 550.26$. This needs to be an integer, so round to the closest integer. Here x = 550. Also, n = 1019. We are looking for evidence that greater than half oppose, so choose $> p_0$. When we do Calculate, we get the test statistic: Z = 2.64 and the p-value: p = 0.006.

2-proportion Z-interval and Z-test

TI-83/84: 2-PROPORTION Z-INTERVAL

Use STAT, TESTS, 2-PropZInt.

- 1. Choose STAT.
- 2. Right arrow to TESTS.
- 3. Down arrow and choose B:2-PropZInt.
- 4. Let x1 be the number of yes's (must be an integer) in sample 1 and let n1 be the size of sample 1.
- 5. Let x_2 be the *number* of yes's (must be an integer) in sample 2 and let n_2 be the size of sample 2.
- 6. Let C-Level be the desired confidence level.
- 7. Choose Calculate and hit ENTER, which returns:

(,)	the confidence interval	
p̂1	sample 1 proportion	

- sample 2 proportion ρ̂2
- size of sample 1 n_1 size of sample 2 n_2

TI-83/84: 2-PROPORTION Z-TEST

Use STAT, TESTS, 2-PropZTest.

1. Choose STAT.

z

 \hat{p}_1

- 2. Right arrow to TESTS.
- 3. Down arrow and choose 6:2-PropZTest.
- 4. Let x1 be the *number* of yes's (must be an integer) in sample 1 and let n1 be the size of sample 1.
- 5. Let x_2 be the *number* of yes's (must be an integer) in sample 2 and let n_2 be the size of sample 2.

p-value

- 6. Choose \neq , <, or > to correspond to H_A.
- 7. Choose Calculate and hit ENTER, which returns:
 - Z-statistic
 - р sample 1 proportion pooled sample proportion p
 - \hat{p}_2 sample 2 proportion

Practice exercises

GUIDED PRACTICE 0.14

A quality control engineer collects a sample of gears, examining 1000 gears from each company and finds that 879 gears pass inspection from the current supplier and 958 pass inspection from the prospective supplier. Use a calculator to find a 95% confidence interval for the difference (current – prospective) in the proportion that would pass inspection.¹³

GUIDED PRACTICE 0.15

Use a calculator to find the test statistic, p-value, and pooled proportion for a test with: H_A : p for fish oil < p for placebo.¹⁴

		heart attack	no event	Total
fisł	1 oil	145	12788	12933
pla	icebo	200	12738	12938

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¹³Navigate to 2-PropZInt on the calculator. Let x1 = 879, n1 = 1000, x2 = 958, and n2 = 1000. C-Level is .95. This should lead to an interval of (-0.1027, -0.0553), which matches what we found previously.

¹⁴Navigate to 2-PropZTest on the calculator. Correctly going through the calculator steps should lead to a solution with the test statistic z = -2.977 and the p-value p = 0.00145. These two values match our calculated values from the previous example to within rounding error. The pooled proportion is given as $\hat{p} = 0.0133$. Note: values for x1 and x2 were given in the table. If, instead, proportions are given, find x1 and x2 by multiplying the proportions by the sample sizes and rounding the result to an *integer*.

Finding areas under the chi-square curve

TI-84: FINDING AN UPPER TAIL AREA UNDER THE CHI-SQUARE CURVE

Use the χ^2 cdf command to find areas under the chi-square curve.

- 1. Hit 2ND VARS (i.e. DISTR).
- 2. Choose $8:\chi^2$ cdf.
- 3. Enter the lower bound, which is generally the chi-square value.
- 4. Enter the upper bound. Use a large number, such as 1000.
- 5. Enter the degrees of freedom.
- 6. Choose Paste and hit ENTER.

TI-83: Do steps 1-2, then type the lower bound, upper bound, and degrees of freedom separated by commas. e.g. $\chi^2 cdf(5, 1000, 3)$, and hit ENTER.

Chi-square goodness of fit test

TI-84: CHI-SQUARE GOODNESS OF FIT TEST

Use STAT, TESTS, χ^2 GOF-Test.

- 1. Enter the observed counts into list L1 and the expected counts into list L2.
- 2. Choose STAT.
- 3. Right arrow to TESTS.
- 4. Down arrow and choose $D: \chi^2 GOF$ -Test.
- 5. Leave Observed: L1 and Expected: L2.
- 6. Enter the degrees of freedom after df:
- 7. Choose Calculate and hit ENTER, which returns:
 - χ^2 chi-square test statistic
 - p p-value
 - df degrees of freedom

TI-83: Unfortunately the TI-83 does not have this test built in. To carry out the test manually, make list L3 = $(L1 - L2)^2 / L2$ and do 1-Var-Stats on L3. The sum of L3 will correspond to the value of χ^2 for this test.

Chi-square test for two-way tables

TI-83/84: ENTERING DATA INTO A TWO-WAY TABLE

- 1. Hit 2ND x^{-1} (i.e. MATRIX).
- 2. Right arrow to EDIT.
- 3. Hit 1 or ENTER to select matrix A.
- 4. Enter the dimensions by typing #rows, ENTER, #columns, ENTER.
- 5. Enter the data from the two-way table.

TI-83/84: CHI-SQUARE TEST OF HOMOGENEITY AND INDEPENDENCE

Use STAT, TESTS, χ^2 -Test.

- 1. First enter two-way table data as described in the previous box.
- 2. Choose STAT.
- 3. Right arrow to TESTS.
- 4. Down arrow and choose $C: \chi^2$ -Test.
- 5. Down arrow, choose Calculate, and hit ENTER, which returns
 - χ^2 chi-square test statistic
 - p p-value
 - df degrees of freedom

TI-83/84: FINDING THE EXPECTED COUNTS

- 1. First enter two-way table data as described previously.
- 2. Carry out the chi-square test of homogeneity or independence as described in previous box.
- 3. Hit 2ND x^{-1} (i.e. MATRIX).
- 4. Right arrow to EDIT.
- 5. Hit 2 to see matrix B.

This matrix contains the expected counts.

Practice exercises

GUIDED PRACTICE 0.16 Use a calculator to find the upper tail area for the the chi-square distribution with 5 degrees of freedom and a $\chi^2 = 5.1$.¹⁵

GUIDED PRACTICE 0.17

Use the table below and a calculator to find the χ^2 -statistic and p-value for chi-square goodness of fit test. 16

	Blue	Orange	Green	Yellow	Red	Brown
observed counts:	133	133	139	103	108	96
expected counts:	170.9	142.4	113.9	99.6	92.6	92.6

GUIDED PRACTICE 0.18

The table below shows approval numbers, based on a random sample conducted by the Pew Research poll. Use a calculator to find the expected values and the χ^2 -statistic, df, and p-value for the chi-square test for independence.¹⁷

		Congress				
	Obama	Democrats	Republicans	Total		
Approve	842	736	541	2119		
Disapprove	616	646	842	2104		
Total	1458	1382	1383	4223		

¹⁵Use a lower bound of 5.1, an upper bound of 1000, and df = 5. The upper tail area is 0.4038.

¹⁶Enter the observed counts into L1 and the expected counts into L2. the GOF test. Make sure that ⁰⁵Deserved: is L1 and Expected: is L2. Let df: be 5. You should find that $\chi^2 = 17.36$ and p-value = 0.004. ¹⁷First create a 2 × 3 matrix with the data. The final summaries should be $\chi^2 = 106.4$, p-value is $p = 8.06 \times 10^{-24} \approx 0$, and df = 2. Below is the matrix of expected values:

	Obama	Congr. Dem.	Congr. Rep.
Approve	731.59	693.45	693.96
Disapprove	726.41	688.55	689.04

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Inference for numerical data

1-sample *t*-test and *t*-interval

TI-83/84: 1-SAMPLE T-TEST

Use STAT, TESTS, T-Test.

- 1. Choose **STAT**.
- 2. Right arrow to TESTS.
- 3. Down arrow and choose 2:T-Test.
- 4. Choose Data if you have all the data or Stats if you have the mean and standard deviation.
- 5. Let μ_0 be the null or hypothesized value of μ .
 - If you choose Data, let List be L1 or the list in which you entered your data (don't forget to enter the data!) and let Freq be 1.
 - If you choose Stats, enter the mean, SD, and sample size.
- 6. Choose \neq , <, or > to correspond to H_A.
- 7. Choose Calculate and hit ENTER, which returns:
 - t t statistic Sx the sample standard deviation
 - p-value n the sample size
 - $\bar{\mathbf{x}}$ the sample mean

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TI-83/84: 1-SAMPLE T-INTERVAL

Use STAT, TESTS, TInterval.

- 1. Choose STAT.
- 2. Right arrow to TESTS.
- 3. Down arrow and choose 8:TInterval.
- 4. Choose Data if you have all the data or Stats if you have the mean and standard deviation.
 - If you choose Data, let List be L1 or the list in which you entered your data (don't forget to enter the data!) and let Freq be 1.
 - If you choose Stats, enter the mean, SD, and sample size.
- 5. Let C-Level be the desired confidence level.
- 6. Choose Calculate and hit ENTER, which returns:

(,)	the confidence interval
x	the sample mean
Sx	the sample SD
n	the sample size

Practice exercises

GUIDED PRACTICE 0.19

(G)

(G)

The average time for all runners who finished the Cherry Blossom Run in 2006 was 93.3 minutes. In 2017, the average time for 100 randomly selected participants was 97.3, with a standard deviation of 17.0 minutes. Use a calculator to find the T-statistic and p-value for the appropriate test to see if the average time for the participants in 2017 is different than it was in 2006.¹⁸

GUIDED PRACTICE 0.20

Use a calculator to find a 95% confidence interval for the mean mercury content in croaker white fish (Pacific). The sample size was 15, and the sample mean and standard deviation were computed as 0.287 and 0.069 ppm (parts per million), respectively.¹⁹

¹⁸Navigate to T-Test. Let μ_0 be 93.3. $\bar{\mathbf{x}}$ is 97.3, $S_{\mathbf{x}}$ is 17.0, and $\mathbf{n} = 100$. Choose \neq to correspond to H_A . We get $\mathbf{t} = 2.353$ and the p-value $\mathbf{p} = 0.021$. The df = 100 - 1 = 99.

¹⁹Navigate to TInterval. We do not have all the data, so choose Stats. Enter \bar{x} and Sx. Note: Sx is the sample standard deviation (0.069), not the SE of the sample mean. Let n = 15 and C-Level = 0.95. This should give the interval (0.249, 0.325). The df = 15 - 1 = 14

Matched pairs *t*-test and *t*-interval

TI-83/84: MATCHED PAIRS T-TEST Use STAT, TESTS, T-Test. 1. Choose STAT. 2. Right arrow to TESTS. 3. Down arrow and choose 2:T-Test. 4. Choose Data if you have all the data or Stats if you have the mean and standard deviation. 5. Let μ_0 be the null or hypothesized value of μ_{diff} . • If you choose Data, let List be L3 or the list in which you entered the differences (don't forget to enter the differences!) and let Freq be 1. • If you choose Stats, enter the mean, SD, and sample size of the differences. 6. Choose \neq , <, or > to correspond to H_A. 7. Choose Calculate and hit ENTER, which returns: t statistic t р p-value the sample mean of the differences Ī the sample SD of the differences Sxn the sample size of the differences **TI-83/84: MATCHED PAIRS T-INTERVAL**

Use STAT, TESTS, TInterval.

- 1. Choose STAT.
- 2. Right arrow to TESTS.
- 3. Down arrow and choose 8:TInterval.
- 4. Choose Data if you have all the data or Stats if you have the mean and standard deviation.
 - If you choose Data, let List be L3 or the list in which you entered the differences (don't forget to enter the differences!) and let Freq be 1.
 - If you choose Stats, enter the mean, SD, and sample size of the differences.
- 5. Let C-Level be the desired confidence level.
- 6. Choose Calculate and hit ENTER, which returns:

(__,__) the confidence interval for the mean of the differences

- $\bar{\mathbf{x}}$ the sample mean of the differences
- Sx the sample SD of the differences
- n the number of differences in the sample

(G)

G

Practice exercises

GUIDED PRACTICE 0.21

In our UCLA textbook example, we had 68 paired differences. Because df = 67 was not on our t-table, we rounded the df down to 60. This gave us a 95% confidence interval (0.325, 6.834). Use a calculator to find the more exact 95% confidence interval based on 67 degrees of freedom. How different is it from the one we calculated based on 60 degrees of freedom?²⁰

$n_{\scriptscriptstyle diff}$	$ar{x}_{\scriptscriptstyle diff}$	$s_{\scriptscriptstyle diff}$
68	3.58	13.42

GUIDED PRACTICE 0.22 Use the data in the table above to find the test statistic and p-value for a test of H_0 : $\mu_{diff} = 0$ versus H_A : $\mu_{diff} \neq 0.^{21}$

²⁰Navigate to TInterval. We do not have all the data, so choose Stats. Enter $\bar{x} = 3.58$ and Sx = 13.42. Let n = 68 and C-Level = 0.95. This should give the interval (0.332, 6.828). The intervals are equivalent when rounded to two decimal places.

²¹Navigate to T-Test. We do not have all the data, so choose Stats. Enter $\mu_0 = 0$, $\bar{x} = 3.58$, Sx = 13.42, n = 68, and choose $\neq \mu_0$ since the alternative hypothesis is two-sided. This should give the interval t = 2.2 and p = 0.031.

2-sample *t*-test and *t*-interval

TI-83/84: 2-SAMPLE T-TEST

Use STAT, TESTS, 2-SampTTest.

- 1. Choose STAT.
- 2. Right arrow to TESTS.
- 3. Choose 4:2-SampTTest.
- 4. Choose Data if you have all the data or Stats if you have the means and standard deviations.
 - If you choose Data, let List1 be L1 or the list that contains sample 1 and let List2 be L2 or the list that contains sample 2 (don't forget to enter the data!). Let Freq1 and Freq2 be 1.
 - If you choose **Stats**, enter the mean, SD, and sample size for sample 1 and for sample 2
- 5. Choose \neq , <, or > to correspond to H_A.
- 6. Let Pooled be NO.
- 7. Choose Calculate and hit ENTER, which returns:
 - tt statisticSx1SD of sample 1pp-valueSx2SD of sample 2dfdegrees of freedomn1size of sample 1
 - $\bar{\mathbf{x}}_1$ mean of sample 1 n2
- size of sample 1 size of sample 2
 - $\bar{\mathbf{x}}_2$ mean of sample 2

TI-83/84: 2-SAMPLE T-INTERVAL

Use STAT, TESTS, 2-SampTInt.

- 1. Choose STAT.
- 2. Right arrow to TESTS.
- 3. Down arrow and choose 0:2-SampTTInt.
- 4. Choose Data if you have all the data or Stats if you have the means and standard deviations.
 - If you choose Data, let List1 be L1 or the list that contains sample 1 and let List2 be L2 or the list that contains sample 2 (don't forget to enter the data!). Let Freq1 and Freq2 be 1.
 - If you choose **Stats**, enter the mean, SD, and sample size for sample 1 and for sample 2.
- 5. Let C-Level be the desired confidence level and let Pooled be No.

6. Choose Calculate and hit ENTER, which returns:

(,)	the confidence interval	Sx1	SD of sample 1
df	degrees of freedom	Sx2	SD of sample 2
\bar{x}_1	mean of sample 1	n1	size of sample 1
\bar{x}_2	mean of sample 2	n2	size of sample 2

Practice exercises

GUIDED PRACTICE 0.23

Use the data below and a calculator to find the test statistics and p-value for a one-sided test, testing whether there is evidence that embryonic stem cells (ESCs) help improve heart function for sheep that have experienced a heart attack.²²

	n	\bar{x}	s
ESCs	9	3.50	5.17
$\operatorname{control}$	9	-4.33	2.76

GUIDED PRACTICE 0.24

Use the data below and a calculator to find a 95% confidence interval for the difference in average scores between Version A and Version B of the exam from the previous example.²³

Version	n	\bar{x}	s	\min	max
A	30	79.4	14	45	100
В	30	74.1	20	32	100

(G)

(G)

²²Navigate to 2-SampTTest. Because we have the summary statistics rather than all of the data, choose Stats. Let $\bar{x}1=3.50$, Sx1=5.17, n1=9, $\bar{x}2=-4.33$, Sx2=2.76, and n2=9. We get t = 4.01, and the p-value $p = 8.4 \times 10^{-4} = 0.00084$. The degrees of freedom for the test is df = 12.2.

²³Navigate to 2-SampTInt. Because we have the summary statistics rather than all of the data, choose Stats. Let $\bar{x}1=79.41$, Sx1=14, n1=30, $\bar{x}2=74.1$, Sx2=20, and n2=30. The interval is (-3.6, 14.2) with df = 51.9.

Introduction to linear regression

Finding b_0 , b_1 , R^2 , and r for a linear model

TI-84: FINDING b_0 , b_1 , R^2 , AND r FOR A LINEAR MODEL Use STAT, CALC, LinReg(a + bx).

- 1. Choose STAT.
- 2. Right arrow to CALC.
- 3. Down arrow and choose 8:LinReg(a+bx).
 - Caution: choosing 4:LinReg(ax+b) will reverse a and b.
- 4. Let Xlist be L1 and Ylist be L2 (don't forget to enter the x and y values in L1 and L2 before doing this calculation).
- 5. Leave FreqList blank.
- 6. Leave Store RegEQ blank.
- 7. Choose Calculate and hit ENTER, which returns:
 - a b_0 , the y-intercept of the best fit line
 - **b** b_1 , the slope of the best fit line
 - $\mathbf{r}^2 = R^2$, the explained variance
 - \mathbf{r} r, the correlation coefficient

TI-83: Do steps 1-3, then enter the x list and y list separated by a comma, e.g. LinReg(a+bx) L1, L2, then hit ENTER.

What to do if r^2 and r do not show up on a TI-83/84

WHAT TO DO IF r^2 AND r DO NOT SHOW UP ON A TI-83/84

If r^2 and r do now show up when doing STAT, CALC, LinReg, the *diagnostics* must be turned on. This only needs to be once and the diagnostics will remain on.

- 1. Hit 2ND 0 (i.e. CATALOG).
- 2. Scroll down until the arrow points at DiagnosticOn.
- 3. Hit ENTER and ENTER again. The screen should now say: DiagnosticOn

Done

What to do if a TI-83/84 returns: ERR: DIM MIS-MATCH

WHAT TO DO IF A TI-83/84 RETURNS: ERR: DIM MISMATCH

This error means that the lists, generally L1 and L2, do not have the same length.

- 1. Choose 1:Quit.
- 2. Choose STAT, Edit and make sure that the lists have the same number of entries.

Practice exercises

GUIDED PRACTICE 0.25

The data set 10an50, introduced in Chapter 1, contains information on randomly sampled loans offered through the Lending Club. A subset of the data matrix is shown in Figure 1. Use a calculator to find the equation of the least squares regression line for predicting loan amount from total income.²⁴

	$total_income$	loan_amount
1	59000	22000
2	60000	6000
3	75000	25000
4	75000	6000
5	254000	25000
6	67000	6400
7	28800	3000

Figure 1:	Sample	of o	lata	from	loan50.
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 $^{^{24}}a = 11121$ and b = 0.0043, therefore $\hat{y} = 11121 + 0.0043x$.

Linear regression *t*-test and *t*-interval

TI-83/84: LINEAR REGRESSION T-TEST ON β_1

Use STAT, TESTS, LinRegTTest.

- 1. Choose STAT.
- 2. Right arrow to TESTS.
- 3. Down arrow and choose F:LinRegTest. (On TI-83 it is E:LinRegTTest).
- 4. Let Xlist be L1 and Ylist be L2. (Don't forget to enter the x and y values in L1 and L2 before doing this test.)
- 5. Let Freq be 1.
- 6. Choose \neq , <, or > to correspond to H_A.
- 7. Leave RegEQ blank.

8. Choose Calculate and hit ENTER, which returns:

- t t statistic
- p p-value

- b_1 , slope of the line
- s st. dev. of the residuals
- df degrees of freedom for the test $r^2 R^2$, explained variance

b

- b_0 , y-intercept of the line
- \mathbf{r} r, correlation coefficient

TI-84: T-INTERVAL FOR β_1

Use STAT, TESTS, LinRegTInt.

1. Choose STAT.

a

- 2. Right arrow to TESTS.
- 3. Down arrow and choose G: LinRegTest.
 - This test is not built into the TI-83.
- 4. Let Xlist be L1 and Ylist be L2. (Don't forget to enter the x and y values in L1 and L2 before doing this interval.)
- 5. Let Freq be 1.
- 6. Enter the desired confidence level.
- 7. Leave RegEQ blank.
- 8. Choose Calculate and hit ENTER, which returns:

(,)	the confidence interval
Ъ	b_1 , the slope of best fit line of the sample data
df	degrees of freedom associated with this confidence interval
S	standard deviation of the residuals
a	b_0 , the y-intercept of the best fit line of the sample data
r^2	R^2 , the explained variance
r	r, the correlation coefficient