# List of mathematical symbols

This is a list of symbols used in all branches of mathematics to express a formula or to represent aconstant.

A mathematical concept is independent of the symbol chosen to represent it. For many of the symbols below, the symbol is usually synonymous with the corresponding concept (ultimately an arbitrary choice made as a result of the cumulative history of mathematics), but in some situations, a different convention may be used. For example, depending on context, the triple bar "=" may represent congruence or a definition. However, in mathematical logic, numerical equality is sometimes represented by "=" instead of "=", with the latter representing equality of well-formed formulas of the symbols below, the symbol is usually synonymous with the corresponding concept (ultimately an arbitrary choice made as a result of the cumulative history of mathematics), but in some situations, a different convention may be used. For example, depending on context, the triple bar "=" may represent congruence or a definition. However, in mathematical logic, numerical equality is sometimes represented by "=" instead of "=", with the latter representing equality of well-formed formulas of the symbol symbols are sufficient to the cumulative history of mathematics and the symbols are sufficient to the cumulative history of mathematics and the symbols are sufficient to the sym

Each symbol is shown both in HTML, whose display depends on the browser's access to an appropriate font installed on the particular device, and typeset as an image usingx.

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#### Guide

This list is organized by symbol type and is intended to facilitate finding an unfamiliar symbol by its visual appearance. For a related list organized by mathematical topic, see <u>List of mathematical</u> symbols by subject That list also includes La\(\frac{1}{2}\)X and HTML markup, and Unicode code points for each symbol (notethat this article doesn't have the latter two, but they could certainly be added).

There is a Wikibooks guide for using maths in LaTeX,<sup>[1]</sup> and a comprehensive LaTeX symbol list.<sup>[2]</sup> It is also possible to check to see if a Unicode code point is available as a LaTeX command, or vice versa.<sup>[3]</sup> Also note that where there is no LaTeX command natively available for a particular symbol (although there may be options that require adding packages), the symbol could be added via other options, such as setting the document up to support Unicode,<sup>[4]</sup> and entering the character in a variety of ways (e.g. copying and pasting, keyboard shortcuts, the \unicode{<insertcodepoint>} command<sup>[5]</sup>) as well as other options<sup>[6]</sup> and extensive additional information.<sup>[7]</sup>[8]

- Basic symbols: Symbols widely used in mathematics, roughly through first-year calculus. More advanced meanings are included with some symbols listed here.
- Symbols based on equality "=": Symbols derived from or similar to the equal sign, including double-headed arrows. Not surprisingly these symbols are often associated with ar equivalence relation
- Symbols that point left or right:Symbols, such as < and >, that appear to point to one side or another
- Brackets: Symbols that are placed on either side of a variable or expression, such alx.
- Other non-letter symbols: Symbols that do not fall in any of the other categories.
- Letter-based symbols:Many mathematical symbols are based on, or closely resemble, a letter in some alphabet. This section includes such symbols, including symbols that resemble upside-down letters. Many letters have conventional meanings in various branches of mathematics and physics. These are not listed here. See also section, below has several lists of such usages.
  - Letter modifiers: Symbols that can be placed on or next to any letter to modify the letter's meaning.
  - Symbols based on <u>Latin letters</u>, including those symbols that resemble or contain anX
- Variations: Usage in languages written right-to-left

## **Basic symbols**

	Name Name					
Symbol	Symbol	Read as	Explanation	Examples		
in <u>HTML</u>	in <u>TeX</u>		Explanation	Examples		
		Category				
		addition				
		plus; add	4 + 6 means the sum of 4 and 6.	2 + 7 = 9		
		arithmetic				
+	+	disjoint union				
		the disjoint	$A_1 + A_2$ means the disjoint union of	$A_1 = \{3, 4, 5, 6\} \land A_2 = \{7, 8, 9, 10\} \Rightarrow$		
		union of and	sets $A_1$ and $A_2$ .	$A_1 + A_2 = \{(3, 1), (4, 1), (5, 1), (6, 1), (7, 2), (8, 2), (9, 2), (10, 2)\}$		
		set theory				
		subtraction				
		minus;	36 – 11 means the subtraction of11			
		take;	from 36.	36 – 11 = 25		
		subtract arithmetic				
		negative sign				
		negative;				
_	_	minus;	-3 means the additive inverse of the	-(-5) = 5		
_		the opposite of	number 3.	( 3) 3		
		arithmetic				
		set-theoretic	A - B means the set that contains all			
		complement	the elements of $A$ that are not in $B$ .			
		minus; without	(\ can also be used for set-theoretic	${1, 2, 4} - {1, 3, 4} = {2}$		
		set theory	complement as described below)			
		plus-minus	•			
		plus or minus	$6 \pm 3$ means both $6 + 3$ and $6 - 3$ .	The equation $x = 5 \pm \sqrt{4}$ , has two solutions, $x = 7$ and $x = 3$ .		
	±	arithmetic				
<u>±</u>	\pm	plus-minus	$10 \pm 2$ or equivalently $10 \pm 20\%$			
		plus or minus	means the range from 10 - 2 to	If $a = 100 \pm 1$ mm, then $a \ge 99$ mm and $a \le 101$ mm.		
		measurement	10 + 2.			
- I	<b>手</b>	minus-plus	$6 \pm (3 \mp 5)$ means $6 + (3 - 5)$ and			
<u> </u>	<del>T</del> \mp	minus or plus arithmetic	6 - (3 + 5).	$\cos(x \pm y) = \cos(x)\cos(y) \mp \sin(x)\sin(y).$		
		multiplication				
		times;	$3 \times 4$ or $3 \cdot 4$ means the multiplication	T 0 50		
		multiplied by	of 3 by 4.	$7 \cdot 8 = 56$		
		arithmetic				
		dot product scalar product				
		dot	${f u}\cdot{f v}$ means the dot product ofvectors			
		linear algebra		$(1, 2, 5) \cdot (3, 4, -1) = 6$		
<u>×</u>	×	vector				
	\times	algebra cross product				
_		vector				
	\cdot	product	$\mathbf{u} \times \mathbf{v}$ means the cross product of	$(1, 2, 5) \times (3, 4, -1) = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 1 & 2 & 5 \end{vmatrix} = (-22, 16, -2)$		
·		cross	vectors $\mathbf{u}$ and $\mathbf{v}$	$(1, 2, 5) \times (3, 4, -1) = $ $\begin{vmatrix} 1 & 2 & 5 \\ 3 & 4 & -1 \end{vmatrix} = (-22, 16, -2)$		
		linear algebra vector		3 4 -1		
		algebra				
		placeholder	A · means a placeholder for an			
		(silent)	argument of a function. Indicates the functional nature of an expression	1.1		
		functional	without assigning a specific symbol for			
		analysis	an argument.			
		division (Obelus)		$2 \div 4 = 0.5$		
		divided by;	$6 \div 3$ or $6/3$ means the division of $6$			
		over	by 3.	12/4 = 3		
÷	÷	arithmetic				
_	\div	quotient group	G/H means the quotient of group $G$			
/	/	mod	G / H means the quotient of group $G$ modulo its subgroup $H$ .	$ \{0, a, 2a, b, b + a, b + 2a\} / \{0, b\} = \{\{0, b\}, \{a, b + a\}, \{2a, b + 2a\}\} $		
-	,	group theory				
		quotient set	$A/\sim$ means the set of all $\sim$ equivalence	If we define $\sim$ by $x \sim y \Leftrightarrow x - y \in \mathbb{Z}$ , then		
		mod	classes in A.	$\mathbb{R}/\sim = \{x+n: n \in \mathbb{Z}, x \in [0,1)\}.$		
		set theory				
		square root (radical				
		symbol)	$\sqrt{x}$ means the nonnegative number	$\sqrt{4} = 2$		
		the (principal) square root of	whose square is $x$ .	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\		
,	√ \surd	real numbers				
$\frac{}{}$	$\sqrt{x}$	complex				
	\sqrt{x}	square root	If $z = r \exp(i\omega)$ is represented in rela-			
		the (complex)	If $z = r \exp(i\varphi)$ is represented in <u>polar</u> coordinates with $-\pi < \varphi \le \pi$ , then	$\sqrt{-1} = i$		
		square root of complex	$\sqrt[4]{z} = \sqrt{r} \exp(i\varphi/2).$			
		numbers				
Σ	Σ	summation				
	_	I				

	\sum	sum over from to of calculus	$\sum_{k=1}^n a_k$ means $a_1+a_2+\cdots+a_n$ .	$\sum_{k=1}^{4} k^2 = 1^2 + 2^2 + 3^2 + 4^2 = 1 + 4 + 9 + 16 = 30$
	indefinitintegral antiderivintegral antiderivintegral indefinitegral communication of the antiderivintegral communication of case and case and case antiderivintegral communication of case and		$\int f(x) dx$ means a function whose derivative is $f$ .	$\int x^2 dx = \frac{x^3}{3} + C$
Ţ	∫ ∖int	definite integral integral from to of with respect to calculus	$\int_a^b f(x) dx$ means the signed area between the $x$ -axis and the graph of the function $f$ between $x = a$ and $x = b$ .	$\int_{a}^{b} x^{2} dx = \frac{b^{3} - a^{3}}{3}$
		line integral line/ path/ curve/ integral of along calculus	$\int_C f ds$ means the integral of along the curve $C$ , $\int_a^b f(\mathbf{r}(t))  \mathbf{r}'(t)  dt$ , where $\mathbf{r}$ is a parametrization of $C$ . (If the curve is closed, the symbol $\int_a^{\infty}$ may be used instead, as described below)	
ø	<b>∮</b> \oint	Contour integral; closed line integral contour integral of calculus	Similar to the integral, but used to denote a single integration over a closed curve or loop. It is sometimes used in physics texts involving equations regarding Gauss's Law, and while these formulas involve a closed surface integral, the representations describe only the first integration of the volume over the enclosing surface. Instances where the latter requires simultaneous double integration, the symbol # would be more appropriate. A third related symbol is the closed volume integral, denoted by the symbol ##.  The contour integral can also frequently	If $C$ is a <u>Jordan curve</u> about 0, then $\oint_C \frac{1}{z} dz = 2\pi i$ .
:: :: ::	\ldots \cdots \text{!} \vdots \cdots \cdots	ellipsis and so forth everywhere	Indicates omitted values from a pattern.	<u>1/2 + 1/4 + 1/8 + 1/16 +···</u> = 1
<u>:</u>	∴ \therefore	therefore therefore; so; hence everywhere	Sometimes used in proofs before logical consequences	All humans are mortal. Socrates is a human∴ Socrates is mortal.
<u>:</u>	:· \because	because because; since everywhere	Sometimes used in proofs before reasoning.	11 is $\underline{\text{prime}}$ $\because$ it has no positive integer factors other than itself and one.
<u>!</u>	I	factorial factorial combinatorics logical	$n!$ means the product $1 \times 2 \times \cdots \times n$ .	$4! = 1 \times 2 \times 3 \times 4 = 24$
		negation not propositional logic	The statement A is true if and only if A is false.  A slash placed through another operator is the same as "!" placed in	$\begin{array}{l} \mathbb{I}(A) \Leftrightarrow A \\ x \neq y \Leftrightarrow \mathbb{I}(x = y) \end{array}$
		10900	front.  (The symbol! is primarily from computer science. It is avoided in mathematical texts, where the notation ¬A is preferred.)	

7 ~		logical negation not propositional logic	The statement ¬A is true if and only if A is false.  A slash placed through another operator is the same as "¬" placed in front.  (The symbol ¬ has many other uses, so ¬ or the slash notation is preferred. Computer scientists will often usel but this is avoided in mathematical texts)	$\neg(\neg A) \Leftrightarrow A$ $x \neq y \Leftrightarrow \neg(x = y)$
<u>α</u>		proportionality is proportional to; varies as everywhere	constant k.	if $y = 2x$ , then $y \propto x$ .
	∞ \infty	infinity infinity numbers	∞ is an element of the extended number line that is greater than all real numbers; it often occurs in limits.	$\lim_{x\to 0}\frac{1}{ x }=\infty$
	Box	end of proof QED; tombstone; Halmos finality symbol everywhere	Used to mark the end of a proof. (May also be written Q.E.D.)	

# Symbols based on equality

Symbol in <u>HTML</u>	Symbol in <u>TeX</u>	Read as  Category	Explanation	Examples
=	=	equality is equal to; equals everywhere	$oldsymbol{x} = oldsymbol{y}$ means $oldsymbol{x}$ and $oldsymbol{y}$ represent the same thing or value.	2 = 2  1 + 1 = 2  36 - 5 = 31
<u>≠</u>	<b>≠</b> \ne	inequality is not equal to; does not equal everywhere	$x \neq y$ means that $x$ and $y$ do not represent the same thing or value.  (The forms!=, $ =$ or <> are generally used in programming languages where ease of typing and use oASCII text is preferred.)	$2+2 \neq 5$ $36-5 \neq 30$
<b>≈</b>	≈ \approx	approximately equal is approximately equal to everywhere isomorphism is isomorphic to	$x \approx y$ means $x$ is approximately equal toy.  This may also be written $\approx$ , $\approx$ , $\sim$ , $\triangle$ (Libra Symbol), or $\rightleftharpoons$ .	$\pi \approx 3.14159$ $Q_8 / C_2 \approx V$
		group theory probability distribution has distribution statistics	( $\cong$ can also be used for isomorphic, as described below) $X \sim D, \text{ means the } \underline{\text{random variable}} X \text{ has the probability distribution } D.$	$X \sim N(0,1)$ , the <u>standard</u> normal distribution
		row equivalence is row equivalent to matrix theory	$A \sim B$ means that $B$ can be generated by using a series of elementary row operations on $A$	$\begin{bmatrix} 1 & 2 \\ 2 & 4 \end{bmatrix} \sim \begin{bmatrix} 1 & 2 \\ 0 & 0 \end{bmatrix}$
~_	~ \sim	same order of magnitude roughly similar; poorly approximates is on the order of approximation theory	$m \sim n$ means the quantities $m$ and $n$ have the same order of magnitude, or general size.  (Note that $\sim$ is used for an approximation that is poor otherwise use $\approx$ .)	$2 \sim 5$ $8 \times 9 \sim 100$ but $\pi^2 \approx 10$
		is similar to <sup>[9]</sup> geometry	$\triangle$ ABC ~ $\triangle$ DEF means triangle ABC is similar to (has the same shape) triangle DEF.	
		asymptotically equivalent is asymptotically equivalent to asymptotic analysis	$f \sim g$ means $\lim_{n \to \infty} \frac{f(n)}{g(n)} = 1$ .	x ~ x+1
		equivalence relation are in the same equivalence class everywhere	$a \sim b$ means $b \in [a]$ (and equivalently $a \in [b]$ ).	1 ~ 5 mod 4
=:	=:			
:= =	:= = \equiv			
= :⇔	:⇔ :\Leftrightarrow	is defined as; is equal by	x := y, y =: x  or  x = y  means  x  is defined to be another name fory, under certain assumptions taken in context.	$\cosh x := \frac{e^x + e^{-x}}{2}$
	≜ \triangleq	definition to everywhere	(Some writers use $\equiv$ to mean <u>congruence</u> ). $P \Leftrightarrow Q$ means $P$ is defined to be <u>logically equivalent</u> to $Q$ .	$[a,b] := a \cdot b - b \cdot a$
def	<pre>\overset{\underset{\mathrm{def}}</pre>			
÷	≐ \doteq	congruence		
~	≅	is congruent to geometry	$\triangle$ ABC $\cong$ $\triangle$ DEF means triangle ABC is congruent to (has the same measurements as) triangle DEF	
<b>≅</b>	\cong	isomorphic is isomorphic to abstract algebra	$G \cong H$ means that group $G$ is isomorphic (structurally identical) to group $H$ .  ( $\approx$ can also be used for isomorphic, as described above).	$\underline{V}\cong\underline{C_2}\timesC_2$
≣	≡ \equiv	congruence relation is congruent to modulo modular arithmetic	$a \equiv b \pmod{n}$ means $a - b$ is divisible by $n$	5 ≡ 2 (mod 3)
⇔	⇔ \Leftrightarrow ⇔ \iff	material equivalence if and only if;	$A \Leftrightarrow B$ means $A$ is true if $B$ is true and $A$ is false if $B$ is false.	$x + 5 = y + 2 \Leftrightarrow x + 3 = y$
$\leftrightarrow$	\iff ↔	iff propositional logic		

	\leftrightarrow				
:=	:= =:	Assignment is defined to be	A := b means $A$ is defined to have the value $b$ .	Let $a := 3$ , then f(x) := x + 3	
=:	·	everywhere			

# Symbols that point left or right

Symbol	Symbol	Read as	Explanation	Examples	
in <u>HTML</u>	in <u>TeX</u>		Explanation	Lampies	
		Category strict inequality			
		strict inequality is less than,	x < y means x is less than y.	3 < 4	
		is greater than	x > y means x is greater than y.	5 > 4	
<	<	order theory			
<u>&lt;</u> >	>	proper subgroup			
_		is a proper	H < G means $H$ is a proper subgroup of $G$ .	5Z < Z	
		subgroup of	The modulation of broken company is a	$A_3 < S_3$	
		group theory significant			
		(strict) inequality			
		is much less	" # " magne v is much lose than v		
		than,	$x \ll y$ means x is much less thany. $x \gg y$ means x is much greater thany.	0.003	
		is much greater than	, ,		
		order theory			
		asymptotic			
	«	comparison			
<u>≪</u> ≫	≪ ≫ \11	is of smaller order than,	$f \ll g$ means the growth of $f$ is asymptotically bounded by $g$ .	v	
≫	\dg \11	is of greater	(This is I. M. Vinogradov's notation. Another notation is the Big O notation, which looks like $f = O(q)$ .)	$x \ll e^x$	
	.99	order than	, ,		
		analytic number theory			
		absolute			
		continuity			
		is absolutely	$\mu \ll \nu$ means that $\mu$ is absolutely continuous with respect to $\nu$ , <i>i.e.</i> ,	If $c$ is the counting measure on $[0,1]$ and $\mu$ is	
		continuous with respect to	whenever $ u(A)=0$ , we have $\mu(A)=0$ .	the Lebesgue measure, then $\mu \ll c$ .	
		measure theory			
			$x \le y$ means $x$ is less than or equal to $y$ .		
		inequality is less than or	$x \ge y$ means x is greater than or equal toy.		
		equal to,	(The forms <= and >= are generally used in programming languages, where ease of typing and use of ASCII text is preferred.)	$3 \le 4$ and $5 \le 5$	
		is greater than or equal to	where ease or typing and use oinself text is preferred.	$5 \ge 4$ and $5 \ge 5$	
		order theory	(≦ and ≧ are also used by some writers to mean the same thing a≤ and		
			≥, but this usage seems to be less common).		
<	≤ ≥ \le \ge	subgroup	U < C mana I in a subgroup of C	$Z \le Z$	
<u>≤</u>		group theory	$H \leq G$ means $H$ is a subgroup of $G$ .	$A_3 \leq S_3$	
=		group tricory		If	
		reduction			
		is reducible to	A < P moone the problem A can be reduced to the result.	$\exists f \in F . \forall x \in \mathbb{N} . x \in A \Leftrightarrow f(x) \in B$	
		computational	$A \le B$ means the problem $A$ can be reduced to the problem $B$ . Subscripts can be added to the $\le$ to indicate what kind of reduction.	then	
		complexity			
		ancory		$A \leq_F B$	
		congruence			
		relation			
		is less than is greater than		$10a \equiv 5 \pmod{5}$ for $1 \le a \le 10$	
_	≦	modular			
<b>≅</b>	≦ ≧ \leqq	arithmetic			
≦	\geqq \geqq	vector inequality	$x \le y$ means that each component of vectorx is less than or equal to each corresponding component of vectory.		
		is less than or	$x \ge y$ means that each component of vectorx is greater than or equal to		
		equal is greater than or	each corresponding component of vectory.		
		equal	It is important to note that $x \le y$ remains true if every element is equal. However, if the operator is changed, $x \le y$ is true if and only if $x \ne y$ is also		
		order theory	true.		
		Karp reduction			
		is Karp reducible			
		to; is polynomial-			
		time many-one	$L_1 \prec L_2$ means that the problem $L_1$ is Karp reducible to $L_2$ .[10]	If $L_1 \prec L_2$ and $L_2 \in \underline{\mathbf{P}}$ , then $L_1 \in \mathbf{P}$ .	
	_	reducible to			
<		computational complexity			
>	\prec	theory			
	\succ	Nondominated			
		order			
		is nondominated by	$P \prec Q$ means that the elementP is nondominated by elementQ. $^{[11]}$	If $P_1 < Q_2$ then $\forall_i P_i \leq Q_i \land \exists P_i < Q_i$	
		Multi-objective			
		optimization			
◁	4	normal			
>	> \triangleleft	subgroup is a normal	$N \lhd G$ means that $N$ is a normal subgroup of group $G$ .	$Z(G) \lhd G$	
-	\triangleright	is a normal subgroup of	$\sim$ G means matry is a normal subgroup of groups.	∠(G) < G	
8.#v25C5		group theory			
◅		ideal			
◅ ▻		10.00.		1	
-		is an ideal of	$I \lhd R$ means that $I$ is an ideal of ring $R$ .	(2) ⊲ Z	
-			$I \lhd R$ means that $I$ is an ideal of ring $R$ .	(2) ⊲ Z	

		the antijoin of relational	there is not a tuple in S that is equal on their common attribute names.	
⇒ → ⊃	⇒ → ⊃ \Rightarrow \rightarrow	algebra material implication implies; if then propositional	$A \Rightarrow B$ means if $A$ is true then $B$ is also true; if $A$ is false then nothing is said about $B$ .  ( $\neg$ may mean the same as $\Rightarrow$ , or it may have the meaning for functions given below)  ( $\supset$ may mean the same as $\Rightarrow$ , [12] or it may have the meaning for superset	$x = 6 \Rightarrow x^2 - 5 = 36 - 5 = 31$ is true, but $x^2 - 5 = 36 - 5 = 31 \Rightarrow x = 6$ is in general false (since <i>x</i> could be -6).
	\supset <u>⊆</u>	logic, Heyting algebra subset	given below)	(A > D) C A
<u>C</u>	C \subseteq \subset	is a subset of set theory	(subset) $A \subseteq B$ means every element of $A$ is also an element of $B$ . [13] (proper subset) $A \subset B$ means $A \subseteq B$ but $A \neq B$ . (Some writers use the symbol $\subset$ as if it were the same as $\subseteq$ .)	$(A \cap B) \subseteq A$ $\mathbb{N} \subset \mathbb{Q}$ $\mathbb{Q} \subset \mathbb{R}$
⊇	⊇ ⊃ \supseteq \supset	is a superset of set theory	$A\supseteq B$ means every element of $B$ is also an element of $A$ . $A\supset B$ means $A\supseteq B$ but $A\neq B$ . (Some writers use the symbol $\supset$ as if it were the same as $\supseteq$ .)	$(A \cup B) \supseteq B$ $\mathbb{R} \supset \mathbb{Q}$
<b>©</b>	\Subset	compact embedding is compactly contained in set theory	$A \subseteq B$ means the closure of $B$ is a compact subset of $A$ .	$\mathbb{Q}\cap(0,1)\Subset[0,5]$
<u></u>	→ \to	function arrow from to set theory, type theory	$f: X \to Y$ means the function $f$ maps the set $X$ into the set $Y$ .	Let $f: \mathbb{Z} \to \mathbb{N} \cup \{0\}$ be defined by $f(x) := x^2$ .
H	→ \mapsto	maps to set theory	$f: a \mapsto b$ means the function $f$ maps the element $a$ to the element $b$ .	Let $f: x \mapsto x + 1$ (the successor function).
<b>←</b>	← \leftarrow	Converse implication if	$a \leftarrow b$ means that for the propositionsa and $b$ , if $b$ implies $a$ , then $a$ is the converse implication of $b$ . $a$ to the element $b$ . This reads as "a if b", or "not b without a". It is not to be confused with the assignment operator in computer science	
<:	<:	subtype is a subtype of type theory	$T_1 <: T_2$ means that $T_1$ is a subtype of $T_2$ .	If $S <: T$ and $T <: U$ then $S <: U$ (transitivity).
<.	<∙	is covered by order theory	x < y means that $x$ is covered by $y$ .	$\{1, 8\} \stackrel{\bullet}{\sim} \{1, 3, 8\}$ among the subsets of $\{1, 2,, 10\}$ ordered by containment.
þ	⊨ \vDash	entailment entails model theory	$A \models B$ means the sentence $A$ entails the sentence $B$ , that is in every model in which $A$ is true, $B$ is also true.	$A \models A \lor \neg A$
<b>-</b>	⊢ ∖vdash	inference infers; is derived from propositional logic, predicate logic	$x \vdash y$ means $y$ is derivable from $x$ .	$A \to B \vdash \neg B \to \neg A$
		partition is a partition of number theory	$p \vdash n$ means that $p$ is a partition of $n$ .	$(4,3,1,1) \vdash 9, \sum_{\lambda \vdash n} (f_{\lambda})^2 = n!$
<b>(</b>	⟨  \langle	the bra; the dual of Dirac notation	$\langle \varphi  $ means the dual of the vector $\psi \rangle$ , a <u>linear functional</u> which maps a ket   $\psi \rangle$ onto the inner product $\langle \varphi   \psi \rangle$ .	
}	} \rangle	ket vector the ket; the vector Dirac notation	arphi angle means the vector with label $arphi$ , which is in a Hilbert space.	A qubit's state can be represented as $\alpha 0\rangle+\beta 1\rangle$ , where $\alpha$ and $\beta$ are complex numbers s.t. $ \alpha ^2+ \beta ^2=1$ .

## **Brackets**

	Symbol n <u>HTML</u>	Symbol in <u>TeX</u>	Read as  Category	Explanation	Examples		
		{\\choose\}	combination, binomial coefficient n choose k	means (in the case of $n = positive$ integer) the number of combinations of $k$ elements drawn from a set of $n$ elements.  (This may also be written asC( $n$ , $k$ ), C( $n$ ; $k$ ), $n$ C $_k$ , $n$ C $_k$ , or	$         \begin{pmatrix} 36 \\ 5 \end{pmatrix} = \frac{36!/(36-5)!}{5!} = \frac{32 \cdot 33 \cdot 34 \cdot 35 \cdot 36}{1 \cdot 2 \cdot 3 \cdot 4 \cdot 5} = 376992 $		
I   I   I   I   I   I   I   I   I   I		\choose\	u multichoose	(when <i>u</i> is positive integer)	$\left( \binom{-5.5}{7} \right) = \frac{-5.5 \cdot -4.5 \cdot -3.5 \cdot -2.5 \cdot -1.5 \cdot5 \cdot .5}{1 \cdot 2 \cdot 3 \cdot 4 \cdot 5 \cdot 6 \cdot 7} = \binom{.5}{7} = \frac{1.5}{7}$		
			value; modulus absolute value of; modulus of numbers	complex plane) between x and zero.	-5  =  5  = 5   i   = 1		
		\ldots	norm or Euclidean length or magnitude Euclidean norm of		For $\mathbf{x} = (3, -4)$ $ \mathbf{x}  = \sqrt{3^2 + (-4)^2} = 5$		
			determinant determinant of	A  means the determinant of the matrixA	$\begin{vmatrix} 1 & 2 \\ 2 & 9 \end{vmatrix} = 5$		
			cardinality cardinality of; size of; order of	X  means the cardinality of the setX. (# may be used instead as described below)	{3, 5, 7, 9}  = 4.		
		\  \ldots \	norm of; length of linear algebra	space. <sup>[14]</sup>	x+y   \le   x   +   y		
			integer function nearest integer to	(This may also be written[x], [x], nint(x) or Round(x).)	1   = 1,   1.6   = 2,   -2.4   = -2,   3.49   = 3		
	<u>{</u> ,}	{,} {\{\!\ \}}\!	the set of		ℕ = { 1, 2, 3, }		
L   floor	{ }	\! { } \{\ \\\} \! {;} \{\\;\\}	the set of such that	$P(x)$ } is the same as $\{x : P(x)\}$ .	${n \in \mathbb{N} : n^2 < 20} = {1, 2, 3, 4}$		
[] $\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$	[]	floor  \[ \ldots \] \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \		equal to x.  (This may also be written[x], floor(x) or int(x).)	[4] = 4, [2.1] = 2, [2.9] = 2, [-2.6] = -3		
Integer function   Integer function   Integer function   Integer to   Integer to	[]	\lceil \ldots	ceiling ceiling	[x] means the ceiling of x, i.e. the smallest integer greater than or equal to x.	[4] = 4, [2.1] = 3, [2.9] = 3, [-2.6] = -2		
	l1	\lfloor \ldots	integer function nearest integer to	(This may also be written[x],   x  , nint(x) or Round(x).)	[2] = 2, [2.6] = 3, [-3.4] = -3, [4.49] = 4		
	[:]	[:]	degree of a field extension	[K:F] means the degree of the extension $K:F$ .			

		field theory equivalence			
		class	[a] means the equivalence class of a, i.e. $\{x : x \sim a\}$ , where $\sim$	Let $a \sim b$ be true iff $a \equiv b \pmod{5}$ .	
		the equivalence	is an <u>equivalence relation</u>	Then $[2] = \{, -8, -3, 2, 7,\}$ .	
		class of	$[a]_R$ means the same, but with $R$ as the equivalence relation.		
		abstract algebra	·		
		floor	[x] means the floor of x, i.e. the largest integer less than or		
		floor;	equal to x.		
		greatest integer;	(This may also be written[ $x$ ], floor( $x$ ) or int( $x$ ). Not to be	[3] = 3, [3.5] = 3, [3.99] = 3, [-3.7] = -4	
		entier	confused with the nearest integer function, as described		
		numbers	below.)		
		nearest integer	[x] means the nearest integer tox.		
		function		[2] = 2, [2.6] = 3, [-3.4] = -3, [4.49] = 4	
		nearest integer to	(This may also be written $[x]$ , $[ x ]$ , nint $(x)$ or Round $(x)$ . Not to be confused with the floor function, as described above).		
		numbers			
		lverson bracket			
[]	[]	1 if true, 0	[S] maps a true statementS to 1 and a false statementS to 0.	[0-5]-0 [7-0]-1 [2-6] 2 3 4N-1 [5-6] 2 3 4N-0	
<u>L 1</u>	[] [\] \!	otherwise	[5] maps a true statements to 1 and a raise statements to 0.	$[0=5]=0, [7>0]=1, [2 \in \{2,3,4\}]=1, [5 \in \{2,3,4\}]=0$	
[,]	[,]	propositional logic			
L , ]	[,]		$f[X]$ means $\{f(x): x \in X\}$ , the image of the function funder		
[,,]	[,,]	image of	the set $X \subseteq \underline{\text{dom}}(f)$ .		
L / / ]		under	(This may also be written asf(X) if there is no risk of	$\sin[\mathbb{R}] = [-1,1]$	
		everywhere	confusing the image off under X with the function application of X. Another notation is Im f, the image off under its domain.)		
		closed			
		closed	$[a,b] = \{x \in \mathbb{R} : a \le x \le b\}.$	0 and 1/2 are in the interval [0,1].	
		interval	$[a, b] = \{a \in \mathbb{R} : a \leq a \leq b\}.$	o and 1/2 are in the interval [0,1].	
		order theory			
		commutator			
		commutator	$[g, h] = g^{-1}h^{-1}gh$ (or $ghg^{-1}h^{-1}$ ), if $g, h \in G$ (a group).	$x^y = x[x, y]$ (group theory).	
		of group theory,	$[a, b] = ab - ba$ , if $a, b \in R$ (a <u>ring</u> or <u>commutative algebra</u> ).	[AB, C] = A[B, C] + [A, C]B (ring theory).	
		ring theory			
		triple scalar product			
		the triple			
		scalar product of	$[\mathbf{a}, \mathbf{b}, \mathbf{c}] = \mathbf{a} \times \mathbf{b} \cdot \mathbf{c}$ , the <u>scalar product</u> of $\mathbf{a} \times \mathbf{b}$ with $\mathbf{c}$ .	[a, b, c] = [b, c, a] = [c, a, b].	
		vector			
		calculus			
		function application			
		of	f(x) means the value of the function at the element $x$ .	If $f(x) := x^2 - 5$ , then $f(6) = 6^2 - 5 = 36 - 5 = 31$ .	
		set theory			
		image	$f(X)$ means { $f(x) : x \in X$ }, the image of the function f under the set $X \subseteq \text{dom}(f)$ .		
		image of	the set $X \subseteq \underline{\text{dom}}(f)$ .	$\sin(\mathbb{R}) = [-1,1]$	
			the set $X \subseteq \underline{dom}(f)$ . (This may also be written asf[X] if there is a risk of confusing the image off under X with the function application of X.	$\sin(\mathbb{R}) = [-1,1]$	
		image of under everywhere	the set $X \subseteq \underline{\text{dom}}(f)$ . (This may also be written asf[X] if there is a risk of confusing	$\sin(\mathbb{R}) = [-1,1]$	
		image of under	the set $X \subseteq \underline{\mathrm{dom}}(f)$ . (This may also be written asf[X] if there is a risk of confusing the image off under X with the function application of X. Another notation isIm f, the image off under its domain.)		
		image of under everywhere precedence grouping parentheses	the set $X \subseteq \underline{\mathrm{dom}}(f)$ .  (This may also be written $asf[X]$ if there is a risk of confusing the image off under $X$ with the function application of $X$ . Another notation is $Imf$ , the image off under its domain.)  Perform the operations inside the parentheses first.	$sin(\mathbb{R}) = [-1, 1]$ $(8/4)/2 = 2/2 = 1, \text{ but } 8/(4/2) = 8/2 = 4.$	
		image of under everywhere precedence grouping	the set $X \subseteq \underline{\mathrm{dom}}(f)$ .  (This may also be written $asf[X]$ if there is a risk of confusing the image off under $X$ with the function application of $X$ . Another notation is $Imf$ , the image off under its domain.)  Perform the operations inside the parentheses first.		
$\Omega$	() (\ ) \!	image of under everywhere precedence grouping parentheses everywhere tuple	the set $X \subseteq \underline{\mathrm{dom}}(f)$ .  (This may also be written $asf[X]$ if there is a risk of confusing the image off under $X$ with the function application of $X$ . Another notation is $Imf$ , the image off under its domain.)  Perform the operations inside the parentheses first.	(8/4)/2 = 2/2 = 1, but 8/(4/2) = 8/2 = 4.	
		image of under everywhere precedence grouping parentheses everywhere tuple tuple; n-tuple; ordered	the set $X \subseteq \underline{\mathrm{dom}}(f)$ .  (This may also be written asf[X] if there is a risk of confusing the image off under X with the function application of X. Another notation is Im f, the image off under its domain.)  Perform the operations inside the parentheses first.  An ordered list (or sequence, or horizontal vectoror row	(8/4)/2 = 2/2 = 1, but $8/(4/2) = 8/2 = 4$ . (a, b) is an ordered pair (or 2-tuple).	
<u>()</u> (,)	() (\ ) \! (,) (\ ,\ ) \!	image of under everywhere precedence grouping parentheses everywhere tuple tuple; n-tuple; ordered pair/triple/etc;	the set $X \subseteq \underline{\mathrm{dom}}(f)$ .  (This may also be written $asf[X]$ if there is a risk of confusing the image off under $X$ with the function application of $X$ . Another notation is $Imf$ , the image off under its domain.)  Perform the operations inside the parentheses first.  An ordered list (or sequence, or horizontal vectoror row vector) of values.  (Note that the notation $(a,b)$ is ambiguous: it could be an ordered pair or an open interval. Set theorists and computer	(8/4)/2 = 2/2 = 1, but $8/(4/2) = 8/2 = 4$ . (a, b) is an ordered pair (or 2-tuple). (a, b, c) is an ordered triple (or 3-tuple).	
		image of under everywhere precedence grouping parentheses everywhere tuple tuple; n-tuple; ordered	the set $X \subseteq \underline{\mathrm{dom}}(f)$ .  (This may also be written asf[X] if there is a risk of confusing the image off under X with the function application of X. Another notation isIm f, the image off under its domain.)  Perform the operations inside the parentheses first.  An ordered list (or sequence, or horizontal vectoror row vector) of values.  (Note that the notation (a,b) is ambiguous: it could be an ordered pair or an open interval. Set theorists and computer scientists often use angle brackets ( ) instead of	(8/4)/2 = 2/2 = 1, but $8/(4/2) = 8/2 = 4$ . (a, b) is an ordered pair (or 2-tuple).	
		image of under everywhere precedence grouping parentheses everywhere tuple tuple; n-tuple; ordered pair/triple/etc; row vector;	the set $X \subseteq \underline{\mathrm{dom}}(f)$ .  (This may also be written asf[X] if there is a risk of confusing the image off under X with the function application of X. Another notation isIm f, the image off under its domain.)  Perform the operations inside the parentheses first.  An ordered list (or sequence, or horizontal vectoror row vector) of values.  (Note that the notation $(a,b)$ is ambiguous: it could be an ordered pair or an open interval. Set theorists and computer scientists often use angle brackets ( ) instead of parentheses.)	(8/4)/2 = 2/2 = 1, but $8/(4/2) = 8/2 = 4$ . (a, b) is an ordered pair (or 2-tuple). (a, b, c) is an ordered triple (or 3-tuple).	
		image of under everywhere  precedence grouping parentheses everywhere  tuple tuple; n-tuple; ordered pair/triple/etc; row vector; sequence everywhere	the set $X \subseteq \underline{\mathrm{dom}}(f)$ .  (This may also be written asf[X] if there is a risk of confusing the image off under X with the function application of X. Another notation isIm f, the image off under its domain.)  Perform the operations inside the parentheses first.  An ordered list (or sequence, or horizontal vectoror row vector) of values.  (Note that the notation $(a,b)$ is ambiguous: it could be an ordered pair or an open interval. Set theorists and computer scientists often use angle brackets ( ) instead of parentheses.)	(8/4)/2 = 2/2 = 1, but $8/(4/2) = 8/2 = 4$ . (a, b) is an ordered pair (or 2-tuple). (a, b, c) is an ordered triple (or 3-tuple).	
		image of under everywhere  precedence grouping parentheses everywhere  tuple tuple; n-tuple; ordered pair/triple/etc; row vector; sequence everywhere	the set $X \subseteq \underline{\mathrm{dom}}(f)$ .  (This may also be written asf[X] if there is a risk of confusing the image off under X with the function application of X. Another notation isIm f, the image off under its domain.)  Perform the operations inside the parentheses first.  An ordered list (or sequence, or horizontal vectoror row vector) of values.  (Note that the notation $(a,b)$ is ambiguous: it could be an ordered pair or an open interval. Set theorists and computer scientists often use angle brackets ( ) instead of parentheses.)	(8/4)/2 = 2/2 = 1, but $8/(4/2) = 8/2 = 4$ . (a, b) is an ordered pair (or 2-tuple). (a, b, c) is an ordered triple (or 3-tuple).	
		image of under everywhere  precedence grouping parentheses everywhere  tuple tuple; n-tuple; ordered pair/triple/etc; row vector; sequence everywhere  highest common factor highest	the set $X \subseteq \underline{\mathrm{dom}}(f)$ .  (This may also be written asf[X] if there is a risk of confusing the image off under X with the function application of X. Another notation isIm f, the image off under its domain.)  Perform the operations inside the parentheses first.  An ordered list (or sequence, or horizontal vectoror row vector) of values.  (Note that the notation $(a,b)$ is ambiguous: it could be an ordered pair or an open interval. Set theorists and computer scientists often use angle brackets ( ) instead of parentheses.)	(8/4)/2 = 2/2 = 1, but $8/(4/2) = 8/2 = 4$ . (a, b) is an ordered pair (or 2-tuple). (a, b, c) is an ordered triple (or 3-tuple).	
		image of under everywhere  precedence grouping parentheses everywhere  tuple tuple; n-tuple; ordered pain/friple/etc; row vector; sequence everywhere  highest common factor	the set $X \subseteq \underline{\mathrm{dom}}(f)$ .  (This may also be written asf[X] if there is a risk of confusing the image off under X with the function application of X. Another notation isIm f, the image off under its domain.)  Perform the operations inside the parentheses first.  An ordered list (or sequence, or horizontal vectoror row vector) of values.  (Note that the notation $(a,b)$ is ambiguous: it could be an ordered pair or an open interval. Set theorists and computer scientists often use angle brackets ( ) instead of parentheses.)	(8/4)/2 = 2/2 = 1, but 8/(4/2) = 8/2 = 4.  (a, b) is an ordered pair (or 2-tuple). (a, b, c) is an ordered triple (or 3-tuple).  () is the empty tuple (or 0-tuple).	
		image of under everywhere  precedence grouping parentheses everywhere  tuple tuple; n-tuple; ordered pain/ftriple/etc; row vector; sequence everywhere  highest common factor highest common factor; greatest	the set X ⊆ dom(f).  (This may also be written asf[X] if there is a risk of confusing the image off under X with the function application of X. Another notation isIm f, the image off under its domain.)  Perform the operations inside the parentheses first.  An ordered list (or sequence, or horizontal vectoror row vector) of values.  (Note that the notation (a,b) is ambiguous: it could be an ordered pair or an open interval. Set theorists and computer scientists often use angle brackets ( ) instead of parentheses.)	(8/4)/2 = 2/2 = 1, but $8/(4/2) = 8/2 = 4$ . (a, b) is an ordered pair (or 2-tuple). (a, b, c) is an ordered triple (or 3-tuple).	
		image of under everywhere  precedence grouping parentheses everywhere  tuple tuple; n-tuple; ordered pair/triple/etc; row vector; sequence everywhere  highest common factor, greatest common divisor; hcf;	the set $X \subseteq \underline{\mathrm{dom}}(f)$ .  (This may also be written $asf[X]$ if there is a risk of confusing the image off under $X$ with the function application of $X$ . Another notation is $Im f$ , the image off under its domain.)  Perform the operations inside the parentheses first.  An ordered list (or sequence, or horizontal vectoror row vector) of values.  (Note that the notation $(a,b)$ is ambiguous: it could be an ordered pair or an open interval. Set theorists and computer scientists often use angle brackets $( )$ instead of parentheses.)	(8/4)/2 = 2/2 = 1, but 8/(4/2) = 8/2 = 4.  (a, b) is an ordered pair (or 2-tuple). (a, b, c) is an ordered triple (or 3-tuple).  () is the empty tuple (or 0-tuple).	
		image of under everywhere  precedence grouping parentheses everywhere  tuple tuple; n-tuple; ordered pair/triple/etc; row vector; sequence everywhere  highest common factor, ighest common factor; greatest common divisor; hcf; gcd	the set $X \subseteq \underline{\mathrm{dom}}(f)$ .  (This may also be written $asf[X]$ if there is a risk of confusing the image off under $X$ with the function application of $X$ . Another notation is $Im f$ , the image off under its domain.)  Perform the operations inside the parentheses first.  An ordered list (or sequence, or horizontal vectoror row vector) of values.  (Note that the notation $(a,b)$ is ambiguous: it could be an ordered pair or an open interval. Set theorists and computer scientists often use angle brackets $( )$ instead of parentheses.)	(8/4)/2 = 2/2 = 1, but 8/(4/2) = 8/2 = 4.  (a, b) is an ordered pair (or 2-tuple). (a, b, c) is an ordered triple (or 3-tuple).  () is the empty tuple (or 0-tuple).	
		image of under everywhere  precedence grouping parentheses everywhere  tuple tuple; n-tuple; ordered pair/triple/etc; row vector; sequence everywhere  highest common factor, greatest common divisor; hcf;	the set $X \subseteq \underline{\mathrm{dom}}(f)$ .  (This may also be written $asf[X]$ if there is a risk of confusing the image off under $X$ with the function application of $X$ . Another notation is $Im f$ , the image off under its domain.)  Perform the operations inside the parentheses first.  An ordered list (or sequence, or horizontal vectoror row vector) of values.  (Note that the notation $(a,b)$ is ambiguous: it could be an ordered pair or an open interval. Set theorists and computer scientists often use angle brackets $( )$ instead of parentheses.)	(8/4)/2 = 2/2 = 1, but 8/(4/2) = 8/2 = 4.  (a, b) is an ordered pair (or 2-tuple). (a, b, c) is an ordered triple (or 3-tuple).  () is the empty tuple (or 0-tuple).	
(,)	(,) (\ ,\ ) \!	image of under everywhere  precedence grouping parentheses everywhere  tuple tuple; n-tuple; ordered pain/triple/etc; row vector; sequence everywhere  highest common factor highest common factor; greatest common divisor; hcf; gcd number theory	the set $X \subseteq \underline{\mathrm{dom}}(f)$ .  (This may also be written $asf[X]$ if there is a risk of confusing the image off under $X$ with the function application of $X$ . Another notation is $Im f$ , the image off under its domain.)  Perform the operations inside the parentheses first.  An ordered list (or sequence, or horizontal vectoror row vector) of values.  (Note that the notation $(a,b)$ is ambiguous: it could be an ordered pair or an open interval. Set theorists and computer scientists often use angle brackets $( )$ instead of parentheses.)	(8/4)/2 = 2/2 = 1, but 8/(4/2) = 8/2 = 4.  (a, b) is an ordered pair (or 2-tuple). (a, b, c) is an ordered triple (or 3-tuple).  () is the empty tuple (or 0-tuple).	
	(,) (\ ,\ ) \!	image of under everywhere precedence grouping parentheses everywhere  tuple tuple; n-tuple; ordered pair/triple/etc; row vector; sequence everywhere  highest common factor highest common factor; greatest common divisor; hcf; gcd number theory open interval	the set $X \subseteq \underline{\mathrm{dom}}(f)$ .  (This may also be written asf[X] if there is a risk of confusing the image off under X with the function application of X. Another notation isIm f, the image off under its domain.)  Perform the operations inside the parentheses first.  An ordered list (or sequence, or horizontal vectoror row vector) of values.  (Note that the notation $(a,b)$ is ambiguous: it could be an ordered pair or an open interval. Set theorists and computer scientists often use angle brackets ( ) instead of parentheses.)  (a, b) means the highest common factor of and b.  (This may also be writtenhcf(a, b) or $\gcd(a, b)$ .)	(8/4)/2 = 2/2 = 1, but 8/(4/2) = 8/2 = 4.  (a, b) is an ordered pair (or 2-tuple). (a, b, c) is an ordered triple (or 3-tuple).  () is the empty tuple (or 0-tuple).  (3, 7) = 1 (they are coprime); (15, 25) = 5.	
(,)		image of under everywhere  precedence grouping parentheses everywhere  tuple tuple; n-tuple; ordered pain/triple/etc; row vector; sequence everywhere  highest common factor highest common factor; greatest common divisor; hcf; gcd number theory	the set $X \subseteq \underline{\mathrm{dom}}(f)$ .  (This may also be written $asf[X]$ if there is a risk of confusing the image off under $X$ with the function application of $X$ . Another notation is $Im f$ , the image off under its domain.)  Perform the operations inside the parentheses first.  An ordered list (or sequence, or horizontal vectoror row vector) of values.  (Note that the notation $(a,b)$ is ambiguous: it could be an ordered pair or an open interval. Set theorists and computer scientists often use angle brackets $( )$ instead of parentheses.)  ( $a,b$ ) means the highest common factor of and $b$ .  ( $Im f(x)$ ) means the highest common factor of and $Im f(x)$ .	(8/4)/2 = 2/2 = 1, but 8/(4/2) = 8/2 = 4.  (a, b) is an ordered pair (or 2-tuple). (a, b, c) is an ordered triple (or 3-tuple).  () is the empty tuple (or 0-tuple).  (3, 7) = 1 (they are coprime); (15, 25) = 5.	

	\!]			
(,]	(]\!  ,  ]\!]	left-open interval half-open interval; left-open interval order theory	$(a,b] = \{x \in \mathbb{R} : a < x \le b\}$	(-1, 7] and (-∞, -1]
[,[	[\\)\!	right-open interval half-open interval; right-open interval order theory	$[a,b) = \{x \in \mathbb{R} : a \leq x < b\}.$	[4, 18) and [1, +∞)
		inner product inner product of linear algebra	$\langle u,v \rangle$ means the inner product ofu and $v$ , where $u$ and $v$ are members of an inner product space  Note that the notation $\langle u,v \rangle$ may be ambiguous: it could mean the inner product or the linear span.  There are many variants of the notation, such as $\langle u   v \rangle$ and $\langle u   v \rangle$ , which are described below For spatial vectos, the dot product notation, $x \cdot y$ is common. For matrices, the colon notation $A : B$ may be used. As $\langle and \rangle$ can be hard to type, the more "keyboard friendly" forms and $\rangle$ are sometimes seen. These are avoided in mathematical texts.	The standard inner productbetween two vectors $x = (2, 3)$ and $y = (-1)$ is: $(x, y) = 2 \times -1 + 3 \times 5 = 13$
		average of statistics	let S be a subset of N for example, (S) represents the average of all the elements in S.	for a time series $y(t)$ $(t=1,2,)$ we can define the structure functions $S_q(\tau)$ : $S_q = \langle  g(t+\tau) - g(t) ^q \rangle_t$
()	() \langle\ \rangle \!	expectation value  the expectation value of probability theory	For a single discrete variable $x$ of a function $f(x)$ , the expectation value of $f(x)$ is defined as $\langle f(x) \rangle = \sum_x f(x) P(x)$ , and for a single continuous variable the expectation value of $f(x)$ is defined as $\langle f(x) \rangle = \int_x f(x) P(x)$ ; where $P(x)$ is the PDF of the variable $x$ . [16]	
(,)	\langle\ ,\ \rangle \!	linear span (linear) span of; linear hull of linear algebra	$\langle S \rangle$ means the span of $S \subseteq V$ . That is, it is the intersection of all subspaces of $V$ which contain $S$ . $\langle u_1, u_2, \rangle$ is shorthand for $\langle \{u_1, u_2,\} \rangle$ . Note that the notation $\langle u, v \rangle$ may be ambiguous: it could mean the inner product or the linear span. The span of $S$ may also be written as $Sp(S)$ .	$\left\langle \left( egin{smallmatrix} 1 \ 0 \ 0 \end{smallmatrix} \right), \left( egin{smallmatrix} 0 \ 1 \ 0 \end{smallmatrix} \right), \left( egin{smallmatrix} 0 \ 0 \end{smallmatrix} \right) \right angle = \mathbb{R}^3.$
		subgroup generated by a set the subgroup generated by group theory	$\langle S \rangle$ means the smallest subgroup of (where $S \subseteq G$ , a group) containing every element of $(g_1, g_2, \ldots)$ is shorthand for $(\{g_1, g_2, \ldots\})$ .	In $\underline{S_3}$ , $\langle (1\ 2) \rangle = \{id,\ (1\ 2)\}$ and $\langle (1\ 2\ 3) \rangle = \{id,\ (1\ 2\ 3), (1\ 3\ 2))\}$ .
		tuple tuple; n-tuple; ordered pair/triple/etc; row vector; sequence everywhere	An ordered list (or sequence, or horizontal vectoror row vector) of values.  (The notation (a,b) is often used as well)	$\langle a,b \rangle$ is an ordered pair (or 2-tuple). $\langle a,b,c \rangle$ is an ordered triple (or 3-tuple). $\langle b \rangle$ is the empty tuple (or 0-tuple).
( )	\  \  \  \  \  \  \  \  \  \  \  \  \  \	inner product	$\langle u \mid v \rangle$ means the inner product of $u$ and $v$ , where $u$ and $v$ are members of an inner product space $[17]$ ( $u \mid v$ ) means the same.  Another variant of the notation is $\langle u, v \rangle$ which is described	
(1)	( ) (\  \ ) \!	of linear algebra	above. For spatial vectors, the dot product notation, $x \cdot y$ is	

## Other non-letter symbols

Symbol	Symbol	Name		
in HTML	in TeX	Read as	Explanation	Examples
··· <u>·····</u>		Category		
		convolution		
		convolution;	full as making the constalistion off and a	(\$. \(\delta\) \(\begin{array}{cccccccccccccccccccccccccccccccccccc
			f * g means the convolution of $f$ and $g$ .	$(f*g)(t) = \int_0^t f(\tau)g(t-\tau) d\tau.$
		functional analysis		
		complex		
		conjugate	z* means the complex conjugate ofz.	
		conjugate	( $\overline{z}$ can also be used for the conjugate of z, as	$(3+4i)^* = 3-4i.$
		complex numbers		
			R* consists of the set of units of the ringR,	
		group of units the group of	along with the operation of multiplication.	$(\mathbb{Z}/5\mathbb{Z})^* = \{[1], [2], [3], [4]\}$
		units of	This may also be written DX as described	≃ C <sub>4</sub>
		ring theory	This may also be writtenR <sup>x</sup> as described above, or U(R).	
*	*	hyperreal		
_		numbers		
		the (set of) hyperreals	*R means the set of hyperreal numbers.  Other sets can be used in place of R.	*N is the hypernatural numbers.
		non-standard	•	
		analysis		
		Hodge dual	*v means the Hodge dual of a vectory. If $v$	_
		Hodge dual;	is a <u>k-vector</u> within an <u>n-dimensional</u> <u>oriented</u>	If $\{e_i\}$ are the standard basis vectors of $\mathbb{R}^5$ ,
		Hodge star linear algebra	inner product space, then $*v$ is an $(n-k)$ -vector.	$*(e_1 \wedge e_2 \wedge e_3) = e_4 \wedge e_5$
		Kleene star		
		Kleene star	Corresponds to the usage of * inregular expressions. If $\Sigma$ is a set of strings, then $\Sigma$ * is	If $\Sigma = ('a', 'b', 'c')$ then $\Sigma^*$ includes ", 'a', 'ab', 'aba',
		computer	the set of all strings that can be created by	etc. The full set cannot be enumerated here since
		science,	concatenating members of ∑. The same string can be used multiple times, and the	countably infinite, but each individual string must h finite length.
		mathematical logic	empty string is also a member of $\Sigma^*$ .	, and the second
		proportionality		
		is proportional	v manna that v = lov for some constantly	if w = 2w them was
		to; varies as	$y \propto x$ means that $y = kx$ for some constant $k$ .	if $y = 2x$ , then $y \propto x$ .
		everywhere		
		Karp		
α.	<u>«</u>	reduction <sup>[18]</sup>		
_	\propto \!	is Karp reducible to;		
		is polynomial-	$A \propto B$ means the problem A can be	If $L_1 \propto L_2$ and $L_2 \in \mathbf{P}$ , then $L_1 \in \mathbf{P}$ .
		time many-one reducible to	polynomially reduced to the problemB.	
		computational		
		complexity		
		set-theoretic		
		complement	$A \setminus B$ means the set that contains all those	
\	\	minus; without;	elements of $A$ that are not in $B$ . [13]	(1 2 2 4) \ (2 4 5 6) = (1 2)
`	\setminus	throw out;	(– can also be used for set-theoretic	{1,2,3,4} \ {3,4,5,6} = {1,2}
		not	complement as described above)	
		set theory		
		conditional event	P(A B) means the probability of the eventA	if X is a uniformly random day of the year P(X is M
		given	occurring given that B occurs.	X is in May) = 1/31
		probability		
		restriction		
1	,	restriction of	$f _A$ means the function $f$ is restricted to the	The function $f: \mathbf{R} \to \mathbf{R}$ defined by $f(x) = x^2$ is not inj
I	'	to; restricted to	set $A$ , that is, it is the function withdomain $A \cap dom(f)$ that agrees with $f$ .	but $f _{\mathbf{R}^+}$ is injective.
		set theory	<del>.</del>	
		such that		S = [(v,v)   0 < v < f(v)]
		such that;	means "such that", see ":" (lescribed	$S = \{(x,y) \mid 0 < y < f(x)\}$ The set of $(x,y)$ such that y is greater than 0 and le
		so that everywhere	below).	than f(x).
		2701311111111	a   b means a divides b.	
1	, 1, ,	divisor, divides	$a \nmid b$ means a does not divide b.	
1	\mid	divides divides	(The symbol   can be difficult to type, and its	Since $15 = 3 \times 5$ , it is true that 3   15 and 5   15.
ł	<u> </u>	number theory	negation is rare, so a regular but slightly	
1	\nmid		shorter vertical bar  character is often used instead.)	
		exact		
П	l II	divisibility	$p^a \mid \mid n$ means $p^a$ exactly divides $n$ (i.e. $p^a$	03 11 000
	\mid\mid	exactly divides	divides $n$ but $p^{a+1}$ does not).	2 <sup>3</sup>    360.
		number theory		
	Į,	parallel	$x \parallel y$ means $x$ is parallel to $y$ .	If $I \parallel m$ and $m \perp n$ then $I \perp n$ .
	\    Requires the viewer to support	is parallel to	$x \nmid y$ means x is not parallel to y. $x \neq y$ means x is equal and parallel to y.	
ł	Unicode: \unicode{x2225},	geometry		
"	\unicode{x2226}, and \unicode{x22D5}.		(The symbol    can be difficult to type, and its negation is rare, so two regular but slightly	
#	\mathrel{\rlap{\parallel}}		longer vertical bar   characters are often used instead.)	
			INVITEDORIA	·

	requires \setmathfont{MathJax}.[19]	incomparability		
		is incomparable to order theory	$x \parallel y$ means $x$ is incomparable toy.	{1,2} ∥ {2,3} under set containment.
		cardinality cardinality of; size of; order of set theory	#X means the cardinality of the setX.  ([  may be used instead as described above.)	#{4, 6, 8} = 3
#_	# \sharp	connected sum  connected sum of; knot sum of; knot composition of topology, knot theory		$A\#S^m$ is homeomorphic to $A$ , for any manifold $A$ , and the sphere $S^m$ .
		primorial primorial number theory	<i>n#</i> is product of all prime numbers less than or equal to <i>n</i> .	12# = 2 × 3 × 5 × 7 × 11 = 2310
		such that such that; so that everywhere	: means "such that", and is used in proofs and the <u>set-builder notation</u> (described below).	∃ $n \in \mathbb{N}$ : $n$ is even.
		extends; over field theory	$K: F$ means the field $K$ extends the field $F$ .  This may also be written as $K \ge F$ .	R: Q
<u>:</u>	·	inner product of matrices inner product of linear algebra	$A: B$ means the Frobenius inner product of the matrices $A$ and $B$ .  The general inner product is denoted by(u, v), (u   v) or (u   v), as described below For spatial vectors, the dot product notation, $x \cdot y$ is common. See also bra–ket notation	$A:B=\sum_{i,j}A_{ij}B_{ij}$
		index of a subgroup index of subgroup group theory	The index of a subgroupH in a group G is the "relative size" of H in G: equivalently, the number of "copies" (cosets) of H that fill up G	$ G:H =rac{ G }{ H }$
		division divided by over everywhere	A: B means the division of A with B (dividing A by B)	10:2=5
:	: \vdots \!	vertical ellipsis vertical ellipsis everywhere	important terms are being listed	$P(r,t)=\chi\dot{E}(r,t_1)E(r,t_2)E(r,t_3)$
1	\wr\!	wreath product wreath product of by group theory	A by the group H.	$\mathbf{S}_n \wr \mathbf{Z}_2$ is isomorphic to the <u>automorphism</u> group of the <u>complete bipartite graphon</u> $\overline{(n,n)}$ vertices.
<i>4</i> □ ⇒=	\blitza \lighting: requires \usepackage{stmaryd} \bar{20} \smashtimes requires \usepackage{unicode-math} and \setmathfont{XITS Math} or another Open Type Math Font. \bar{21} \rightarrow\Leftarrow \L\bar{22} \kappa \bar{2} \hat\bar{2} \hat\bar{2} \hat\bar{2} \hat\bar{2} \hat\bar{2} \contradiction \bar{2} \bar{2} \contradiction \bar{2} \bar{2}	downwards zigzag arrow contradiction; this contradicts that everywhere	Denotes that contradictory statements have been inferred. For clarity the exact point of contradiction can be appended.	$x + 4 = x - 3 \times$ Statement: Every finite, non-empty ordered set has a largest element. Otherwise, let's assume that $X$ is a finite, non-empty, ordered set with no largestelement. Then, for some $x_1 \in X$ , there exists an $x_2 \in X$ with $x_1 < x_2$ , but then there's also an $x_3 \in X$ with $x_2 < x_3$ and so on. Thus, $x_1, x_2, x_3, \ldots$ are distinct elements $X$ . $x_1 \times x_2 \times x_3 \times x_3 \times x_4 \times x_4 \times x_5 $
Ф <u>V</u>	⊕ \oplus \! <u>⊻</u> \veebar \!	exclusive or xor propositional logic, Boolean algebra	same.	$(\neg A) \oplus A$ is always true, $A \oplus A$ is always false.
		direct sum of	The direct sum is a special way of combining several objects into one general object.	Most commonly, for vector spaces $U$ , $V$ , and $W$ , the following consequence is used: $U = V \oplus W \Leftrightarrow (U = V + W) \land (V \cap W = \{0\})$

	abstract algebra	(The bun symbol $⊕$ , or the <u>coproduct</u> symbol $\bigsqcup$ , is used; $\veebar$ is only for logic.)	
{~\wedge\!\!\!\!\!\bigcirc~}	Kulkarni– Nomizu product Kulkarni– Nomizu product tensor algebra	Derived from the tensor product of two symmetric type (0,2)tensors; it has the algebraic symmetries of the Riemann tensor. $f = g \bigotimes h$ has components $f_{\alpha\beta\gamma\delta} = g_{\alpha\gamma}h_{\beta\delta} + g_{\beta\delta}h_{\alpha\gamma} - g_{\alpha\delta}h_{\beta\gamma} - g_{\beta\gamma}h_{\alpha\delta}$	
	D'Alembertian wave operator non-Euclidean Laplacian vector calculus	It is the generalisation of the <u>Laplace</u> operator in the sense that it is the differential operator which is invariant under the isometry group of the underlying space and it reduces to the <u>Laplace</u> operator if restricted to time independent functions.	$\Box = \frac{1}{c^2} \frac{\partial^2}{\partial t^2} - \frac{\partial^2}{\partial x^2} - \frac{\partial^2}{\partial y^2} - \frac{\partial^2}{\partial z^2}$

## **Letter-based symbols**

Includes upside-down letters.

## Letter modifiers

Also called diacritics.

		Name		
Symbol in HTML	Symbol in <u>TeX</u>	Read as	Explanation	Examples
III HIML		Category	·	·
		mean		
		overbar; bar	$\bar{\boldsymbol{x}}$ (often read as "x bar") is themean (average value of $\boldsymbol{x_i}$ ).	$x = \{1, 2, 3, 4, 5\}; \bar{x} = 3.$
		statistics		
		finite sequence, tuple		
		finite sequence, tuple	$\overline{a}$ means the finite sequence/tuple $(a_1,a_2,\ldots,a_n)$ .	$\overline{a} := (a_1, a_2, \ldots, a_n)$
		model theory		
$\frac{\overline{a}}{a}$	<b>ā</b> \bar{a}	algebraic closure	_	The field of algebraic numbers is sometimes denoted as $\overline{f Q}$
_	(bai {a}	algebraic closure of	$\overline{m{F}}$ is the algebraic closure of the field $\!F$ .	because it is the algebraic closure of the ational numbers $\mathbb{Q}$ .
		field theory complex		
		conjugate	$\overline{z}$ means the complex conjugate ofz.	
		conjugate	(z* can also be used for the conjugate of z, as described above.)	$\overline{3+4i}=3-4i.$
		complex numbers		
		topological closure	_	
		(topological)	$\overline{m{S}}$ is the topological closure of the setS.	In the space of the real numbers, $\overline{\mathbb{Q}} = \mathbb{R}$ (the rational numbers
		closure of	This may also be denoted ascl(S) or Cl(S).	are <u>dense</u> in the real numbers).
		topology vector		
	a       \overset{\rightharpoonup}       {a}	harpoon		
$\overrightarrow{a}$		linear		
		algebra		
		unit vector hat	â (pronounced "a hat") is thenormalized version	
	<b>â</b> \hat a	geometry	of vector <b>a</b> , having length 1.	
â		estimator		_
		estimator	narameter #	The estimator $\hat{\mu} = \frac{\sum_{i} x_{i}}{n}$ produces a sample estimate $\hat{\mu}(\mathbf{x})$ for
		for		the mean $\mu$ .
		statistics		r
		derivative	$f'(x)$ means the derivative of the function at the point $x$ , i.e., the slope of the tangent to $f$ at $x$ .  If $f(x) := x^2$ , then $f'(x) = 2x$ .	
'	,	prime; derivative of		If $f(x) := x^2$ , then $f'(x) = 2x$ .
-		calculus	(The single-quote character is sometimes used instead, especially in ASCII text)	
		derivative		
	\dot{}	dot;	$\dot{\boldsymbol{x}}$ means the derivative of x with respect to time.	
		time derivative of	That is $\dot{x}(t) = \frac{\partial}{\partial t}x(t)$ .	If $x(t) := t^2$ , then $\dot{x}(t) = 2t$ .
_		calculus	or ·	
		Jaiouius		

## Symbols based on Latin letters

Name					
Symbol Symbol		Read as			
Symbol in HTML	Symbol in TeX	Category	Explanation	Examples	
III HIWL	in <u>iex</u>	- Cutogoly			
		universal quantification			
Y	¥	for all; for any;	$\forall x, P(x)$ means $P(x)$ is true for all $x$ .	$\forall n \in \mathbb{N}, n^2 \ge n.$	
_	\forall	for each; for every	V A, I (A) means P (A) is title for all A.	V 11 C 14, 11 Z 11.	
		predicate logic			
$\mathbb{B}$	<b>B</b>	boolean domain			
_	\mathbb{B}	B; the (set of) boolean values;	$\mathbb{B}$ means either {0, 1}, {false, true}, {FT}, or { $\bot$ , T}.	$(\neg False) \in \mathbb{B}$	
В	<b>B</b> ∖mathbf{B}	the (set of) truth values;			
	©	set theory, boolean algebra			
$\mathbb{C}$	\mathbb{C}	complex numbers C;		$i = \sqrt{-1} \in \mathbb{C}$	
	C	the (set of) complex numbers	$\mathbb{C}$ means $\{a+b \ i: a,b \in \mathbb{R}\}$ .	$i = \sqrt{-1} \in \mathbb{C}$	
<u>C</u>	\mathbf{C}	numbers			
		cardinality of the continuum		$c = \beth_1$	
П	<b>¢</b> ∖mathfrak c	cardinality of the continuum; c;	The cardinality of $\mathbb{R}$ is denoted by $ \mathbb{R} $ or by the symbol $\mathfrak{c}$ (a lowercase Fraktur letter C).	· -1	
_	, macrir an	cardinality of the real numbers			
		partial derivative			
		partial;	$\partial f/\partial x_i$ means the partial derivative off with respect to $x_i$ , where $f$ is	If $f(x,y) := x^2y$ , then $\partial f/\partial x = 2xy$ ,	
		d calculus	a function on $(x_1,, x_n)$ .	in (x,y) .= x y, then onex = 2xy,	
	ð	boundary			
$\underline{\partial}$	\partial	boundary of	$\partial M$ means the boundary of $M$	$\partial \{x :   x   \le 2\} = \{x :   x   = 2\}$	
		topology			
		degree of a polynomial degree of	$\partial f$ means the degree of the polynomial.	$\partial(x^2-1)=2$	
		algebra	(This may also be writtendeg f.)	$O(x^ 1) = 2$	
E	E	expected value			
	\mathbb E	expected value	the value of a random variable one would "expect" to find if one could repeat the random variable process an infinite number of	$\mathbb{E}[X] = rac{x_1p_1 + x_2p_2 + \cdots + x_kp_k}{p_1 + p_2 + \cdots + p_k}$	
E	<b>E</b> \mathrm{E}	probability theory	times and take the average of the values obtained	$p_1+p_2+\cdots+p_k$	
	(macri m (2)	existential quantification			
_	∃ \exists  	there exists;			
3		there is; there are	$\exists x: P(x)$ means there is at least onex such that $P(x)$ is true.	$\exists n \in \mathbb{N}: n \text{ is even.}$	
		predicate logic			
٦,	3!	uniqueness quantification		$\exists ! \ n \in \mathbb{N}: n+5=2n.$	
3!	\exists!	there exists exactly one predicate logic	$\exists ! x: P(x)$ means there is exactly onex such that $P(x)$ is true.		
_	€	set membership			
$\in$	\in	is an element of;	$a \in S$ means $a$ is an element of the setS; $[15]$ $a \notin S$ means $a$ is	$(1/2)^{-1} \in \mathbb{N}$	
∉	≠	is not an element of	not an element of S. <sup>[15]</sup>	2 <sup>-1</sup> ∉ ℕ	
<b>Y</b> -	\notin	everywhere, set theory			
∌	. ∌	set membership does not contain as an element	$S \not\ni e$ means the same thing ase $\notin S$ , where $S$ is a set and $e$ is		
"	\not\ni	set theory	not an element of S.		
		such that symbol	often abbreviated as "s.t."; : and   are also used to abbreviate		
	∋ \ni	such that	"such that". The use of∋ goes back to early mathematical logic and its usage in this sense is declining. The symbob ("back	Choose $x \ni 2 x$ and $3 x$ . (Here   is	
∍		mathematical logic	anailant) is compating a provisically used for though the till to avoid	used in the sense of "divides".)	
		set membership	contaston with set membership.		
		contains as an element	$S \ni e$ means the same thing ase $\in S$ , where $S$ is a set and $e$ is an element of $S$ .		
		set theory			
H	<b>H</b> \mathbb{H}	quaternions or Hamiltonian quaternions			
		H;	$\mathbb{H}$ means $\{a+b \mathbf{i}+c \mathbf{j}+d \mathbf{k}: a,b,c,d \in \mathbb{R}\}.$		
H	<b>H</b> \mathbf{H}	the (set of) quaternions numbers			
		numbers	N means either { 0, 1, 2, 3,} or { 1, 2, 3,}.		
	N \mathbb{N} N \mathbf{N}				
N		natural numbers	The choice depends on the area of mathematics being studied; e.g. number theorists prefer the latter; analysts, set theorists and		
		the (set of) natural numbers	computer scientistsprefer the former. To avoid confusion, always check an author's definition of N.	$\mathbb{N} = \{ a  : a \in \mathbb{Z}\} \text{ or } \mathbb{N} = \{ a  > 0: a \in \mathbb{Z}\}$	
<u>N</u>		numbers			
			denote the set of natural numbers (including zero), along with the		
			standard ordering relation≤.		
_	0	Hadamard product	For two matrices (or vectors) of the same dimensions $A, B \in \mathbb{R}^{m \times n}$ the Hadamard product is a matrix of the same		
0	\circ	entrywise product linear algebra	dimensions $A \circ B \in \mathbb{R}^{m \times n}$ with elements given by	$\begin{bmatrix} 1 & 2 \\ 2 & 4 \end{bmatrix} \circ \begin{bmatrix} 1 & 2 \\ 0 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 4 \\ 0 & 0 \end{bmatrix}$	
	E		( /•,) (/•,) (/•,)	\(\(\alpha\) \(\alpha\) \(\dots\)	
•	0	function composition	$f \circ g$ is the function such that $f \circ g(x) = f(g(x))$ . <sup>[22]</sup>	if $f(x) := 2x$ , and $g(x) := x + 3$ , then (f	

	\circ	composed with		$\circ g(x) = 2(x + 3).$	
		set theory			
0	О	Big O notation	The Big O notation describes the limiting behavior of a function,	If $f(x) = 6x^4 - 2x^3 + 5$ and $g(x) = x^4$ ,	
<u>O</u>	0	big-oh of	when the argument tends towards a particular value omfinity.	then $f(x) = O(g(x))$ as $x \to \infty$	
	, a	Computational complexity theory			
~	Ø				
Ø	\empty	empty set			
	Ø	the empty set null set	$\varnothing$ means the set with no elements [15] { } means the same.	$\{n \in \mathbb{N} : 1 < n^2 < 4\} = \emptyset$	
{ }	\varnothing {}	set theory			
	<b>{}</b> \{\}				
		set of primes			
		P;	${\Bbb P}$ is often used to denote the set of prime numbers.	$2 \in \mathbb{P}, 3 \in \mathbb{P}, 8 \notin \mathbb{P}$	
		the set of prime numbers	a is often used to denote the set of prime numbers.	201,301,001	
		arithmetic			
		projective space			
		P; the projective space;			
TD.	IP	the projective line;	$\mathbb{P}$ means a space with a point at infinity	<b>₽</b> <sup>1</sup> , <b>₽</b> <sup>2</sup>	
${\mathbb P}$	\mathbb{P}	the projective plane			
	P	topology			
P	\mathbf{P}	probability	$\mathbb{P}(X)$ means the probability of the eventX occurring.	If a fair coin is flipped, $\mathbb{P}(\text{Heads}) =$	
_		the probability of	This may also be written asP(X), $P(X)$ , $P[X]$ or $Pr[X]$ .	$\mathbb{P}(\text{Tails}) = 0.5.$	
		probability theory	This may also be written asp(x), PI(x), P[x] of PI[x].		
		_	Given a set S, the power set of S is the set of all subsets of the set	The power set $P(\{0, 1, 2\})$ is the se	
		Power set	S. The power set of S0 is	of all subsets of {0, 1, 2}. Hence,	
		the Power set of	denoted by P(S).	$P(\{0, 1, 2\}) = \{\emptyset, \{0\}, \{1\}, \{2\}, \{0, 1\}\} $ $\{0, 2\}, \{1, 2\}, \{0, 1, 2\} \}.$	
		Powerset			
		rotional numbers		0.14000 5.0	
$\mathbb Q$	<b>Q</b> \mathbb{Q}	rational numbers		3.14000 ∈ ℚ	
•	/mariinn{V}	Q; the (set of) rational numbers;	$\mathbb{Q}$ means $\{p/q: p \in \mathbb{Z}, q \in \mathbb{N}\}.$	π ∉ ℚ	
Q	Q	the rationals			
<u> </u>	\mathbf{Q}	numbers			
$\mathbb{R}$	R	real numbers		$\pi \in \mathbb{R}$	
11/2	\mathbb{R}	R;		// 1) / D	
_	R	the (set of) real numbers; the reals	$\mathbb R$ means the set of real numbers.	√(-1) ∉ ℝ	
$\mathbf{R}$	\mathbf{R}	numbers			
		conjugate transpose			
		conjugate transpose;	.+		
†	t	adjoint;	$A^{\dagger}$ means the transpose of the complex conjugate of A.[23]	If $A = (a)$ then $A^{\dagger} = (\overline{a})$	
_	{}^\dagger	Hermitian	. This may also be written $A^{*T}$ , $A^{T*}$ , $A^*$ , $\overline{A}^T$ or $\overline{A}^{\overline{T}}$ .	If $A = (a_{ij})$ then $A^{\dagger} = (\overline{a_{ji}})$ .	
		adjoint/conjugate/transpose/dagger			
		matrix operations transpose			
T	т	transpose	$A^{T}$ means $A$ , but with its rows swapped for columns.	If $A = (a_{ij})$ then $A^{T} = (a_{ij})$ .	
_	{}^{T}	matrix operations	This may also be writtenA', A <sup>t</sup> or A <sup>tr</sup> .	(ajj) then it = (ajj).	
		top element	-		
		the top element	op means the largest element of a lattice.	$\forall x : x \ V \ \top = \top$	
_	Т	lattice theory	, and the second		
<u>T</u>	\top	top type		∀ types T, T <: ⊤	
		the top type; top	T means the top or universal type; every type in the type system of interest is a subtype of top.		
		type theory			
		perpendicular	$x \perp y$ means x is perpendicular to y; or more generally x is	If $l \perp m$ and $m \perp n$ in the plane,	
		is perpendicular to	orthogonal to y.	then $I    n$ .	
		geometry			
		orthogonal complement			
		orthogonal/ perpendicular complement of;	$W^{\perp}$ means the orthogonal complement of W (where W is a subspace of the inner product space V), the set of all vectors in V	Within $\mathbb{R}^3$ , $(\mathbb{R}^2)^{\perp} \cong \mathbb{R}$ .	
		perp	orthogonal to every vector inW.	······································	
		linear algebra			
		coprime			
		is coprime to	$x \perp y$ means x has no factor greater than 1 in common withy.	34 ⊥ 55	
		number theory			
<u></u>	L \bot	independent	$A \perp B$ means A is an event whose probability is independent of		
		is independent of	event $B$ . The double perpendicular symbol $(L)$ is also commonly used for the purpose of denoting this, for instance $A \perp L B$ (In	If $A \perp B$ , then $\underline{P(A B)} = P(A)$ .	
		probability	LaTeX, the command is: "A \perp\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\		
		bottom element			
			$oldsymbol{\perp}$ means the smallest element of a lattice.	$\forall x : x \land \bot = \bot$	
		the bottom element		l .	
		the bottom element lattice theory			
		lattice theory bottom type the bottom type;	$oldsymbol{\perp}$ means the bottom type (a.k.a. the zero type or empty type);	∀ tynes 7   < 7	
		lattice theory bottom type the bottom type; bot	⊥ means the bottom type (a.k.a. the zero type or empty type); bottom is the subtype of every type in the system.	∀ types <i>T</i> , ⊥ <: <i>T</i>	
		lattice theory bottom type the bottom type;			
		lattice theory bottom type the bottom type; bot		$\{e, \pi\} \perp \{1, 2, e, 3, \pi\}$ under set	
		lattice theory bottom type the bottom type; bot type theory			
		lattice theory bottom type the bottom type; bot type theory comparability	bottom is the subtype of every type in the system.	$\{e, \pi\} \perp \{1, 2, e, 3, \pi\}$ under set	
U	U	lattice theory bottom type the bottom type; bot type theory comparability is comparable to	bottom is the subtype of every type in the system.	$\{e, \pi\} \perp \{1, 2, e, 3, \pi\}$ under set	

<u>u</u>	<b>U</b> \mathbf{U}	U; the universal set; the set of all numbers; all numbers considered	of these—hence the term "universal".	If instead, $\mathbb{U}$ = { $\mathbb{Z},\mathbb{C}$ }, then $\pi \notin \mathbb{U}.$	
U	U \cup	set-theoretic union set theory the union of or; union set theory	$A \cup B$ means the set of those elements which are either in A, or in B, or in both $^{[13]}$	$A \subseteq B \Leftrightarrow (A \cup B) = B$	
Λ	∩ \cap	intersected with; intersect set theory	$A \cap B$ means the set that contains all those elements that A and B have in common $^{[13]}$	$\{x \in \mathbb{R} : x^2 = 1\} \cap \mathbb{N} = \{1\}$	
V	V \lor	logical disjunction or join in a lattice  or; max; join propositional logic, lattice theory	The statement $A \lor B$ is true if $A$ or $B$ (or both) are true; if both are false, the statement is false.  For functions $A(x)$ and $B(x)$ , $A(x) \lor B(x)$ is used to mean max( $A(x)$ , $B(x)$ ).	$n \ge 4 \lor n \le 2 \Leftrightarrow n \ne 3 \text{ when } n \text{ is a }$ natural number.	
٨	Λ \land	logical conjunction or meet in a lattice  and; min; meet  propositional logic, lattice theory	The statement $A \land B$ is true if $A$ and $B$ are both true; else it is false.  For functions $A(x)$ and $B(x)$ , $A(x) \land B(x)$ is used to mean min( $A(x)$ , $B(x)$ ).	$n < 4 \land n > 2 \Leftrightarrow n = 3 \text{ when } n \text{ is a } \frac{1}{n}$	
		wedge product wedge product; exterior product exterior algebra	$u$ $\wedge$ $v$ means the wedge product of any multivectors $u$ and $v$ . In three-dimensional <u>Euclidean space</u> the wedge product and the cross product of two <u>vectors</u> are each other's <u>Hodge dual</u> .	$u \wedge v = *(u  imes v)  ext{ if } u,v \in \mathbb{R}^3$	
		multiplication times; multiplied by arithmetic	3 × 4 means the multiplication of 3 by 4.  (The symbol* is generally used in programming languages, where ease of typing and use of ASCII text is preferred.)	7 × 8 = 56	
×	× \times	Cartesian product the Cartesian product of and; the direct product of and set theory	X × Y means the set of all <u>ordered pairs</u> with the first element of each pair selected from X and the second element selected from Y.	$\{1,2\} \times \{3,4\} = \{(1,3),(1,4),(2,3),(2,4)\}$	
_		cross product cross linear algebra	<b>u</b> × <b>v</b> means the cross product of <u>vectors</u> <b>u</b> and <b>v</b>	(1,2,5) × (3,4,-1) = (-22, 16, -2)	
		group of units the group of units of ring theory	$R^{\times}$ consists of the set of units of the ringR, along with the operation of multiplication.  This may also be writtenR* as described below or U(R).	$(\mathbb{Z}/5\mathbb{Z})^{\times} = \{[1], [2], [3], [4]\}$ $\cong C_4$	
8	\times \tensor product \tensor product of \\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\		$V\otimes U$ means the tensor product of $V$ and $U^{[24]}V\otimes_R U$ means the tensor product of modules $V$ and $U$ over the $\underline{\text{ring}}\ R$ .	$\{1, 2, 3, 4\} \otimes \{1, 1, 2\} = \{\{1, 1, 2\}, \{2, 2, 4\}, \{3, 3, 6\}, \{4, 4, 8\}\}$	
×	<b>⋉</b> \ltimes	semidirect product the semidirect product of group theory	$N \rtimes_{\mathfrak{Q}} H$ is the semidirect product of $N$ (a normal subgroup) and $H$ (a subgroup), with respect to $\mathfrak{Q}$ . Also, if $G = N \rtimes_{\mathfrak{Q}} H$ , then $G$ is said to split over $N$ . ( $\bowtie$ may also be written the other way round, as $\bowtie$ , or as $\bowtie$ .)	$D_{2n}\cong \mathrm{C}_n times \mathrm{C}_2$	
×	∦ \rtimes	semijoin the semijoin of relational algebra	$R \ltimes S$ is the semijoin of the relations $R$ and $S$ , the set of all tuples in $R$ for which there is a tuple in $S$ that is equal on their common	$R \ltimes S = \mathbf{II}_{a_1,\dots,a_n}(R \bowtie S)$	
×	natural join  howtie  natural join  the natural join of relational		$R\bowtie S$ is the natural join of the relationsR and S, the set of all combinations of tuples inR and S that are equal on their common attribute names.		
Z	<b>Z</b> \mathbb{Z}	integers the (set of) integers	$\mathbb{Z}$ means {, -3, -2, -1, 0, 1, 2, 3,}. $\mathbb{Z}^+$ or $\mathbb{Z}^>$ means {1, 2, 3,}. $\mathbb{Z}^\ge$ means {0, 1, 2, 3,}.	$\mathbb{Z} = \{ p, \neg p : p \in \mathbb{N} \cup \{0\} \}$	
Z	<b>Z</b> \mathbf{Z}	numbers	$\mathbb{Z}^{\star}$ is used by some authors to mean {0, 1, 2, 3,}^{[25]} and others to mean {2, -1, 1, 2, 3, }^{[26]} .		
$\mathbb{Z}_n$ $\mathbb{Z}_p$	Z <sub>n</sub> \mathbb{Z}_n integers mod n the (set of) integers modulon		$\mathbb{Z}_n$ means {[0], [1], [2],[ $n$ -1]} with addition and multiplication modulo $n$ .  Note that any letter may be used instead of $n$ , such as $p$ . To avoid	$\mathbb{Z}_3 = \{[0], [1], [2]\}$	
$\mathbf{Z}_n$	$Z_p$ \mathbb{ $Z$ }_p $Z_n$ \mathbf{ $Z$ }_n	numbers p-adic integers	confusion with p-adic numbers, use $\mathbb{Z}/p\mathbb{Z}$ or $\mathbb{Z}/(p)$ instead.		
$\mathbf{Z}_p$	\matnbf{2}_n \\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	the (set of) p-adic integers  numbers	Note that any letter may be used instead op, such as n or l.		

Symbol in HTML	Symbol in <u>TeX</u>	Name Read as Category	Explanation	Examples
*	¥ ∖aleph	aleph number aleph set theory	$\aleph_\alpha$ represents an infinite cardinality (specificallythe $\alpha$ -th one, where $\alpha$ is an ordinal).	$ \mathbb{N} =\aleph_0$ , which is called aleph-null.
ے	⊐ \beth	beth number beth set theory	$\beth_\alpha$ represents an infinite cardinality (similar tox), but $\beth$ does not necessarily index all of the numbers indexed byx. ).	$\beth_1 =  P(\mathbb{N})  = 2^{\aleph_0}$ .
		Dirac delta function Dirac delta of hyperfunction Kronecker delta		δ(x)
<u>δ</u>	<b>δ</b> ∖delta	Kronecker delta of hyperfunction	$egin{aligned} \delta_{ij} &= egin{cases} 1, & i = j \ 0, & i  eq j \end{cases} \ &iggl  rac{\delta F[arphi(x)]}{\delta arphi(x)}, f(x) iggr  = \int rac{\delta F[arphi(x)]}{\delta arphi(x')} f(x') dx' \end{aligned}$	$\delta_{ij}$
		Functional derivative of Differential operators	$=\lim_{arepsilon o 0}rac{F[arphi(x)+arepsilon f(x)]-F[arphi(x)]}{arepsilon}$	$rac{\delta V(r)}{\delta  ho(r')} = rac{1}{4\pi\epsilon_0  r-r' }$
Δ	∆ \vartriangle	symmetric		
θ	⊖ \ominus	symmetric difference	$A \triangle B$ (or $A \ominus B$ ) means the set of elements in exactly one of $A$ or $B$ .  (Not to be confused with delta $\triangle$ , described below)	$\{1,5,6,8\} \Delta \{2,5,8\} = \{1,2,6\}$ $\{3,4,5,6\} \ominus \{1,2,5,6\} = \{1,2,3,4\}$
<b>⊕</b>	⊕ \oplus	set theory		
Δ	Δ	delta delta; change in calculus	$\Delta x$ means a (non-infinitesimal) change inx. (If the change becomes infinitesimal $\delta$ and even d are used instead. Not to be confused with the symmetric difference, written $\Delta$ , above.)	$\frac{\Delta y}{\Delta x}$ is the gradient of a straight line.
	\Delta	Laplacian  Laplace operator  vector calculus	The Laplace operator is a second order diferential operator in n-dimensional Euclidean space	If $f$ is a twice-differentiable real-valued function, then the Laplacian of $f$ is defined by $\Delta f = \nabla^2 f = \nabla \cdot \nabla f$
		gradient  del; nabla; gradient of  vector calculus	$\nabla f(x_1,,x_n) \text{ is the vector of partial derivatives } \partial f/\partial x_1,, \\ \partial f/\partial x_n).$	If $f(x,y,z) := 3xy + z^2$ , then $\nabla f = (3y, 3x, 2z)$
<u> </u>	<b>▽</b> \nabla	del dot; divergence of vector calculus	$ abla \cdot ec{v} = rac{\partial v_x}{\partial x} + rac{\partial v_y}{\partial y} + rac{\partial v_z}{\partial z}$	If $ec{v}:=3xy\mathbf{i}+y^2z\mathbf{j}+5\mathbf{k}$ , then $ abla\cdotec{v}=3y+2yz$ .
		curl of vector calculus	$ abla  imes ec{v} = \left(rac{\partial v_z}{\partial y} - rac{\partial v_y}{\partial z} ight)\mathbf{i} \\ + \left(rac{\partial v_x}{\partial z} - rac{\partial v_z}{\partial x} ight)\mathbf{j} + \left(rac{\partial v_y}{\partial x} - rac{\partial v_z}{\partial y} ight)\mathbf{k}$	If $ec{v}:=3xy\mathbf{i}+y^2z\mathbf{j}+5\mathbf{k}$ , then $ abla imesec{v}=-y^2\mathbf{i}-3x\mathbf{k}$ .
		pi; 3.1415926; ≈355÷113 mathematical constant		$\underline{A} = \pi \underline{R}^2 = 314.16 \rightarrow R = 10$
<u>π</u>	<b>π</b> \pi	Projection of relational algebra	$\pi_{a_1,\ldots,a_n}(R)$ restricts $R$ to the $\{a_1,\ldots,a_n\}$ attribute set.	$\pi_{ ext{Age,Weight}}( ext{Person})$
		Homotopy group  the nth Homotopy group of  Homotopy theory	$\pi_n(X)$ consists of homotopy equivalence classes of base point preserving maps from an n-dimensional sphere (with base point) into the pointed space X.	$\pi_i(S^4)=\pi_i(S^7)\oplus\pi_{i-1}(S^3)$
П	∏ ∖prod	product product over from to of arithmetic	$\prod_{k=1}^n a_k$ means $a_1 a_2 \ldots a_n$ .	$\prod_{k=1}^{4} (k+2) = (1+2)(2+2)(3+2)(4+2) = 3 \times 4 \times 5 \times 6 = 360$
		Cartesian product the Cartesian product of;		$\prod_{n=1}^{3} \mathbb{R} = \mathbb{R} \times \mathbb{R} \times \mathbb{R} = \mathbb{R}^{3}$
			$(y_0,, y_n).$	

		the direct product of set theory		
П	II \coprod	coproduct coproduct over from to of  category theory	A general construction which subsumes the disjoint union of sets and of topological spaces the free product of groups and the direct sum of modules and vector spaces. The coproduct of a family of objects is essentially the "least specific" object to which each object in the family admits a morphism.	
σ	σ \sigma	Selection Selection of relational algebra		$\sigma_{ ext{Age} \geq 34}( ext{Person}) \ \sigma_{ ext{Age} =  ext{Weight}}( ext{Person})$
Σ	\sum	summation sum over from to of arithmetic	$\sum_{k=1}^n a_k$ means $a_1+a_2+\cdots+a_n$ .	$\sum_{k=1}^{4} k^2 = 1^2 + 2^2 + 3^2 + 4^2 = 1 + 4 + 9 + 16 = 30$

### **Variations**

In mathematics written in Persian or Arabic, some symbols may be reversed to make right-to-left writing and reading easie [27]

#### See also

- Greek letters used in mathematics, science, and engineering
- · List of letters used in mathematics and science
- List of common physics notations
- Diacritic
- ISO 31-11 (Mathematical signs and symbols for use in physical sciences and technology)
- Latin letters used in mathematics
- List of mathematical abbreviations
- List of mathematical symbols by subject
- Mathematical Alphanumeric Symbols (Unicode block)
- Mathematical constants and functions
- Mathematical notation
- Mathematical operators and symbols in Unicode
- · Notation in probability and statistics
- Physical constants
- Table of logic symbols
- Table of mathematical symbols by introduction date
- Typographical conventions in mathematical formulae

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## **External links**

- The complete set of mathematics Unicode characters
- Jeff Miller: Earliest Uses of Various Mathematical Symbols
- Numericana: Scientific Symbols and Icons
- GIF and PNG Images for Math Symbols
- Mathematical Symbols in Unicode
- Using Greek and special characters from Symbol font in HTML
- DeTeXify handwritten symbol recognition— doodle a symbol in the box, and the program will tell you what its name is
- Handbook for Spoken Mathematics— pronunciation guide to many commonly used symbols

Some Unicode charts of mathematical operators and symbols:

- Index of Unicode symbols
- Range 2100–214F: Unicode Letterlike Symbols
- Range 2190–21FF: Unicode Arrows
- Range 2200–22FF: Unicode Mathematical Operators
- Range 27C0–27EF: Unicode Miscellaneous Mathematical Symbols–A
- Range 2980–29FF: Unicode Miscellaneous Mathematical Symbols–B
- Range 2A00–2AFF: Unicode Supplementary Mathematical Operators

#### Some Unicode cross-references:

- Short list of commonly used LaTeX symbols and Comprehensive LaTeX Symbol List
- MathML Characters- sorts out Unicode, HTML and MathML/€X names on one page
- Unicode values and MathML names
- Unicode values and Postscript namesfrom the source code for Ghostscript

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