Algorithms and Data Structures for Data Science

2D Lists, Stacks, and Queues

CS 277
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ILLINOIS
URBANA-CHAMPAIGN

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The purpose of assessments in CS 277

Reminder: MP 0 due today!

Informal Early Feedback

An anonymous survey about the class

If 70% of class completes, everyone gets bonus points

Please provide constructive criticism and positive feedback

Learning Objectives

Observe data structure tradeoffs between data access and speed

Understand the fundamentals of the stack and queue

Introduce NumPy and practice 2D lists

Array Implementation

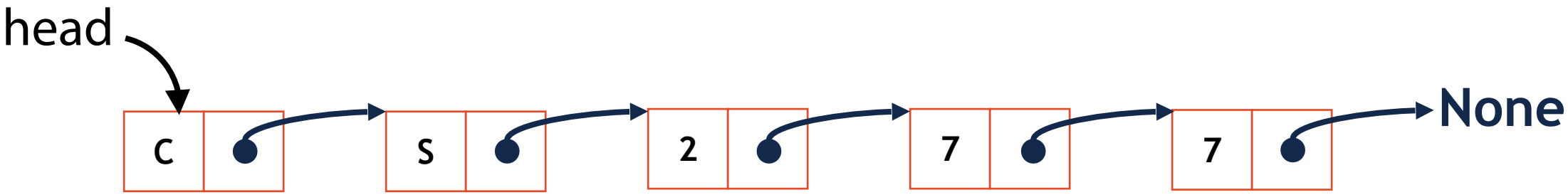
	Singly Linked List	Array
Look up **arbitrary** location	O(n)	**O(1)**
Insert after **given** element	**O(1)**	O(n)
Remove after **given** element	**O(1)**	O(n)
Insert at **arbitrary** location	O(n)	O(n)
Remove at **arbitrary** location	O(n)	O(n)
Search for an input **value**	O(n)	O(n)

Thinking critically about lists: tradeoffs

Can we make our lists better at some things? What is the cost?

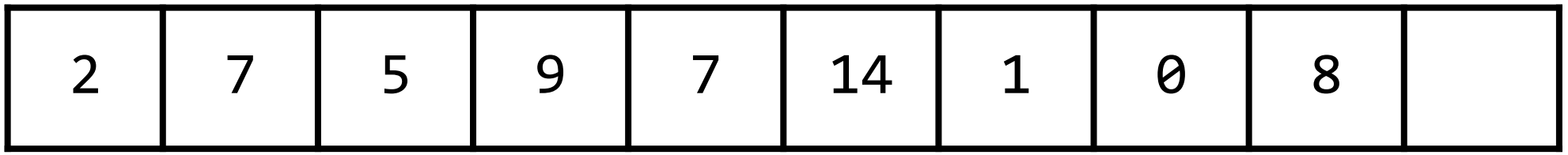
Thinking critically about lists: tradeoffs

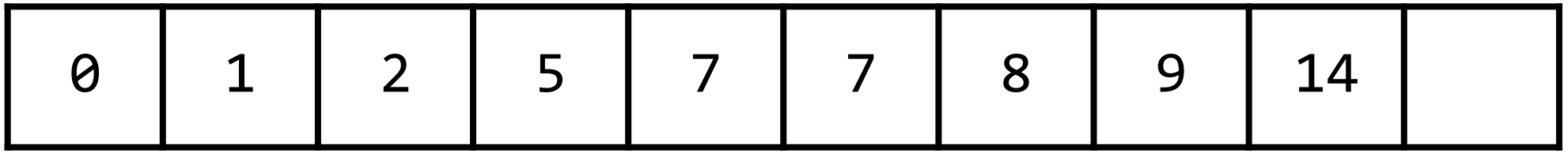
Getting the size of a linked list has a Big O of:



Thinking critically about lists: tradeoffs

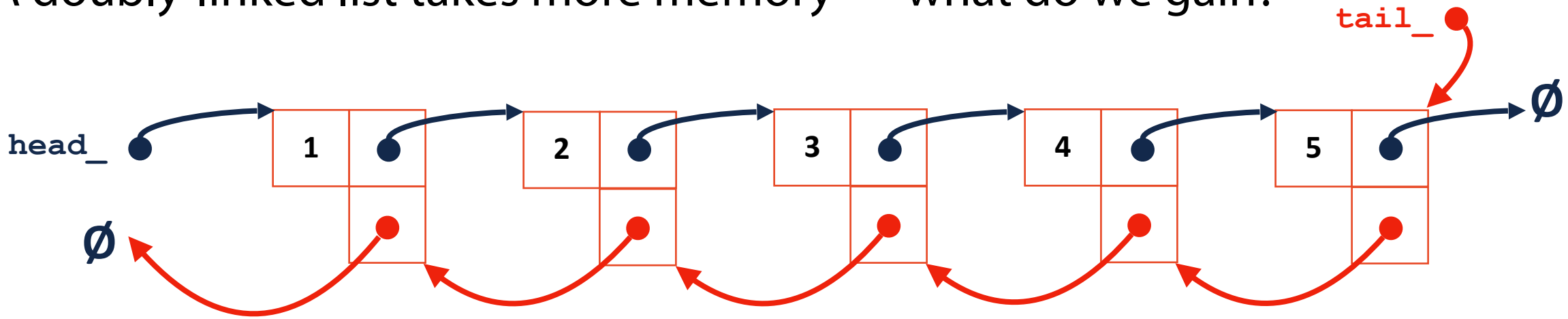
Does knowing our list is sorted change our Array Big O?





Thinking critically about lists: tradeoffs

A doubly-linked list takes more memory — what do we gain?



Thinking critically about lists: tradeoffs

Consider carefully how data structures can be modified for a problem!

Lets see two examples of this:

I want a data structure that can add and remove in O(1).

I'm willing to 'trade away' a lot of utility to do this.

The Stack ADT

A **stack** stores an ordered collection of objects (like a list)

However you can only do three operations:

Push: Put an item on top of the stack

Pop: Remove the top item of the stack (and return it)

Top: Look at the value of the top item

```
push(3); push(5); top(); pop(); push(2)
```

Programming Toolbox: Stack

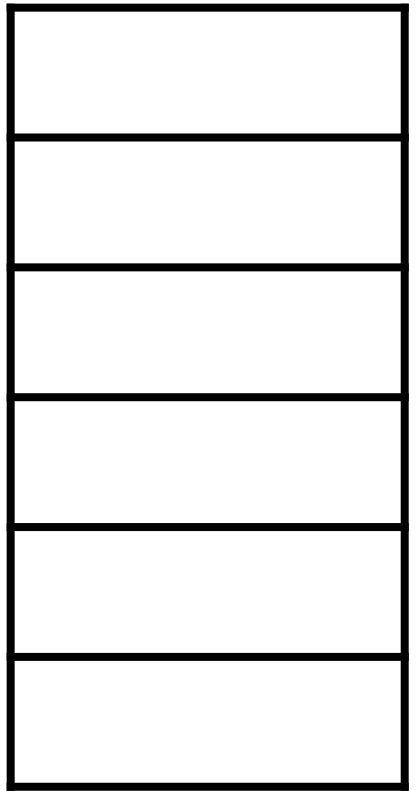
The stack is a **last in — first out** data structure (LIFO)

```
1  def reverse(inList):
2      s = stack()
3      for v in inList:
4          s.push(v)
5
6      out = []
7      while not s.empty():
8          out.append(s.pop())
9      return out
```

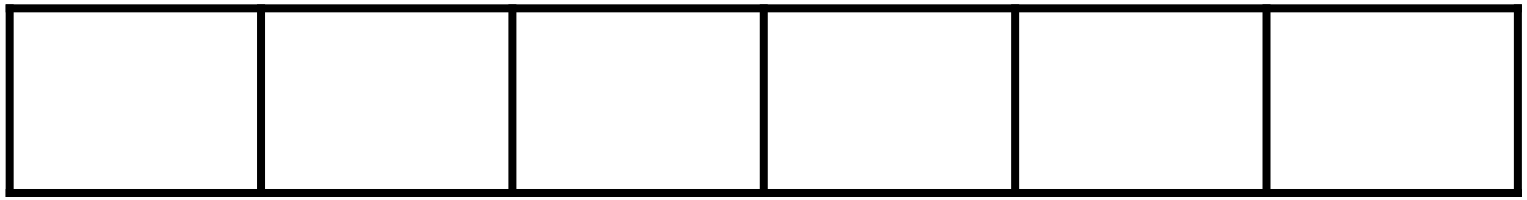
Not a Python built-in!

```
reverse([3, 4, 5, 6, 7, 8])
```

stack s



out



Stack Implementation (using Lists)

	Singly Linked List	Array
Look up **arbitrary** location	O(n)	**O(1)**
Insert after **given** element	**O(1)**	O(n)
Remove after **given** element	**O(1)**	O(n)
Insert at **arbitrary** location	O(n)	O(n)
Remove at **arbitrary** location	O(n)	O(n)
Search for an input **value**	O(n)	O(n)

Stack as a Linked List

`push(X)`

Push() adds the provided item to the top of my list

Stack as a Linked List

`pop()`

Pop() removes the top item from my list

Stack as a Linked List

`top()`

Top() looks at the top item of the list

Stack Implementation

```
class Node:
    def __init__(self, value, next = None):
         self.val = value
         self.next = next

class stack:
    def __init__(self):
        self.head = None
        self.length = 0

    def push(self, value):
        self.length += 1
        newNode = Node(value)
        newNode.next = self.head
        self.head = newNode

    def __len__(self):
        return self.length
```

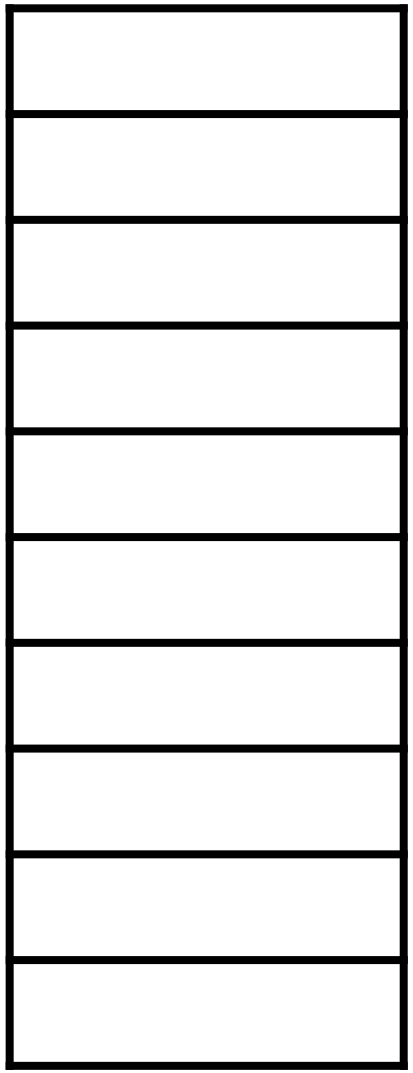
```
# class stack:
    def top(self):
        if self.length > 0:
            return self.head.val
        return None

    def pop(self):
        if (self.length > 0):
            self.length -= 1
            popped = self.head
            self.head = self.head.next
            return popped.val
        return None

# Some other support functions in code base
```

On your own: Stack Practice

What will the stack look like as you run the following code?

Try it by hand and run the code to check!

```
 1 s = stack()
 2
 3 print(s.empty())
 4
 5 for i in range(0, 10, 2):
 6     s.push(i)
 7
 8 print(s)
 9
10 x = s.pop()
11 print(x, s)
12
13 print(len(s))
14
15 print(s.top())
16 s.pop()
17 print(s.top())
18
19 print(s.empty())
```



The Call Stack

```
 1 def Happy():
 2     print("Calling Happy!")
 3     return "Happy"
 4
 5 def Little():
 6     print("Calling Little!")
 7     return "Little"
 8
 9 def Trees():
10     print("Calling Trees!")
11     return "Trees"
12
13 def LittleTrees():
14     print("Calling LittleTrees!")
15     return Little() + Trees()
16
17 def BobRoss():
18     print("Calling BobRoss!")
19     return Happy() + LittleTrees()
20
21 print(BobRoss())
22
23
```

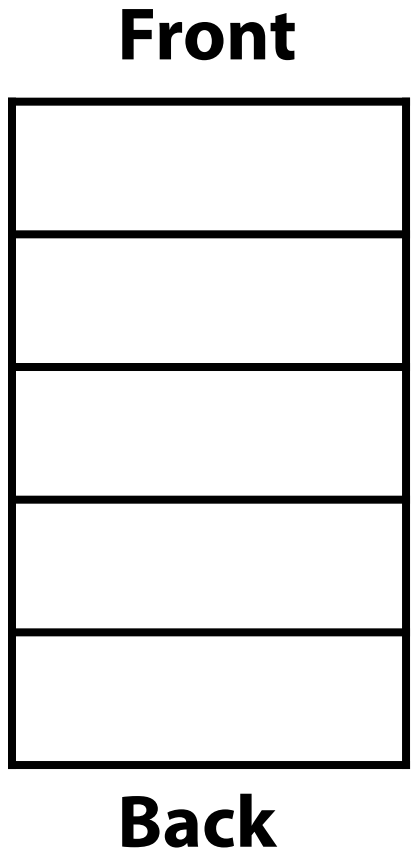
Queue Data Structure

A **queue** stores an ordered collection of objects (like a list)

However you can only do two operations:

Enqueue: Put an item at the back of the queue

Dequeue: Remove and return the front item of the queue




```
enqueue(3); enqueue(5); dequeue(); enqueue(2)
```

Queue Data Structure

The queue is a **first in — first out** data structure (FIFO)

What data structure excels at removing from the front?

Can we make that same data structure good at inserting at the end?

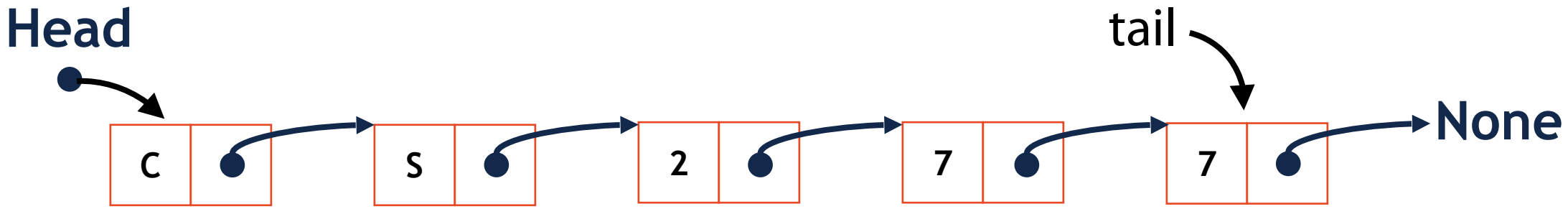
Queue Data Structure

Once again, a linked list is a great implementation of a queue!

But we need one modification…

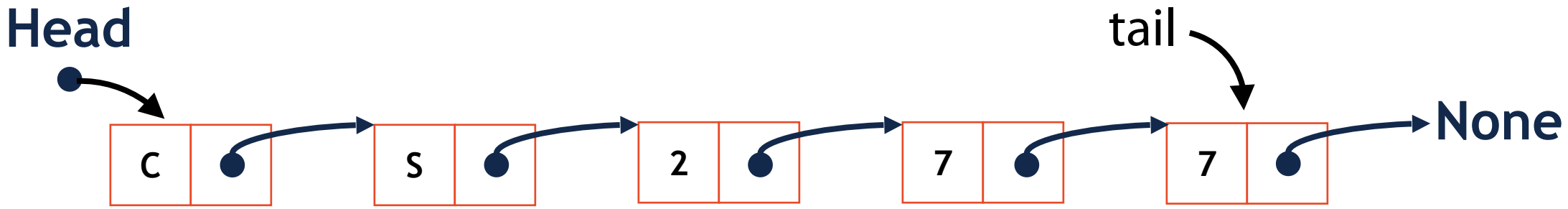
Queue as Linked List

`enqueue(b)`



Queue as Linked List

`dequeue()`



Queue Implementation

```
class Node:
    def __init__(self, value, next = None):
         self.val = value
         self.next = next

class queue:
    def __init__(self):
        self.length = 0
        self.head = None
        self.tail = None

    def enqueue(self, value):
        self.length += 1
        item = Node(value)
        if self.head == None:
            self.head = item
            self.tail = item
        else:
            self.tail.next = item
            self.tail = self.tail.next
```

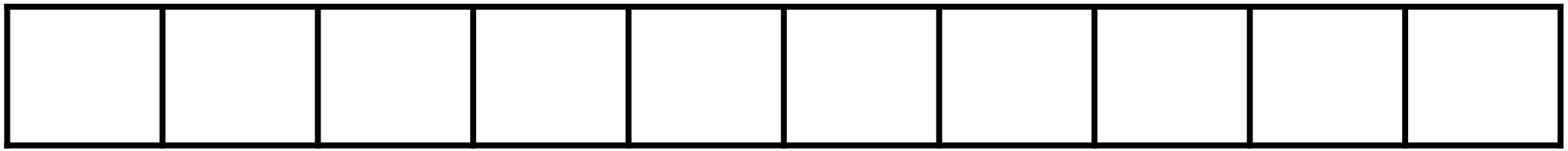
```
# class queue:
    def dequeue(self):
        if self.length > 0:
            self.length -= 1
            item = self.head
            self.head = item.next

            if self.head == None:
                self.tail = None
            return item.val

        return None

    def front(self):
        if self.length > 0:
            return self.head.val
        return None

# Other support functions in code base
```

On your own: Queue Practice

```
 1 q = queue()
 2
 3 print(q.empty())
 4
 5 for i in range(0,20, 2):
 6     q.enqueue(i)
 7 print(q)
 8
 9 x = q.dequeue()
10 print(x, q)
11
12 print(len(q))
13
14 print(q.front())
15 q.dequeue()
16 print(q.front())
17
18 print(q.empty())
```

What will this code output?

Try it by hand and run the code to check!



The CS 277 Queue

Now you know how the CS 277 queue works!

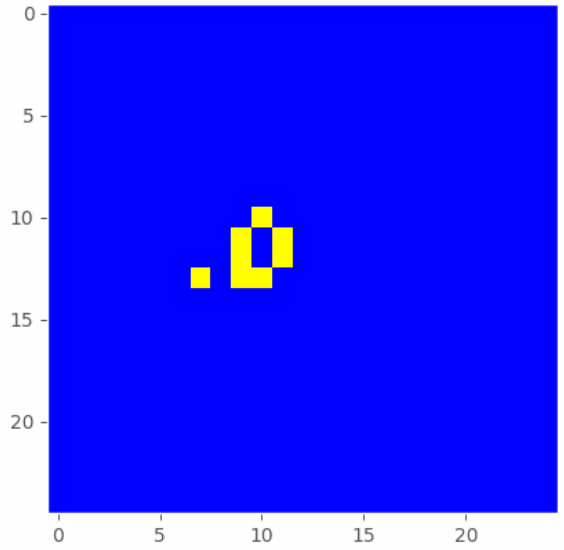
https://queue.illinois.edu/q/course/185

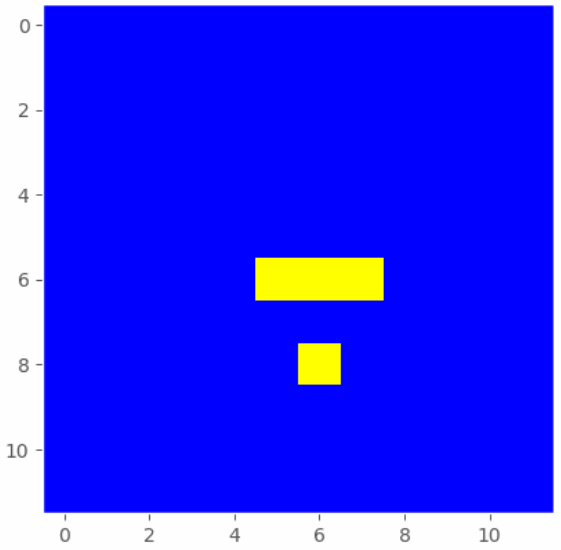
Cellular Automata — probably pushed back?

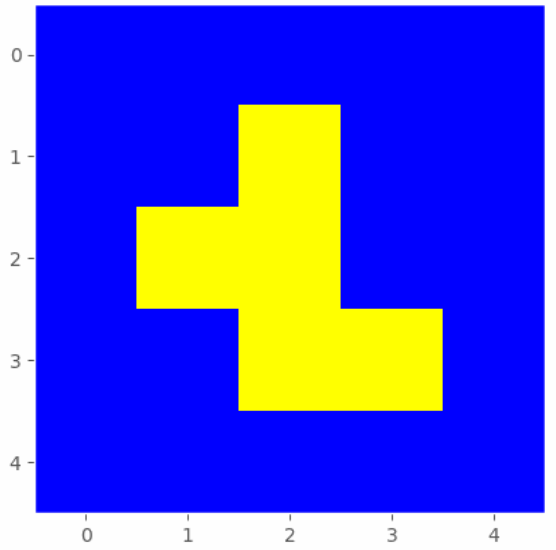
A computational model consisting of a **matrix** and a **set of rules**

Each iteration, the matrix changes based on its current state

There are a number of emergent behaviors that can be discovered!







Programming Practice: 2D Lists

Given a function that passes in three lists, make a 2D array storing all three.

How would I search a 2D list for a specific value?

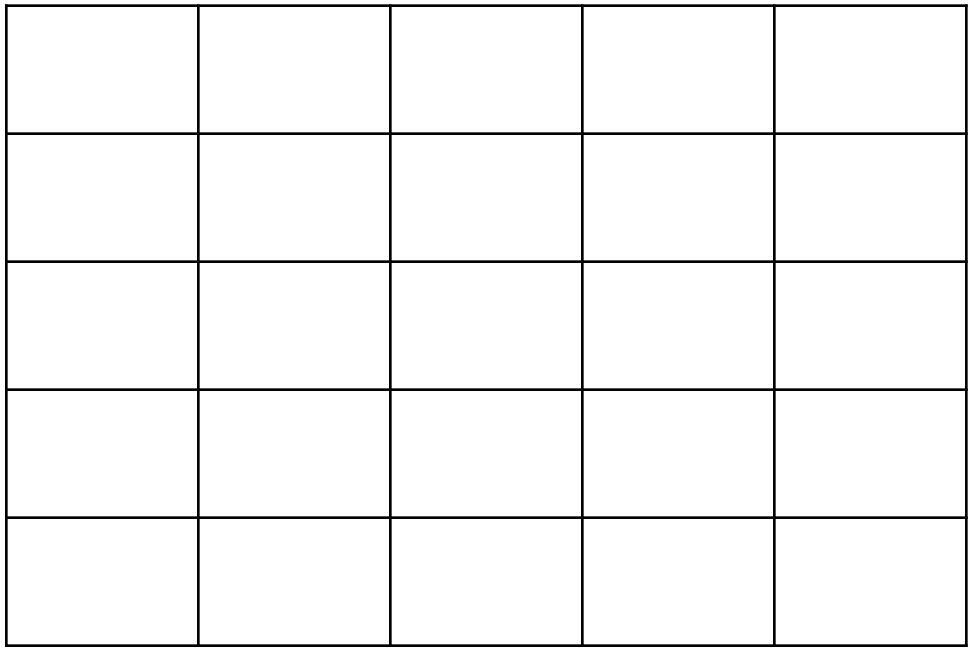
Programming Practice: 2D Lists

What shape will this code produce?

```
outerList = []

for i in range(5):
    innerList = []

    for j in range(5):
        innerList.append(i+j)

    outerList.append(innerList)
```

Programming Practice: 2D Lists

What values will this list produce?



```
1  outerList = []
2
3  for i in range(5):
4      innerList = []
5
6      for j in range(5):
7          innerList.append(i+j)
8
9      outerList.append(innerList)
10
11
12
13
14
15
16
17
18
```

Programming Practice: 2D Lists

What are the indices of every value of 4 in this list?

0	1	2	3	4
1	2	3	4	5
2	3	4	5	6
3	4	5	6	7
4	5	6	7	8

```
1  outerList = []
2
3  for i in range(5):
4      innerList = []
5
6      for j in range(5):
7          innerList.append(i+j)
8
9      outerList.append(innerList)
10
11
12
13
14
15
16
17
18
```

Programming Practice: 2D Lists

What are the indices of the square around the point (x, y)?

	`(x, y)`	

Programming Tip: Make a quick example!

I want to make a fast matrix with the values:

1	2	3
4	5	6
7	8	9

```
count = 0
out = []
for i in range(3):
    tmp = []
    for j in range(3):
        tmp.append(count)
        count+=1
    out.append(tmp)

print(out[2][2])

print(out[2][1])

print(out[1][2])
```

```
import numpy as np

x = np.arange(9).reshape(3, 3)

print(x)
```

Programming Toolbox: NumPy

NumPy is optimized for multidimensional arrays of numbers

```
1  import numpy as np
2
3  # Convert list to np list
4  nl = np.array([1, 2, 3, 4, 5, 6])
5  print(nl)
6
7  # See list shape
8  print(nl.shape)
9
10 # Modify list shape
11 nl2 = nl.reshape(3, 2)
12
13 print(nl)
14 print(nl2)
15
16 # Create a new list
17 nl3 = np.arange(15).reshape(5, 3)
18 nl4 = np.zeros((2, 5))
19
20 print(nl3)
21 print(nl4)
22
23
```

np.array(<list>)

Convert a built-in list to a NumPy List

<nparray>.shape

Get the shape of the NumPy array

np.reshape(<row>, <col>)

If the list contains exactly row x col items

reshape the list to those dimensions

np.arange()

returns a NumPy array with range() values

np.zeros((<row>, col>))

Create a list of 0s of the provided shape

Programming Toolbox: NumPy

Basic operations are applied **elementwise** (to each item of a list)

```
1  nl = np.arange(4).reshape(2, 2)
2
3  print(nl)
4
5  nl2 = nl * 2
6
7  print(nl2)
8
```

NumPy lists of equal size can also be added / subtracted / multiplied / etc…

```
1  m1 = np.arange(9).reshape(3,3)
2  print(m1)
3
4  m2 = np.arange(9, 0, -1).reshape(3,3)
5  print(m2)
6
7  print(m1+m2)
8
```

Programming Toolbox: NumPy

NumPy is huge and can do many things

```
1  nl = np.arange(4).reshape(2, 2)
2  nl2 = nl * 2
3
4  # Matrix multiplication
5  # 0*0+1*4      0*0+1*6
6  # 2*0+3*4      2*2+3*6
7  print(nl.dot(nl2))
8
9  # Unique items
10 x = np.array([1, 1, 1, 2, 3, 4, 4, 5, 5, 6])
11 print(np.unique(x))
12
```

Explore on your own: https://numpy.org/devdocs/

Next Week: Copying 2D Lists

What happens when we run the following code? Why?

```
1  orig = [ [1,2,3], [4, 5, 6]]
2
3  copy = orig[:]
4
5  orig[1][1]=9
6  copy[0][2]=7
7
8  print(orig)
9  print(copy)
10
11
12
13
14
15
16
17
18
```