# Number Sense Tips & Problem Solving

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Azle ISD – 1974 to 2017

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## **UIL Elementary & Junior High Number Sense**

Individuals are called upon every day to use their ability to make quick mental calculations to make decisions. The development of such abilities should be an integral part of the math curriculum. Concepts covered include, but are not limited to: addition, subtraction, multiplication, division, proportions, and use of mathematical notation.

Students will be given a 10-minute, fill-in-the-blank test which they must complete without doing calculations on paper or on a calculator. Erasures and mark-outs are not permitted.

Every tenth problem is an estimation problem with an integral answer an a 5% range of the answer.

#### **Problem 1 – 20**

- 1. Addition, subtraction, multiplication, & division of whole numbers
- 2. Recognizing place value
- 3. Rounding off whole numbers
- 4. Multiplication short-cuts
- 5. Remainder type problems
- 6. Even & odd number type problems
- 7. Expanded notation
- 8. Sums of whole numbers with regrouping
- 9. Differences of whole numbers with regrouping
- 10. Roman numerals/Arabic numbers conversion

#### **Problems 21 – 40**

- Addition/subtraction of fractions with common denominators
- 2. Addition, subtraction, multiplication, & division of decimal fractions
- 3. Comparing decimal fractions
- 4. Conversion problems (either way): fraction/decimal, percent/fraction, percent/decimal
- 5. Order of operations
- 6. More multiplication short-cuts
- 7. Ratio/proportion
- 8. Consumer type problems

## Problems 21 – 40 (continued)

- 9. Problems about prime numbers
- 10. Greatest common divisor (GCD) & least common multiple (LCM)
- 11. Conversion problems (either way): length, measurements, time

## <u>Problems 41 – 60</u>

- Addition, subtraction, multiplication & division of fractions and mixed numbers
- 2. Substitution problems
- 3. Perimeter/area of: square, rectangle, triangle
- 4. Radius/diameter of a circle
- 5. Powers & roots of numbers

## Problems 41 – 60 (continued)

- 6. Solving simple equations
- 7. Sequences
- 8. Sets
- 9. Word problems
- 10. Volume of cube/rectangular box
- 11. Right triangle problems
- 12. More multiplication short-cuts
- 13. Base systems conversions

## <u>Problems 61 – 80</u>

- 1. Addition, subtraction, multiplication & division of integers
- Inverses
- 3. Basic geometry facts
- 4. More area problems
- 5. Squaring two-digit numbers
- 6. More multiplication short-cuts
- 7. More powers and roots of numbers
- 8. More consumer type problems
- 9. Inequalities
- 10. Probability
- 11. More area problems: parallelogram, rhombus, trapezoid

## Problems 61 – 80 (continued)

- 12. Coordinate geometry number line
- 13. More percent type problems

#### **Problems 1 – 20**

- 1. Addition, subtraction, multiplication & division of whole numbers, fractions, and decimals
- 2. Order of operations
- 3. Use of the distributive property
- 4. Comparison of fractions & decimals
- 5. Multiplication short-cuts
- 6. Squaring numbers
- 7. Roman numerals/Arabic numbers
- 8. Mean, median, mode
- 9. Sums of whole numbers of multiple terms of a finite series

#### **Problems 21 – 40**

- 1. Addition, subtraction, multiplication & division of mixed numbers and integers
- 2. More multiplication short-cuts
- 3. Percent problems
- 4. Conversion problems (either way): English/metric, length, area, capacity, time
- 5. Consumer type problems
- 6. Substitution problems
- 7. Solving simple equations
- 8. Square roots/cube roots
- 9. Greatest common divisor (GCD) & least common multiple (LCM)

## Problems 21 – 40 (continued

- 10. Number theory prime numbers and divisors
- 11. Perimeter/area of: square, rectangle, circle
- 12. Ratio/proportion
- 13. Inverses
- 14. Multiplication of 101, 111

#### **Problems 41 – 60**

- 1. Sets
- 2. Word problems
- 3. Pythagorean theorem
- 4. Sequences

## Problems 41 – 60 (continued)

- 5. Volume/surface area of rectangular solid/cube
- 6. Base systems: conversions and basic operations
- 7. Area of: parallelogram, rhombus, trapezoid, circle
- 8. Solving inequalities
- 9. Basic geometry facts
- 10. Remainder problems

## <u>Problems 61 – 80</u>

- 1. Repeating decimals
- 2. More number theory
- 3. Powers of numbers

## Problems 61 – 80 (continued)

- 4. Volume of: circular cylinder, cone, sphere
- 5. Sequences & series
- 6. Factorial
- 7. Coordinate geometry
- 8. Probability/odds
- 9. More percent type problems: Advanced
- 10. More remainder type problems
- 11. More multiplication short-cuts

$$8 \div 4 = 2$$

$$2 \times 100 =$$

200

$$75 = \frac{300}{4}$$

$$23 \div 4 = 5.75$$

#### **1725**

(3) XXIX = \_\_\_\_\_Arabic Number

$$M = 1000$$
;  $D = 500$ ;  $C = 100$ ;  $L = 50$ ;  $X = 10$ ;  $V = 5$ ;  $I = 1$ 

$$XXIX = 20 + 9$$

(4) 
$$\frac{11}{9} - \frac{5}{9} =$$
 \_\_\_\_\_(fraction)

$$\frac{6}{8}$$

$$\frac{6}{8} \div \frac{2}{2}$$

Since 
$$26 = 25 + 1$$
 and  $24 = 25 - 1$ 

$$24 \times 26 = (25 + 1)(25 - 1)$$

$$24 \times 26 = 25^2 - 1^2$$

$$24 \times 26 = 625 - 1$$

(6) 
$$24 \times 26 =$$
 (Another Way)\_\_\_\_

Since ten's digits are the same

And one's digits add up to 10

Multiply units digits  $\rightarrow$  4 x 6 = 24 – write this down \_\_\_24

Multiply one of the tens digit by the other increased by one  $2 \times (2 + 1) = 6$  – write this down for the finished answer.

(7) 
$$24 \times 26 = ___(Still Another Way)____$$

Multiply  $4 \times 6 = 24 - \text{write down 4}$  and keep 2 in your memory.  $4 \times (LAST)$ 

Multiply 
$$(4 \times 2) + (2 \times 6) + 2 = 22 - \text{write down 2 and keep}$$
 \_\_24  
 $(INNER + OUTER)$  2 in your memory

Multiply  $(2 \times 2) + 2 = 6$  – write this down for the finished answer (FIRST)

$$.121212\ldots = \frac{12}{99}$$

$$\frac{12}{99} \div \frac{3}{3}$$

(9) 
$$1 + 2 + 3 + \ldots + 9 = \underline{\hspace{1cm}}$$

$$1 + 2 + 3 + \ldots + n = \frac{n(n+1)}{2}$$

$$SUM = \frac{9(9+1)}{2}$$
 45

Note: You should know the formulas for sums of odd and even integers also!

For sums of equally spaced numbers, multiply the median of the numbers by the number of terms.

$$SUM = 20 \times 5$$

100

For sums of equally spaced numbers, multiply the median of the numbers by the number of terms.

SUM = 
$$25\frac{1}{2} \times 4$$

(12) 
$$4\frac{1}{3} \times 4\frac{2}{3} =$$
\_\_\_\_(mixed number)

(13) 
$$6\frac{1}{3} \times 3\frac{1}{3} =$$
\_\_\_\_(mixed number)

**(14)** 16% of 36 is 8% of\_\_\_\_\_\_

In equation form looks like this:

$$16\% \times 36 = 8\% \times ?$$

Solving for ? 
$$\rightarrow \frac{16\%}{8\%} \times 36 = ?$$

$$\frac{2}{1}$$
 x 36 = ?

$$5 + 7 = 12$$

$$12 \div 8 = 1$$
 remainder 4

12 · 8 = 1 remainder 4

Write down 4 and "carry" 1-----

(16) The radius of a circle with an area of  $16\pi$  is\_\_\_\_\_

$$A = \pi r^2$$

$$r = \sqrt{\frac{16\pi}{\pi}}$$

(17) 
$$12 \div 4 \times 3 =$$
 \_\_\_\_\_

$$12 \div 4 = 3$$
  $3 \times 3$ 

$$3 \times 3$$

(18) 
$$12 + 4^2 \times 3 =$$

$$4^2 = 16$$

$$16 \times 3 = 48$$

$$12 + 48$$

**60** 

(19) 
$$26 \times 86 =$$
 \_\_\_\_\_

Since one's digits are the same

And ten's digits add up to 10

$$6 \times 6 = 36$$
 – write this down \_\_\_36

 $(2 \times 8) + 6 = 22 - write this down for the finished answer$ 

(20) 113<sup>2</sup> ÷ 4 has a remainder of \_\_\_\_\_

Just look at the last two digits of the number

$$13 \div 4 \rightarrow \text{remainder} = 1$$

$$1^2 \div 4 = 0 + remainder$$

(21) (13<sup>2</sup> + 11 x 15) ÷ 7 has a remainder of \_\_\_\_\_

(22) How many total subsets can be made of the set {A, U, S, T, I, N}? \_\_\_\_\_

The set has 6 elements, so the number of subset is

26

64

(23) The area of a rhombus with diagonals 17 and 20 is \_\_\_\_\_

Area of a rhombus = 
$$\frac{(diagonal_1) \times (diagonal_2)}{2}$$

$$A_{\text{rhombus}} = \frac{17 \times 20}{2}$$
 64

(24) What is the area of a square with diagonal 14?

Area = 
$$\frac{\left(diagonal\right)^2}{2}$$

$$A = \frac{14^2}{2}$$
 98

(25) What is the length of the side of an equilateral triangle with area  $9\sqrt{3}$ ?

$$Area = \frac{\left(side\right)^2 \sqrt{3}}{4} \qquad \rightarrow side = \sqrt{\frac{4(Area)}{\sqrt{3}}}$$

$$side = \sqrt{\frac{4(9\sqrt{3})}{\sqrt{3}}}$$

6

(26) 
$$91 \times 96 =$$
 \_\_\_\_\_

$$100 - 91 = 9$$
 and  $100 - 96 = 4$ .

Multiply 9 x 4 and write down.-----

Subtract 9 from 96 or 4 from 91 and write down.

8736

(27) 
$$6\frac{3}{4} \div \frac{1}{4} =$$

Recall  $\div \frac{1}{4}$  is same as multiplying by 4

Also recall  $6\frac{3}{4}$  is the same as  $(6 + \frac{3}{4})$ 

$$(6 + \frac{3}{4}) \times 4 = 24 + 3$$
 27

(28) 
$$\frac{5}{9} + \frac{9}{5} =$$
\_\_\_\_\_(mixed number)

Write down the number 2 for the whole number part of the answer

$$2\frac{16}{45}$$

$$2\frac{16}{45}$$

Square the difference between the numerator and denominator and place this over the product of the numerator and denominator as the fraction part of the answer.

Starting at the right end of the number group the digits into sets of 3 digits.

Convert each of the sets from base 2 to base 8 numbers and write down as final answer.

Recall 
$$\frac{5}{8} = .625$$

$$\frac{5000}{8}$$
 × 240 = 150000

142 272 - 157 248

\*(32) 
$$101^2 - 99^2 =$$

$$(101 - 99) \times (101 + 99)$$
  
 $(2) \times (200)$   
 $= 400$ 

380 - 420

$$\frac{1}{6} \approx .167$$

$$\frac{1000}{6} \times 360 + 0$$

56 987 - 62 985

\*(34) 
$$269 \times 3\frac{5}{9} =$$
\_\_\_\_\_

$$270 \times \frac{32}{9}$$

$$270 \div 9 = 30$$

$$30 \times 32 = 960$$

$$909 - 1005$$

\*(35) 
$$\sqrt{224} \times \sqrt{325} =$$

Recall:  $15^2 = 225$  and  $18^2 = 324$ 

$$15 \times 18 = 270$$

257 - 283

\*(36) 
$$83\frac{1}{3} \times 2390 =$$
\_\_\_\_\_

Recall: 
$$\frac{5}{6} = .83333...$$

$$\frac{500}{6}$$
 x 2400 = 200000

# Sample Problems (Practice)

(1) 
$$25 \times 32 =$$

(2) 
$$1 + 2 + 3 + \ldots + 19 = \underline{\hspace{1cm}}$$

(3) 
$$97 \times 93 =$$

- (4) What is the area of a square with diagonal 8?
- (5) DCLX = \_\_\_\_\_(Arabic Number)
- (6)  $17 \times 97 =$
- (7)  $113^2 \div 9$  has a remainder of\_\_\_\_\_
- (8)  $77 \times 73 =$
- \*(9) 119 x 165 = \_\_\_\_
- \*(10) 119 x 251 = \_\_\_\_\_

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No Sense in Mathematics (4th edition). By Don Skow

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