## Pearson Edexcel

Mark Scheme (Results)
January 2021

Pearson Edexcel International GCSE
Mathematics A (4MA1)
Paper 1H

## Edexcel and BTEC Qualifications

Edexcel and BTEC qualifications are awarded by Pearson, the UK's largest awarding body. We provide a wide range of qualifications including academic, vocational, occupational and specific programmes for employers. For further information visit our qualifications websites at www.edexcel.com or www.btec.co.uk. Alternatively, you can get in touch with us using the details on our contact us page at www.edexcel.com/contactus.

## Pearson: helping people progress, everywhere

Pearson aspires to be the world's leading learning company. Our aim is to help everyone progress in their lives through education. We believe in every kind of learning, for all kinds of people, wherever they are in the world. We've been involved in education for over 150 years, and by working across 70 countries, in 100 languages, we have built an international reputation for our commitment to high standards and raising achievement through innovation in education. Find out more about how we can help you and your students at: www.pearson.com/uk

January 2021
Publications Code 4MA1_1H_2101_MS
All the material in this publication is copyright
© Pearson Education Ltd 2021

## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.
Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.
- Types of mark
- M marks: method marks
- A marks: accuracy marks
- B marks: unconditional accuracy marks (independent of M marks)
- Abbreviations
- cao - correct answer only
- ft - follow through
- isw - ignore subsequent working
- SC - special case
- oe - or equivalent (and appropriate)
- dep - dependent
- indep - independent
- awrt - answer which rounds to
- eeoo - each error or omission


## - No working

If no working is shown then correct answers normally score full marks
If no working is shown then incorrect (even though nearly correct) answers score no marks.

## - With working

If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.
If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.
If a candidate misreads a number from the question. Eg. Uses 252 instead of 255; method marks may be awarded provided the question has not been simplified. Examiners should send any instance of a suspected misread to review. If there is a choice of methods shown, mark the method that leads to the answer on the answer line; where no answer is given on the answer line, award the lowest mark from the methods shown.
If there is no answer on the answer line then check the working for an obvious answer.

- Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.
It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.
Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

## - Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded to another.

## International GCSE Maths

Apart from questions 5(b), 15, 17, 18, 19, 23 and 24 (where the mark scheme states otherwise) the correct answer, unless clearly obtained by an incorrect method, should be taken to imply a correct method

| Q | Working | Answer | Mark |  | Notes |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\begin{aligned} & \text { e.g. } 0.7 \times 20160 \text { oe }(=14112) \\ & \text { or } 0.3 \times 20160 \text { oe }(=6048) \end{aligned}$ |  | 4 | M1 |  |
|  | $\begin{aligned} & \hline \text { e.g. " } 14112 " \div(9+5+2)(=882) \\ & \text { or }(20160-" 6048 ") \div(9+5+2)(=882) \end{aligned}$ |  |  | M1 | $\begin{aligned} & \text { M2 for } \\ & \frac{9-2}{9+5+2} \times \text { "14112" oe } \end{aligned}$ |
|  | e.g. $9 \times$ " 882 " - $2 \times$ " 882 " |  |  | M1 |  |
|  |  | 6174 |  | A1 |  |
|  |  |  |  |  | Total 4 |


| 2 (a) |  | $70<s \leq 80$ | 1 | B1 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (b) | $\begin{aligned} & 10 \times 45+16 \times 55+19 \times 65+23 \times 75+12 \times 85 \\ & \text { or } 450+880+1235+1725+1020(=5310) \end{aligned}$ |  | 4 | M2 | $f \times d$ for at least 4 products with correct mid-interval values and intention to add. <br> If not M2 then award M1 <br> for $d$ used consistently for at least 4 products within interval (including end points) and intention to add or <br> for at least 4 correct products with correct mid-interval values with no intention to add |
|  | " $5310 " \div 80$ |  |  |  | dep on at least M1 allow division by their $\sum f$ provided addition or total under column seen |
|  |  | 66.4 |  | A1 | accept 66.37-66.4 |
|  |  |  |  |  | Total 5 marks |


| 3 | $\begin{aligned} & \text { e.g. } 30 \times 20 \times 125(=75000) \\ & \text { or } 85 \times 40 \times 125(=425000) \\ & \text { or }(60 \times 30+(85-30) \times 40) \times 125(=500000) \text { oe } \end{aligned}$ |  | 4 | M1 for a method to find the volume of water already pumped out or the volume of water left or the total volume of the container |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & " 75000 " \div 1.5(=50000) \\ & \text { or " } 75000 " \div 90\left(=833.3 \ldots \text { or } \frac{2500}{3}\right) \\ & \text { or " } 425000 " \div 75000 "\left(=5.66 \ldots \text { or } \frac{17}{3}\right) \\ & \text { or " } 500000 " \div " 75000 "\left(=6.66 \ldots \text { or } \frac{20}{3}\right) \end{aligned}$ |  |  | M1 | $\begin{aligned} & \text { M2 for } \frac{425000 "}{" 75000 "} \times 1.5 \text { oe }(=8.5) \\ & \text { or } \frac{" 500000 "}{" 75000 "} \times 1.5 \text { oe }(=10) \end{aligned}$ |
|  | $\begin{aligned} & " 425000 " \div \text { " } 50000 "(=8.5) \\ & \text { or " } 425000 " \div(" 833.3 \ldots " \times 60) \text { oe }(=8.5) \\ & \text { or " } 5.66 \ldots . " \times 1.5(=8.5) \text { or " } 6.66 \ldots . . \times 1.5(=10) \end{aligned}$ |  |  | M1 |  |
|  |  | 2030 |  | A1 Allow 830 (pm) |  |
|  |  |  |  |  | Total 4 marks |


| $\mathbf{4}$ (i) |  | 21,27 | 1 | B1 |
| :--- | :--- | :--- | :--- | :--- |
|  | (ii) |  | $21,23,24,25,27,29$ | 1 |
|  |  |  |  | B1 |
|  |  |  | Total 2 marks |  |


| $5 \quad \text { (a) }$ |  | $5 y^{3}(3 y+4 u)$ | 2 |  | for $5 y^{3}(3 y+4 u)$ <br> for $5 y\left(3 y^{3}+4 u y^{2}\right)$ <br> or $5 y^{2}\left(3 y^{2}+4 u y\right)$ <br> or $y^{2}\left(15 y^{2}+20 u y\right)$ <br> or $y^{3}(15 y+20 u)$ <br> or $5 y^{3}(\ldots)$ where there is only one mistake in the brackets) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (b) | $\begin{aligned} & 4 \times(4-3 x)=5-8 x \text { oe } \\ & \text { or } 16-12 x=5-8 x \text { oe } \\ & \text { or } 4-3 x=\frac{5}{4}-2 x \text { oe } \end{aligned}$ |  | 3 | M | for removal of fraction in a correct equation |
|  | e.g. $16-5=12 x-8 x$ <br> or $11=4 x$ oe <br> or $4-\frac{5}{4}=3 x-2 x$ |  |  | M | for terms in $x$ on one side and numbers on the other side in an equation, allow correct rearrangement of their equation in the form $a x+b=c x+d$ |
|  |  | 2.75 |  |  | $\text { (dep on M1) oe e.g. } 2 \frac{3}{4} \text { or } \frac{11}{4}$ |
|  |  |  |  |  | Total 5 marks |


| $\mathbf{6}$ (a) |  | $2.84 \times 10^{9}$ | 1 | B1 |  |
| :--- | :--- | :--- | :---: | :---: | :---: |
|  | (b) |  | 0.00025 | 1 | B1 |
|  |  |  |  |  |  |


| 7 (a) | for $0.035 \times 40000$ oe $(=1400)$ <br> or $1.035 \times 40000 ~ o e ~$ <br> $(=41400)$ OR <br> $1.035 \times 41400 "$ oe $(=4289)$  |  | 3 |  | for finding $3.5 \%$ or $103.5 \%$ of 40000 | $\begin{aligned} & \hline \text { OR M2 for } 40000 \times \\ & 1.035^{3} \\ & \text { or } 40000 \times 1.035^{4} \\ & (=45900.92) \\ & \\ & (\text { M1 for } 40000 \times \\ & \left.1.035^{2}(=42849)\right) \\ & \hline \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1.035 \times$ "41 400" oe (=42 849)  <br> $1.035 \times$ "42 849" oe (=44 348.72) $40000 \times$ <br>  $1.035^{3}$ |  |  |  | for completing method to find total amount in the account |  |
|  |  | 44349 |  | A1 | accept 44348-44349 |  |
|  |  |  |  |  | SC: if no other marks $g$ $0.105 \times 40000$ oe or 42 <br> accept $(1+0.035)$ as eq throughout | ined award M1 for 00 or 44200 <br> ivalent to 1.035 |
| (b) | e.g. $30481 \div(1-0.065)$ or $30481 \div 0.935$ |  | 3 | M2 <br> (M1) | for a complete method <br> for $30481 \div(100-6.5)$ <br> or $(100-6.5) \%=3048$ <br> or e.g. $(1-0.065) x=30$ | $\begin{aligned} & (=326) \\ & 1 \text { or } 93.5 \%=30481 \\ & 481 \end{aligned}$ |
|  |  | 32600 |  | A1 |  |  |
|  |  |  |  |  |  | Total 6 mark |


| 8 | $\begin{aligned} & 2 \times \pi \times 7(=43.982 \ldots \text { or } 14 \pi) \\ & \text { or }(2 \times \pi \times 7) \div 2(=21.991 \ldots \text { or } 7 \pi) \\ & \text { or } 2 \times \pi \times 9(=56.548 \ldots \text { or } 18 \pi) \\ & \text { or }(2 \times \pi \times 9) \div 2(=28.274 \ldots \text { or } 9 \pi) \\ & \hline \end{aligned}$ |  | 3 | M1 for finding the circumference of either the full circle or the length of the arc for either semicircle |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { e.g. " } 21.991 "+">28.274 "(=50.26 \ldots) \\ & \text { or " } 7 \pi \pi+" 9 \pi "(=16 \pi) \\ & \text { or " } 21.991 "+" 28.274 "+2(=52.26 \ldots) \\ & \text { or " } 7 \pi "+" 9 \pi "+2(=52.26 \ldots) \\ & \text { or " } 21.991 "+" 28.274 "+2+2 \\ & \text { or " } 7 \pi "+" 9 \pi "+2+2 \end{aligned}$ |  |  | M | for a method to find the length of the two arcs with intention to add |
|  |  | 54.3 |  | A1 | accept $54.2-54.3$ |
|  |  |  |  |  | Total 3 marks |


| 9 (a) |  | $16 x^{12} y^{20}$ | 2 | B2 | B1 for an answer in the form $a x^{n} y^{m}$ with 2 correct from $a=16, n=12, m=20$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (b)(i) | $(x \pm 9)(x \pm 4)$ |  | 2 |  | for $(x \pm 9)(x \pm 4)$ <br> or for $(x+a)(x+b)$ <br> where $a b=-36$ or $a+b=5$ |
|  |  | $(x+9)(x-4)$ |  | A1 |  |
| (ii) |  | -9, 4 | 1 | B1 | ft from (b)(i) |
|  |  |  |  |  | Total 5 m |


| 10 | $\begin{aligned} & \text { e.g. } \sin 65=\frac{16}{A B} \text { or } \cos 25=\frac{16}{A B} \\ & \text { or } \frac{A B}{\sin 90}=\frac{16}{\sin 65} \text { or } \tan 65=\frac{16}{A D} \\ & \text { or } \tan 25=\frac{A D}{16} \text { or } \frac{A D}{\sin 25}=\frac{16}{\sin 65} \end{aligned}$ |  | 4 | M1 for a correct trig ratio for $A B$ or $A D$ accept $180-90-65$ for 25 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { e.g. }(A B=) \frac{16}{\sin 65}(=17.654 \ldots) \\ & \text { or }(A B=) \frac{16}{\cos 25}(=17.654 \ldots) \\ & \text { or }(A B=) \frac{16 \sin 90}{\sin 65}(=17.654 \ldots) \\ & \text { and } \\ & (A D=) \frac{16}{\tan 65}(=7.460 \ldots) \\ & \text { or }(A D)=16 \times \tan 25(=7.460 \ldots) \\ & \text { or }(A D=) \frac{16 \sin 25}{\sin 65}(=7.460 \ldots) \end{aligned}$ |  |  |  | for finding $A B$ and $A D$ <br> Allow use of Pythagoras $(A D=) \sqrt{117.654 \ldots{ }^{.2}-16^{2}}(=7.460 \ldots)$ <br> or $(A B=) \sqrt{17.460 \ldots .^{2}+16^{2}}(=17.654 \ldots)$ |
|  | $(" 17.654 \ldots \times 2)+\left({ }^{\prime} 7.460 \ldots>\times 2\right)$ oe |  |  |  | for a complete method to find the perimeter |
|  |  | 50.2 |  | A1 | accept $49.6-50.6$ |
|  |  |  |  |  | Total 4 marks |


| $\mathbf{1 1}$ (a) |  |  | 2 | M1 for use of cf at 45 |
| :--- | :--- | :--- | :---: | :--- |
|  |  | 146 |  | A1 accept in the range $145-147$ |
| (b) | $93.75 \div 3.75(=25)$ |  | 3 | M1 |
|  | Using cf diagram at $90-" 25 "(=65)$ |  | M1 for use of cf at " 65 " |  |
|  |  | 151 |  | A1 accept in the range $150-152$ |
|  |  |  |  |  |


| $12$ <br> (a) | $\begin{aligned} & \frac{4(x+1)-3(x-2)}{(x-2)(x+1)} \\ & \text { or } \frac{4(x+1)}{(x-2)(x+1)}-\frac{3(x-2)}{(x-2)(x+1)} \end{aligned}$ |  | 3 | M1 for expressing both fractions correctly with a common denominator. |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\frac{4 x+4-3 x+6}{(x-2)(x+1)} \text { or } \frac{4 x+4-3 x+6}{x^{2}-x-2}$ |  |  |  | for removing brackets in a single fraction with a correct denominator. Allow denominator to be expanded. Allow one error in the expansion of the numerator. |
|  |  | $\frac{x+10}{(x-2)(x+1)}$ |  |  | accept $\frac{x+10}{x^{2}-x-2}$ oe |
| (b) | $\begin{aligned} & 2 x(x-5)=2 x^{2}-10 x \\ & \text { or } 2 x(x-3)=2 x^{2}-6 x \\ & \text { or }(x-5)(x-3)=x^{2}-5 x-3 x+15\left(=x^{2}-8 x+15\right) \end{aligned}$ |  | 3 | M | for multiplying $2 x$ by a bracket with both terms correct or the 2 brackets with at least 3 out of 4 terms correct or at least 2 out of 3 terms correct |
|  | $\begin{aligned} & \left(2 x^{2}-10 x\right)(x-3)=2 x^{3}-6 x^{2}-10 x^{2}+30 x \\ & \text { or }\left(2 x^{2}-6 x\right)(x-5)=2 x^{3}-10 x^{2}-6 x^{2}+30 x \\ & \text { or } 2 x\left(x^{2}-5 x-3 x+15\right)=2 x^{3}-10 x^{2}-6 x^{2}+30 x \\ & \text { or } 2 x\left(x^{2}-8 x+15\right)=2 x^{3}-16 x^{2}+30 x \end{aligned}$ |  |  |  | (dep) for multiplying the product of $2 x$ and the $1^{\text {st }}$ bracket (ft from the $1^{\text {st }}$ stage) by the $2^{\text {nd }}$ bracket and getting at least 3 out of 4 terms correct <br> or multiplying the product of the 2 brackets (ft from the $1^{\text {st }}$ stage) by the $2 x$, and getting at least 3 out of 4 or 2 out of 3 terms correct |
|  |  | $2 x^{3}-16 x^{2}+30 x$ |  | A1 |  |
|  |  |  |  |  | Total 6 marks |


| $\mathbf{1 3}$ (a) | $\frac{8--4}{5-9}\left(=\frac{12}{-4}\right)$ oe or $\frac{-4-8}{9-5}\left(=\frac{-12}{4}\right)$ oe | 2 | M1condone correct gradient embedded <br> in an equation e.g. $y=-3 x+c$ <br> or expression e.g. $-3 x$ <br> or for an answer of 3 <br>  <br> (b) |  |
| :---: | :---: | :---: | :---: | :--- |


| 14 (a) | $0.6 \times 0.9$ |  | 2 | M1 | oe |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 0.54 |  |  | $\text { oe e.g. } \frac{27}{50}, \frac{54}{100}, 54 \%$ |
| (b) | $\begin{aligned} & \hline 0.6 \times 0.1(=0.06) \\ & \text { or } 0.4 \times 0.25(=0.1) \\ & \text { or } 0.4 \times 0.75(=0.3) \\ & \hline \end{aligned}$ |  | 3 | M1 | oe |
|  | $\begin{aligned} & 0.6 \times 0.1+0.4 \times 0.25 \\ & \text { or } 1-(0.4 \times 0.75)-" 0.54 " \end{aligned}$ |  |  | M | oe, ft their answer from (a) |
|  |  | 0.16 |  |  | $\text { oe e.g. } \frac{4}{25}, \frac{8}{50}, \frac{16}{100}, 16 \%$ |
|  |  |  |  |  | Total 5 |


| 15 | 9.55 or 9.65 or 3.75 or 3.85 or 1.835 or 1.845 |  | 3 |  | accept $9.64 \dot{9}$ for $9.65,3.84 \dot{9}$ for 3.85 , $1.844 \dot{9}$ for 1.845 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $a=\frac{U B_{v}-L B_{u}}{L B_{t}} \text { e.g. } a=\frac{9.65-3.75}{1.835}(=3.2152 \ldots)$ |  |  | M1 | for correct substitution of $\begin{aligned} & 9.6<U B_{v} \square 9.65 \\ & \text { and } 3.75 \square L B_{u}<3.8 \\ & \text { and } 1.835 \square L B_{t}<1.84 \end{aligned}$ |
|  |  | 3.22 |  | A1 | accept 3.21-3.22 from correct working |
|  |  |  |  |  | Total 3 marks |


| 16 | $\left(B C^{2}=\right) 150^{2}+275^{2}-(2 \times 150 \times 275 \times \cos 120)(=139375)$ |  | 5 |  | for correct substitution into the cosine rule |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & (B C=) \sqrt{150^{2}+275^{2}+41250} \text { oe or } \sqrt{139375} \\ & \text { or } 25 \sqrt{223} \text { or } 373 \ldots . \end{aligned}$ |  |  |  | for correct order of operations and square root |
|  | $\begin{aligned} & \text { e.g. } \frac{\sin A B C}{275}=\frac{\sin 120}{" 373 \ldots . . "} \\ & \text { or } 275^{2}=150^{2}+" 373 \ldots{ }^{2}-(2 \times 150 \times " 373 \ldots " \times \cos A B C) \\ & \text { or } \cos A B C=\frac{150^{2}+" 373 \ldots{ }^{\prime 2}-275^{2}}{2 \times 150 \times " 373 \ldots "} \\ & \text { or } \frac{\sin A C B}{150}=\frac{\sin 120}{" 373 \ldots "} \\ & \text { or } 150^{2}=275^{2}+" 373 \ldots{ }^{2}-(2 \times 275 \times " 373 \ldots " \times \cos A C B) \\ & \text { or } \cos A C B=\frac{275^{2}+" 373 \ldots{ }^{2}-150^{2}}{2 \times 275 \times " 373 \ldots "} \\ & \hline \end{aligned}$ |  |  |  | (dep on $1^{\text {st }} \mathrm{M} 1$ ) ft $373 \ldots$ <br> for a correct trig statement involving angle $A B C$ or angle $A C B$ |
|  | $\begin{aligned} & (A B C=) \sin ^{-1}\left(\frac{\sin 120}{" 373 \ldots . .} \times 275\right)(=39.6 \ldots) \\ & \text { or }(A B C=) \cos ^{-1}\left(\frac{150^{2}+" 373 \ldots{ }^{2}-275^{2}}{2 \times 150 \times " 373 \ldots "}\right)(=39.6 \ldots) \\ & \text { or }(A C B=) \sin ^{-1}\left(\frac{\sin 120}{" 373 \ldots "} \times 150\right)(=20.3 \ldots) \\ & \text { or }(A C B=) \cos ^{-1}\left(\frac{275^{2}+" 373 \ldots{ }^{2}-150^{2}}{2 \times 275 \times " 373 \ldots "}\right)(=20.3 \ldots) \end{aligned}$ |  |  |  | for a complete method to find angle $A B C$ or angle ACB |
|  |  | 140 |  |  | accept $140-140.4$ |
|  |  |  |  |  | Total 5 marks |

$\left.\begin{array}{|l|l|l|l|l|}\hline \mathbf{1 7} & \begin{array}{l}\text { e.g. }(V=) \frac{1}{2}\left(\frac{4}{3} \pi x^{3}\right)+\pi x^{2}(20-4 x) \\ \text { or }(V=) \frac{2}{3} \pi x^{3}+20 \pi x^{2}-4 \pi x^{3}\end{array} & 5 & \text { M1 for a correct expression } \\ \hline & \begin{array}{l}\text { e.g. } \frac{1}{3} \pi y=\frac{1}{2}\left(\frac{4}{3} \pi x^{3}\right)+\pi x^{2}(20-4 x) \\ \text { or } \frac{1}{3} \pi y=\frac{2}{3} \pi x^{3}+20 \pi x^{2}-4 \pi x^{3}\end{array} & & \text { M1 for a correct equation } \\ \hline & y=60 x^{2}-10 x^{3} \text { oe } & & & \text { A1 for writing } y \text { in terms of } x\end{array} \quad \begin{array}{l}\text { for differentiating their } a x^{2}+b x^{3} \\ \text { and equating to 0 }\end{array}\right]$
\(\left.$$
\begin{array}{|l|l|l|l|l|}\hline 18 & \begin{array}{l}\text { e.g. } 40+8 \sqrt{x}-5 \sqrt{x}-\sqrt{x} \sqrt{x} \\
\text { or } 40+8 \sqrt{x}-5 \sqrt{x}-(\sqrt{x})^{2} \\
\text { or } 40+8 \sqrt{x}-5 \sqrt{x}-x \\
\text { or } 40+3 \sqrt{x}-x\end{array} & 3 & \begin{array}{l}\text { M1 } \\
\text { for a correct expansion with at } \\
\text { least } 3 \text { out of } 4 \text { terms correct oe } \\
\text { or all } 3 \text { terms correct }\end{array}
$$ <br>

\hline \& \& x=19 \& \& A1 (dep on M1) for x=19\end{array}\right]\)| B1 for $y=3$ |
| :--- |


| 19 | $(1-2 y)^{2}-9 y-(1-2 y)=2 y^{2}-12$ | $x^{2}-9\left(\frac{1-x}{2}\right)-x=2\left(\frac{1-x}{2}\right)^{2}-12$ |  | 5 | M1 substitution of linear equation into quadratic |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | e.g. $2 y^{2}-11 y+12(=0)$ oe allow $2 y^{2}-11 y=-12$ oe | e.g. $x^{2}+9 x+14(=0)$ oe allow $x^{2}+9 x=-14$ oe |  |  | A1 (dep on M1) writing the correct quadratic expression in the form $a x^{2}+b x+c(=0)$ <br> allow $a x^{2}+b x=c$ |
|  | $\begin{aligned} & \text { e.g. }(2 y-3)(y-4)(=0) \\ & (y=) \frac{11 \pm \sqrt{(-11)^{2}-4 \times 2 \times 12}}{2 \times 2} \\ & \text { e.g. } \\ & 2\left[\left(y-\frac{11}{4}\right)^{2}-\left(\frac{11}{4}\right)^{2}\right]=-12 \mathrm{oe} \end{aligned}$ | $\begin{aligned} & \text { e.g. }(x+7)(x+2)(=0) \\ & (x=) \frac{-9 \pm \sqrt{9^{2}-4 \times 1 \times 14}}{2} \\ & \text { e.g. }\left(x+\frac{9}{2}\right)^{2}-\left(\frac{9}{2}\right)^{2}=-14 \end{aligned}$ |  |  | M1 (dep on M1) for a complete method to solve their 3-term quadratic equation (allow one sign error and some simplification - allow as far as $\left.\frac{11 \pm \sqrt{121-72}}{4} \text { or } \frac{-9 \pm \sqrt{81-56}}{2}\right)$ |
|  | $y=\frac{3}{2}$ oe and $y=4$ | $x=-7$ and $x=-2$ |  |  | A1 (dep on M1) both $x$-values or both $y$-values |
|  |  |  | $\begin{gathered} x=-2 \\ y=\frac{3}{2} \text { oe } \\ \text { and } \\ x=-7, \\ y=4 \end{gathered}$ |  | A1 (dep on first M1) must be paired correctly |


| 20 | $\sqrt[3]{\frac{4352}{1836}}$ or $\frac{4}{3}$ or $1.33(33 \ldots)$ or $4: 3$ or $\sqrt[3]{\frac{1836}{4352}}$ or $\frac{3}{4}$ or 0.75 or $3: 4$ |  | 3 | M1 | for a correct length scale factor or a correct length ratio |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | e.g. $1120 \div\left(4 \frac{4}{3}\right)^{2}$ oe or $1120 \times\left(4 \frac{3}{4}\right)^{2}$ oe |  |  | M | (dep on M1) for a correct method to work out the surface area of A |
|  |  | 630 |  | A1 |  |
|  |  |  |  |  | Total 3 marks |


| $\mathbf{2 1}$ (a)(i) |  | $(-12,15)$ | 1 | B1 |  |
| :--- | :--- | :--- | :---: | :---: | :---: |
|  | (ii) |  | $(-9,5)$ | 1 | B1 |
|  | (b) |  | $a=2$ and $b=90$ | 2 | B2for both values correct <br> (B1 for $a=2$ or $b=90$ <br> or $a=-2$ and $b=-90)$ |
|  |  |  |  | Total 4 marks |  |


| 22 | $y=(x-4)^{2}-4^{2}(+5)$ oe or $x=(y-4)^{2}-4^{2}(+5)$ |  | 3 |  | for a correct first step in order to complete the square |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $y=4 \pm \sqrt{11+x}$ or $x=4 \pm \sqrt{11+y}$ |  |  |  | allow $y=4+\sqrt{11+x}$ <br> or $x=4+\sqrt{11+y}$ |
|  |  | 4- $\sqrt{x+11}$ |  | A1 | oe |
|  |  |  |  |  | Total 3 marks |


| 22 | $x^{2}-8 x+(5-y)=0$ <br> $(x=) \frac{8 \pm \sqrt{(-8)^{2}-4 \times 1 \times(5-y)}}{2 \times 1}$ <br> or $y^{2}-8 y+(5-x)=0$ <br> $(y=) \frac{8 \pm \sqrt{(-8)^{2}-4 \times 1 \times(5-x)}}{2 \times 1}$ | 3 <br> ALT | for a correct first step in preparation <br> for use of quadratic formula and <br> substitution into the quadratic <br> formula (allow one sign error) |  |
| :--- | :--- | :--- | :--- | :--- |
|  | $y=4 \pm \sqrt{11+x}$ or $x=4 \pm \sqrt{11+y}$ |  | A1allow $y=4+\sqrt{11+x}$ <br> or $x=4+\sqrt{11+y}$ |  |
|  |  | $4-\sqrt{x+11}$ |  | A1 oe |
|  |  |  | Total 3 marks |  |


| $\begin{gathered} 22 \\ \mathbf{A L T}^{2} \end{gathered}$ | Using $a x^{2}+b x+c=a(x+p)^{2}+q$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\left(p=\frac{b}{2 a}\right)=\frac{-8}{2}(=-4)$ and $q=(4)^{2}-8(4)+5(=-11)$ |  | 3 |  | for finding $p$ and $q$ |
|  | $y=4 \pm \sqrt{11+x}$ or $x=4 \pm \sqrt{11+y}$ |  |  |  | $\begin{aligned} & \text { allow } y=4+\sqrt{11+x} \\ & \text { or } x=4+\sqrt{11+y} \end{aligned}$ |
|  |  | 4- $\sqrt{x+11}$ |  |  | oe |
|  |  |  |  |  |  |


| 23 | $\overrightarrow{A B}=2 \mathbf{b}-2$ a oe or $\overrightarrow{B A}=2 \mathbf{a}-2 \mathbf{b}$ oe or $\overrightarrow{A M}=\mathbf{b}-\mathbf{a}$ oe or $\overrightarrow{M A}=\mathbf{a}-\mathbf{b}$ oe or $\overrightarrow{B M}=\mathbf{b}-\mathbf{a}$ oe or $\overrightarrow{M B}=\mathbf{a}-\mathbf{b}$ oe |  | 6 | M1 for finding $\overrightarrow{A B}$ or $\overrightarrow{B A}$ or $\overrightarrow{A M}$ or $\overrightarrow{M A}$ or $\overrightarrow{B M}$ or $\overrightarrow{M B}$ |
| :---: | :---: | :---: | :---: | :---: |
|  | e.g. $\overrightarrow{O M}=2 \mathbf{a}+(\mathbf{b}-\mathbf{a})(=\mathbf{a}+\mathbf{b})$ oe or $\overrightarrow{M O}=(\mathbf{b}-\mathbf{a})-2 \mathbf{b}(=-\mathbf{a}-\mathbf{b})$ oe or $\overrightarrow{A N}=\frac{4}{3} \mathbf{b}-2 \mathbf{a}$ oe or $\overrightarrow{N A}=2 \mathbf{a}-\frac{4}{3} \mathbf{b}$ oe |  |  | M1 for finding $\overrightarrow{O M}$ or $\overrightarrow{M O}$ or $\overrightarrow{A N}$ or $\overrightarrow{N A}$ |
|  | e.g. $\overrightarrow{O P}=2 \mathbf{a}+\lambda\left(\frac{4}{3} \mathbf{b}-2 \mathbf{a}\right)$ oe or $\overrightarrow{O P}=\frac{4}{3} \mathbf{b}+\lambda\left(2 \mathbf{a}-\frac{4}{3} \mathbf{b}\right)$ oe or $\overrightarrow{O P}=\mu(\mathbf{a}+\mathbf{b})$ oe $\mathbf{O R} \overrightarrow{M P}=\mathbf{a}-\mathbf{b}+k\left(\frac{4}{3} \mathbf{b}-2 \mathbf{a}\right)$ oe or $\overrightarrow{M P}=\mathbf{b}-\mathbf{a}-\frac{2}{3} \mathbf{b}+k\left(2 \mathbf{a}-\frac{4}{3} \mathbf{b}\right)$ oe or $\overrightarrow{M P}=t(-\mathbf{a}-\mathbf{b})$ oe |  |  | M1 for finding $\overrightarrow{O P}$ or $\overrightarrow{P O}$ or $\overrightarrow{M P}$ or $\overrightarrow{P M}$ |
|  | e.g. $2 \mathbf{a}+\lambda\left(\frac{4}{3} \mathbf{b}-2 \mathbf{a}\right)=\mu(\mathbf{a}+\mathbf{b})$ oe or $\frac{4}{3} \mathbf{b}+\lambda\left(2 \mathbf{a}-\frac{4}{3} \mathbf{b}\right)=\mu(\mathbf{a}+\mathbf{b})$ oe or $\mathbf{a}-\mathbf{b}+k\left(\frac{4}{3} \mathbf{b}-2 \mathbf{a}\right)=t(-\mathbf{a}-\mathbf{b})$ oe or $\mathbf{b}-\mathbf{a}-\frac{2}{3} \mathbf{b}+k\left(2 \mathbf{a}-\frac{4}{3} \mathbf{b}\right)=t(-\mathbf{a}-\mathbf{b})$ oe |  |  | M1 for setting up an equation for $\overrightarrow{O P}$ or $\overrightarrow{M P}$ |
|  | $\mu=\frac{4}{5}$ or $t=\frac{1}{5}$ |  |  | M1 for finding $\mu$ or $t$ for either $\overrightarrow{O P}=\mu \overrightarrow{O M}$ or $\overrightarrow{M P}=t \overrightarrow{M O}$ |
|  |  | 4:1 |  | A1 cao (dep on M3) |
|  |  |  |  | Total 6 marks |


| $\mathbf{2 4}$ | $\frac{2 n}{2}[2 a+(2 n-1) d] \mathrm{oe}$ |  | 4 | M1 for a correct expression for $S_{2 n}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | $\frac{2 n}{2}[2 a+(2 n-1) d]=4 \times \frac{n}{2}[2 a+(n-1) d]$ oe |  |  | M1dep on M1 for setting up a correct <br> equation for $S_{2 n}=4 \times S_{n}$ |
|  | $2 a-d=4 a-2 d$ oe |  |  | M1 for a correct linear expression in $a$ |
| and $d$ |  |  |  |  |

