Lesson 12: Systems of Inequalities Word Problems

Example 1

The girls' swim team is hosting a fund raiser. They would like to raise at least \$500. They are selling candles for \$5 and flower arrangements for \$6. The girls estimate that at most they will sell 200 items.

- Write a system of inequalities to represent this situation.
- Graph each inequality on the grid.
- 120 candles have been sold. Use your graph to determine a reasonable number of flower arrangements that must be sold in order for the girls to reach their goal of at least \$500. Justify your answer.





1. The ninth graders are hosting the next school dance. They would like to make at least a \$500 profit from selling tickets. The ninth graders estimate that at most 300 students will attend the dance. They will earn \$3 for each ticket purchased in advance and \$4 for each ticket purchased at the door.

- Write a system of inequalities to represent this situation.
- Graph each inequality on the grid.

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• Suppose only 30 people buy advance tickets. How many people would need to buy tickets at the door? (Identify one realistic solution). Justify your answer.

 In order to prepare for your summer bash, you go to the supermarket to buy hamburgers and chicken. Hamburgers cost \$2 per pound and chicken costs \$3 per pound. You have no more than \$30 to spend. You expect to purchase at least 3 pounds of hamburgers.

- Write a system of inequalities to represent this situation.
- Graph the system of inequalities on the grid.
- Give three possible combinations for buying hamburgers and chicken for your summer bash.
- Justify your answers.





3. Jenny is making jewelry for an Arts and Crafts show. She would like to make at least \$100 in sales. She estimates that she will sell at most 50 pieces of jewelry. The bracelets that she is selling cost \$2 and the necklaces cost \$3.

- Write a system of inequalities to represent this situation.
- Graph each inequality on the grid below.
- Give two possible combinations of bracelets and necklaces that can be sold in order for Jenny to meet her goal. Justify your answer.

4. Jason is buying wings and hot dogs for a party. One package of wings costs \$7. Hot dogs cost \$5 per package. He must spend no more than \$40.

- Write an inequality to represent the cost of Jason's food for the party.
- Jason knows that he will be buying at least 5 packages of hot dogs. Write an inequality to represent this situation.
- Graph both inequalities. Give two options for Jason when buying wings and hot dogs.



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A Dinner Theatre actress is paid \$250 per day to rehearse the play and \$500 per day to perform in front of an audience. In one season, an actress earned between \$2000 and \$5000.

- Write a system of inequalities that represents this situation. (2 points)
- Graph the system of inequalities on the grid. (2 points)
- Identify two different ways the actress may have earned her salary. Justify your answers. (2 points)

Lesson 12: Systems of Inequalities Word Problems (Answer Key)

1. The ninth graders are hosting the next school dance. They would like to make at least a \$500 profit from selling tickets. The ninth graders estimate that at most 300 students will attend the dance. They will earn \$3 for each ticket purchased in advance and \$4 for each ticket purchased at the door.

- Write a system of inequalities to represent this situation.
- Graph each inequality on the grid.

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• Suppose only 30 people buy advance tickets. How many people would need to buy tickets at the door? (Identify one realistic solution) Justify your answer.



2. In order to prepare for your summer bash, you go to the supermarket to buy hamburgers and chicken. Hamburgers cost \$2 per pound and chicken costs \$3 per pound. You have no more than \$30 to spend. You expect to purchase at least 3 pounds of hamburgers.

- Write a system of inequalities to represent this situation.
- Graph the system of inequalities on the grid.
- Give three possible combinations for buying hamburgers and chicken for your summer bash.
- Justify your answers.

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Three possible combinations for buying hamburgers and chicken are:

• 3 pounds of hamburger and 7 pounds of chicken.

Justify:	$2(3) + 3(7) \le 30$	&	x≥3
	<mark>27 ≤ 30</mark> 🙂		<mark>3 ≥ 3</mark> 😳

 6 pounds of hamburger and 6 pounds of chicken.
Justify: 2(6) + 3(6) ≤ 30 & x ≥ 3

 $30 \le 30 \ \textcircled{0} \le 30 \ \textcircled{0} \times 23 \ \textcircled{0} \le 30 \ \textcircled{0}$

 10 pounds of hamburger and 3 pounds of chicken. Justify: 2(10) + 3(3) ≤ 30 & x ≥ 3
29 ≤ 30 ⁽¹⁾ 10≥ 3 ⁽¹⁾

Answers will vary. Any ordered pair within the purple shaded region is correct.

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3. Jenny is making jewelry for an Arts and Crafts show. She would like to make at least \$100 in sales. She estimates that she will sell at most 50 pieces of jewelry. The bracelets that she is selling cost \$2 and the necklaces cost \$3.

- Write a system of inequalities to represent this situation.
- Graph each inequality on the grid below.
- Give two possible combinations of bracelets and necklaces that can be sold in order for Jenny to meet her goal. Justify your answer.





Two possible combinations of bracelet and necklace sales are:

•	20 brac	elets and 25 r	necklad	es.	
	Justify:	2(20) + 3(25)	≥ 100	&	20+ 25 ≤ 50
		115 ≥ 100	\odot	&	45 ≤ 50☺

30 bracelets and 15 necklaces. Justify: $2(30) + 3(15) \ge 100$ & $30+15 \le 50$

105 > 100 🙂

Answers will vary. Any ordered pair within the purple shaded region is correct.

 $45 \leq 50^{\circ}$



4. Jason is buying wings and hot dogs for a party. One package of wings costs \$7. Hot dogs cost \$5 per package. He must spend no more than \$40.

- Write an inequality to represent the cost of Jason's food for the party.
- Jason knows that he will be buying at least 5 packages of hot dogs. Write an inequality to represent this situation.
- Graph both inequalities. Give two options for Jason when buying wings and hot dogs.





Jason doesn't have a whole lot of options for buying wings and hot dogs. Notice that the purple shaded region is very small.

Two options for buying wings and hot dogs are:

(1,5) 1 package of wings	and 5 packages of
hot dogs.	
7(1) + 5(5) ≤ 40	y≥ 5
32≤40 ☺	<mark>5≥5</mark> 🙂
(2,5) 2 packages of wing hot dogs.	s and 5 packages of

7(2) +5(5) ≤ 40	y≥ 5
39 ≤ 40 ☺	5 ≥5 ☺

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A Dinner Theatre actress is paid \$250 per day to rehearse the play and \$500 per day to perform in front of an audience. In one season, an actress earned between \$2000 and \$5000.

• Write a system of inequalities that represents this situation. (2 points)

Let x = the number of days the actress rehearses Let y = the number of days the actress performs

We know that she earned between 2000 and 5000. This means greater than 2000 and less than 5000. So, we will write two equations based on this information.

250x+500y > 2000

250x + 500y < 5000

This is our system of equations.

• Graph the system of inequalities on the grid. (2 points)







• Identify two different ways the actress may have earned her salary. Justify your answers. (2 points)

The actress may have earned her salary by rehearsing for 6 days and performing for 6 days. (6,6)				
Justification:				
250x + 500y > 2000	250x +500y < 5000			
250(6) + 500(6) > 2000	250(6)+500(6) <5000			
4500>2000	4500<5000			
The actress may have rehearsed for 10 days and p	performed for 4 days. (10,4)			
250x + 500y > 2000	250x +500y < 5000			
250(4) + 500(4) > 2000	250(4)+500(4) <5000			
3000>2000	3000<5000			