

Mathematics Assessment Project
CLASSROOM CHALLENGES
A Formative Assessment Lesson

Interpreting Distance-Time Graphs

Mathematics Assessment Resource Service
University of Nottingham & UC Berkeley
Beta Version

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Interpreting Distance–Time Graphs

MATHEMATICAL GOALS

This lesson unit is intended to help you assess how well students are able to interpret distance–time graphs and, in particular, to help you identify students who:

- Interpret distance–time graphs as if they are pictures of situations rather than abstract representations of them.
- Have difficulty relating speeds to slopes of these graphs.

COMMON CORE STATE STANDARDS

This lesson relates to the following *Standards for Mathematical Content* in the *Common Core State Standards for Mathematics*:

- 8.F Construct a function to model a linear relationship between two quantities. Describe qualitatively the functional relationship between two quantities by analyzing a graph

This lesson also relates to the following *Standards for Mathematical Practice* in the *Common Core State Standards for Mathematics*:

2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.

INTRODUCTION

The lesson unit is structured in the following way:

- Before the lesson, students work on a task designed to reveal their current understandings and difficulties. You review their work and create questions for students to answer in order to improve their solutions.
- A whole-class introduction provides students with guidance on how to work through the first task. Students then work in small groups on a collaborative discussion task, matching verbal interpretations with graphs. As they do this, they translate between words and graphical features, and begin to link the representations.
- This is followed by a whole-class discussion about applying realistic data to a graph.
- Students next work in small groups, matching tables of data to the existing matched pairs of cards. They then explain their reasoning to another group of students.
- In a final whole-class discussion, students draw their own graphs from verbal interpretations.
- Finally, students return to their original task and try to improve their individual responses.

MATERIALS REQUIRED

- Each student will need two copies of the assessment task *Journey to the Bus Stop*, a mini-whiteboard, a pen, and an eraser.
- Each small group of students will need copies of *Card Set A: Distance–Time Graphs*, *Card Set B: Interpretations*, *Card Set C: Tables of Data*, a large sheet of paper, and a glue stick for making posters. The cards should be cut up beforehand.
- You will also need a supply of graph paper to give to students who request it. There are some projector resources to support your teaching.

TIME NEEDED

15 minutes before the lesson, a 90-minute lesson (or two 45-minute lessons), and 10 minutes in a following lesson (or homework). Timings are approximate and will depend on the needs of the class.

BEFORE THE LESSON

Assessment task: *Journey to the Bus Stop* (15 minutes)

Set this task, in class or for homework, a few days before the formative assessment lesson. This will give you an opportunity to assess the work, and to find out the kinds of difficulties students have with it. You will then be able to target your help more effectively in the follow-up lesson.

Give each student a copy of *Journey to the Bus Stop*.

Briefly introduce the task and help the class to understand the problem and its context.

Read through the task and try to answer it as carefully as you can.

It is important that, as far as possible, students are allowed to answer the questions without your assistance.

Students should not worry too much if they cannot understand or do everything because in the next lesson they will engage in a similar task that should help them. Explain to students that by the end of the next lesson, they should expect to answer questions such as these confidently. This is their goal.

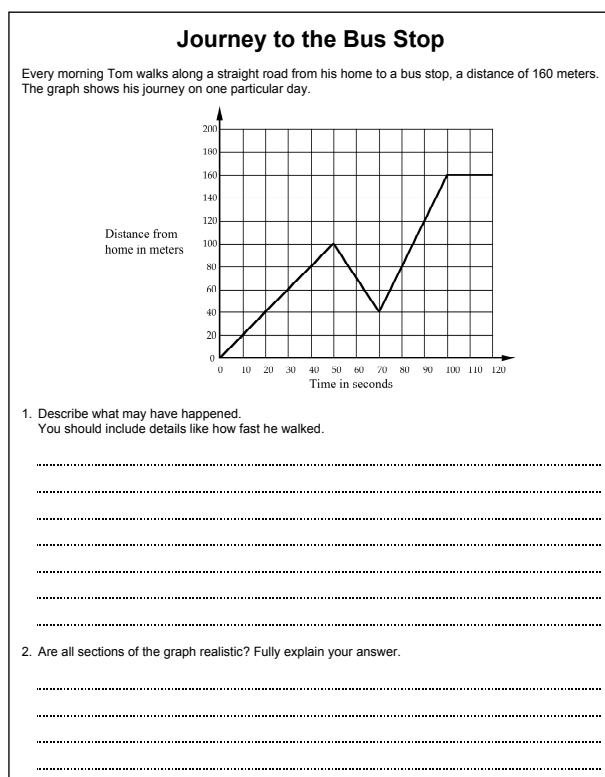
Assessing students' responses

Collect students' responses to the task. Make some notes on what their work reveals about their current levels of understanding and their different problem solving approaches.

We suggest that you do not score students' work. The research shows that this will be counterproductive, as it will encourage students to compare their scores and will distract their attention from what they can do to improve their mathematics.

Instead, help students to make further progress by summarizing their difficulties as a series of questions. Some suggestions for these are given on the next page. These have been drawn from common difficulties observed in trials of this unit.

We suggest that you write a list of your own questions, based on your students' work, using the ideas that follow. You may choose to write questions on each student's work. If you do not have time to do this, select a few questions that will be of help to the majority of students. These can be written on the board at the end of the lesson.



Common issues:**Suggested questions and prompts:**

<p>Student interprets the graph as a picture</p> <p>For example: The student assumes that as the graph goes up and down, Tom’s path is going up and down.</p> <p>Or: The student assumes that a straight line on a graph means that the motion is along a straight path.</p> <p>Or: The student thinks the negative slope means Tom has taken a detour.</p>	<ul style="list-style-type: none"> • If a person walked in a circle around their home, what would the graph look like? • If a person walked at a steady speed up and down a hill, directly away from home, what would the graph look like? • In each section of his journey, is Tom’s speed steady or is it changing? How do you know? • How can you figure out Tom’s speed in each section of the journey?
<p>Student interprets graph as speed–time</p> <p>The student has interpreted a positive slope as speeding up and a negative slope as slowing down.</p>	<ul style="list-style-type: none"> • If a person walked for a mile at a steady speed, away from home, then turned round and walked back home at the same steady speed, what would the graph look like? • How does the distance change during the second section of Tom’s journey? What does this mean? • How does the distance change during the last section of Tom’s journey? What does this mean? • How can you tell if Tom is traveling away from or towards home?
<p>Student fails to mention distance or time</p> <p>For example: The student has not mentioned how far away from home Tom has traveled at the end of each section.</p> <p>Or: The student has not mentioned the time for each section of the journey.</p>	<ul style="list-style-type: none"> • Can you provide more information about how far Tom has traveled during different sections of his journey? • Can you provide more information about how much time Tom takes during different sections of his journey?
<p>Student fails to calculate and represent speed</p> <p>For example: The student has not worked out the speed of some/all sections of the journey.</p> <p>Or: The student has written the speed for a section as the distance covered in the time taken, such as “20 meters in 10 seconds.”</p>	<ul style="list-style-type: none"> • Can you provide information about Tom’s speed for all sections of his journey? • Can you write his speed as meters per second?
<p>Student misinterprets the scale</p> <p>For example: When working out the distance the student has incorrectly interpreted the vertical scale as going up in 10s rather than 20s.</p>	<ul style="list-style-type: none"> • What is the scale on the vertical axis?
<p>Student adds little explanation as to why the graph is or is not realistic</p>	<ul style="list-style-type: none"> • What is the total distance Tom covers? Is this realistic for the time taken? Why?/Why not? • Is Tom’s fastest speed realistic? Is Tom’s slowest speed realistic? Why?/Why not?

SUGGESTED LESSON OUTLINE

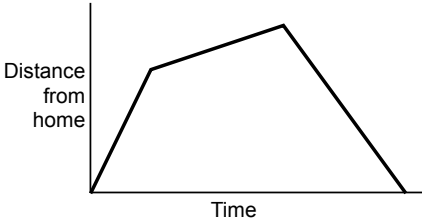
If you have a short lesson or you find the lesson is progressing at a slower pace than anticipated, we suggest you break the lesson after the first sharing of posters and continue it at a later time.

Whole-class introduction: interpreting and sketching graphs (10 minutes)

Throughout this activity, encourage students to articulate their reasoning, justify their choices mathematically, and question the choices put forward by others. This introduction will provide students with a model of how they should work with their partners in the first small-group activity.

Show the class the projector resource *Matching a Graph to a Story*:

Matching a Graph to a Story

<p>A. Tom took his dog for a walk to the park. He set off slowly and then increased his pace. At the park Tom turned around and walked slowly back home.</p>	
<p>B. Tom rode his bike east from his home up a steep hill. After a while the slope eased off. At the top he raced down the other side.</p>	
<p>C. Tom went for a jog. At the end of his road he bumped into a friend and his pace slowed. When Tom left his friend he walked quickly back home.</p>	

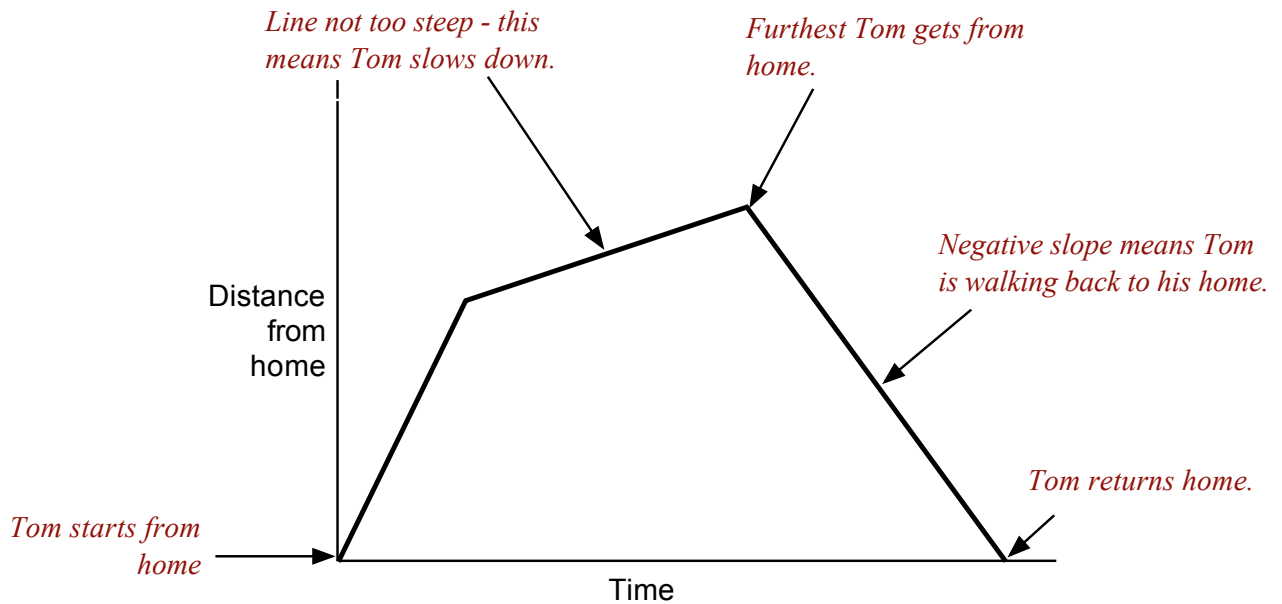
Ask students to match the correct story to the graph. They are to write down at least two reasons to support their decision.

After two or three minutes ask students who selected option A to raise their hands. Ask one or two to justify their choice. You may wish to use some of the questions on the sheet *Suggested questions and prompts* to encourage students to justify their choices and others to challenge their reasoning.

Repeat this with options B and C. Even if explanations are incorrect or only partially correct, write them next to the appropriate section of the graph. Encourage students to challenge these interpretations.

Slide P-2 of the projector resource allows you to write three different student explanations on the board at the same time.

A graph may end up looking like this:



This is how students should annotate their graphs when working on the collaborative task.

Collaborative activity: matching Card sets A and B (20 minutes)

Ask students to work in small groups of two or three students.

Give each group the *Card Set A: Distance–Time Graphs*, and *Card Set B: Interpretations* together with a large sheet of paper, and a glue stick for making a poster.

You are now going to continue exploring matching graphs with a story, but as a group.

You will be given ten graph cards and ten story cards.

In your group take a graph and find a story that matches it. Alternatively, you may want to take a story and find a graph that matches it.

Take turns at matching pairs of cards. Each time you do this, explain your thinking clearly and carefully. If you think there is no suitable card that matches, write one of your own.

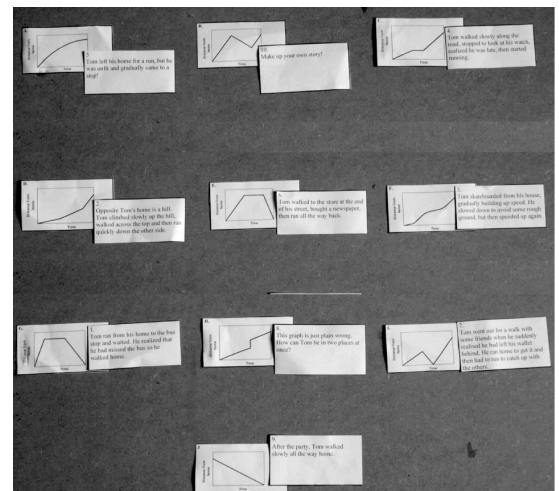
Place your cards side by side on your large sheet of paper, not on top of one another, so that everyone can see them.

Write your reasons for the match on the cards or the poster just as we did with the example in class. Give explanations for each line segment.

Make sure you leave plenty of space around the cards as, eventually, you will be adding another card to each matched pair.

The purpose of this structured group work is to encourage students to engage with each other's explanations and take responsibility for each other's understanding.

Slide P-3 of the projector resource summarizes these instructions.



You have two tasks during the small-group work: to make a note of student approaches to the task, and to support student reasoning.

Make a note of student approaches to the task

Listen and watch students carefully. Note different student approaches to the task and any common mistakes. For example, students may interpret the graph as a picture or students may read the graph from right to left. Also notice the ways students check to see if their match is correct and how they explain and justify a match to each other. You can use this information to focus a whole-class discussion.

Support student reasoning

Try not to make suggestions that move students towards a particular match. Instead, ask questions to help students to reason together. If you find one student has produced a solution for a particular match, challenge another student in the group to provide an explanation.

John matched these cards. Sharon, why do you think John matched these two cards?

If you find students have difficulty articulating their decisions, then use the sheet *Suggested questions and prompts* to support your own questioning of students.

In trials of this lesson some students had difficulty stating where home is on the graph.

For this graph, where does the journey start? Is that home?

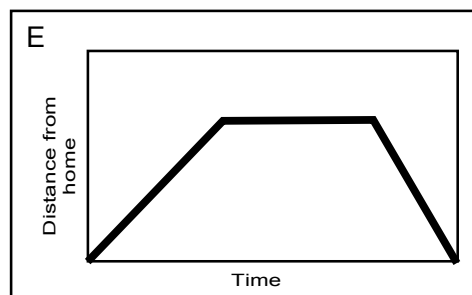
Give me a graph that shows a journey starting away from home.

For this graph, does the journey end at home? How do you know?

If the whole class is struggling on the same issue, you could write a couple of questions on the board and hold an interim, whole-class discussion. You could ask students who performed well in the assessment to help struggling students.

Some of the cards are deliberate distracters. For example, a student who matches Card 2 and E indicates that they think that graphs are pictures of the situation.

2 Opposite Tom's home is a hill. Tom climbed slowly up the hill, walked across the top, and then ran quickly down the other side.



Allow students time to match all the cards they can.

Sharing posters (5 minutes)

As students finish matching the cards, ask one student from each group to visit another group's poster.

You may want to use Slide P-4 of the projector resource to display the following instructions.

If you are staying at your desk, be ready to explain the reasons for your group's matches.

If you are visiting another group, write your card placements on a piece of paper. Go to another group's desk and check to see which matches are different from your own.

If there are differences, ask for an explanation. If you still don't agree, explain your own thinking.

When you return to your own desk, you need to consider as a group whether to make any changes to your own poster.

Students may now want to make changes to their poster. At this stage there is no need for students to glue the cards onto their posters as they may decide to make further changes.

If you need to extend the lesson over two days:

Once students have finished sharing posters, organize a whole-class discussion. Invite pairs of students to describe one pair of cards that they think they have matched correctly and the reasoning they employed. Encourage other students to challenge their explanations.

Finally, ask students to note their matches on the back of their poster and to use a paperclip to attach all cards to the poster.

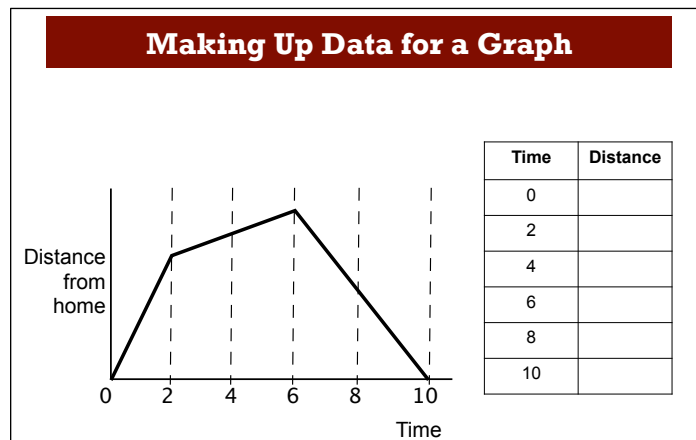
At the start of the second lesson, spend a few minutes reminding the class about the activity:

Can you remember what we were working on in the last lesson?

Return the posters to each group. The whole-class discussion on interpreting tables can serve as an introduction to the lesson.

Whole-class discussion: Interpreting tables (15 minutes)

Bring the class together and give each student a mini-whiteboard, a pen, and an eraser. Display Slide P-5 of the projector resource:



On your whiteboard, create a table that shows possible times and distances for Tom's journey.

After a few minutes, ask students to show you their whiteboards. Ask some students to explain how they created their tables. Write their figures on the board. Ask the rest of the class to check these figures.

Is Tom's speed slower or faster in this section compared to that section?

How do you know from the graph? From the table?

Is this speed constant? How can you tell? Do the figures in the table show a constant speed for this section of the journey?

What units might these be measured in?

Are these figures realistic?

Collaborative activity: matching Card Set C (20 minutes)

Hand out *Card Set C: Tables of Data* and ask students to match these cards with the cards already on their poster.

You are now going to match tables with the cards already on your desk. In your group take a graph and try to find a table that matches it, or take a table and find a graph that matches it.

Again take turns at matching cards you think belong together. Each time you do this, explain your thinking clearly and carefully.

Write your reasons for the match on the poster.

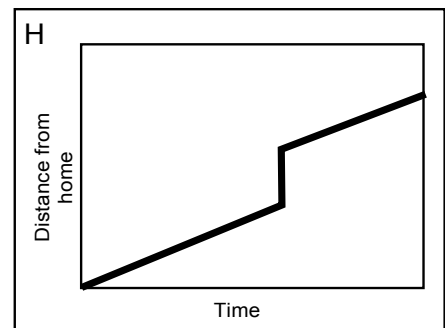
Students may also wish to suggest suitable units for the distances and times on the cards.

The tables should help students confirm or modify existing matches.

As they work on the matching, support the students as in the previous matching activity.

In the past, some students have had difficulty understanding the repetition in Table R. The table is intended to show the impossibility of Graph H.

R	Time	Distance
	0	0
	1	18
	2	36
	3	54
	3	84
	5	120

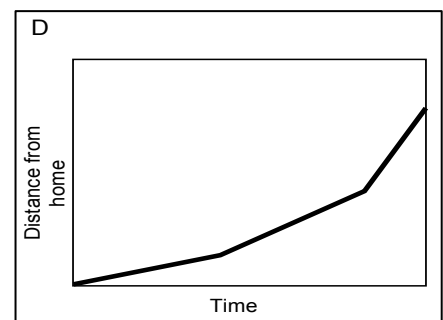


Some teachers have found that it helps students to look at the average speeds between consecutive times, by calculating differences. For example, average speeds for Table of Data Q would look like this.

Q	Time	Distance
	0	0
	1	10
	2	20
	3	40
	4	60
	5	120

Average speed
10
10
20
20
60

This may help students to understand that the table on Card Q matches Tom's hill walk, and that the correct distance-time graph should therefore be Card D.



If some students finish quickly, encourage them to devise their own pairs of cards.

Sharing posters (5 minutes)

When students have completed the task, the student who has not already visited another pair should share their work with another pair of students. Students are to share their reasoning as they did earlier in the lesson unit.

Students may now want to make final changes to their poster. When they are completely satisfied, ask them to glue their cards onto the large sheet of paper.

Whole-class discussion (10 minutes)

Using mini-whiteboards, make up some journeys and ask the class to show you the corresponding graphs.

On your whiteboards, draw a distance–time graph to show each of the following stories:

- *Sam ran out of his front door, then slipped and fell. He got up and walked the rest of the way to school.*
- *Sara walked from home up the steep hill opposite her house. She stopped at the top to put her skates on, then skated quickly down the hill, back home again.*
- *Chris cycled rapidly down the hill that starts at his house. He then slowed down as he climbed up the other side.*

Ask students to show their whiteboards to the whole-class. Select some to explain their graph to the class. Encourage others in the class to challenge their reasoning.

Improving individual solutions to the assessment task (10 minutes)

Return to the students their original assessment task *Journey to the Bus Stop*, as well as a second blank copy of the task.

Look at your original responses and think about what you have learned this lesson.

Using what you have learned, try to improve your work.

If you have not added questions to individual pieces of work then write your list of questions on the board. Students should select from this list only those questions they think are appropriate to their own work.

If you find you are running out of time, you could set this task in the next lesson or for homework.

SOLUTIONS

Assessment task: Journey to the Bus Stop

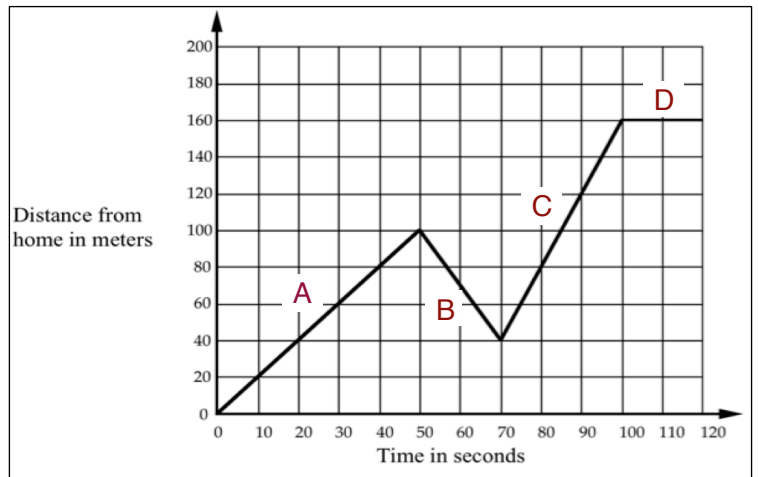
1. The graph shows Tom's journey is split into four sections. The straight lines indicate that Tom moves at a constant but different speed in each section.

A In this section of the journey Tom walks away from home at a speed of 2 meters per second ($100 \div 50$) for 50 seconds.

B The negative slope here means a change in direction. At 100 meters from home Tom starts to walk towards home. He walks for 60 meters at a speed of 3 meters per second ($60 \div 20$).

C At the start of this section Tom changes direction. He is now walking away from home at a fast pace. His speed is 4 meters per second ($120 \div 30$). He moves at this speed for 30 seconds and covers 120 meters.

D Here the slope is zero. This means at 160 meters from home Tom stops. It has taken him 100 seconds to get to this point.



2. The speeds provided in the answer to question 1 are realistic. A speed of 2 meters per second is a brisk walk. A speed of 4 meters per second means Tom is running.

Collaborative activity

Graph	Interpretation	Table	Graph	Interpretation	Table
A	5	W	B	10	S
C	4	V	D	2	Q
E	6	T	F	3	
G	1	P	H	8	R
I	7	U	J	9	X

A

W

Time	Distance
0	0
1	45
2	80
3	105
4	120
5	125

5 Tom left his home for a run, but he was unfit and gradually came to a stop!

B

S

Time	Distance
0	0
1	40
2	80
3	60
4	40
5	60

10 Make up your own story!

C

V

Time	Distance
0	0
1	20
2	40
3	40
4	80
5	120

4 Tom walked slowly along the road, stopped to look at his watch, realized he was late, and then started running.

D

Q

Time	Distance
0	0
1	10
2	20
3	40
4	60
5	120

2 Opposite Tom's home is a hill. Tom climbed slowly up the hill, walked across the top, and then ran quickly down the other side.

E

T

Time	Distance
0	0
1	20
2	40
3	40
4	40
5	0

6 Tom walked to the store at the end of his street, bought a newspaper, and then ran all the way back home.

F

Y

Time	Distance
0	0
1	1
2	2
3	3
4	4
5	5
6	6
7	7
8	8
9	9
10	10

3 Tom skateboarded from his house, gradually building speed. He slowed down on some rough ground, but then speeded up again.

G

P

Time	Distance
0	0
1	40
2	40
3	40
4	20
5	0

1 Tom ran from his home to the bus stop and waited. He realized he had missed the bus so he walked home.

H

R

Time	Distance
0	0
1	18
2	36
3	54
4	84
5	120

8 This graph is just plain wrong. How can Tom be in two places at once?

I

U

Time	Distance
0	0
1	30
2	60
3	0
4	60
5	120

7 Tom went out for a walk with his friends. He suddenly realized he had left his wallet behind. He ran home to get it and then had to run to catch up with the others.

J

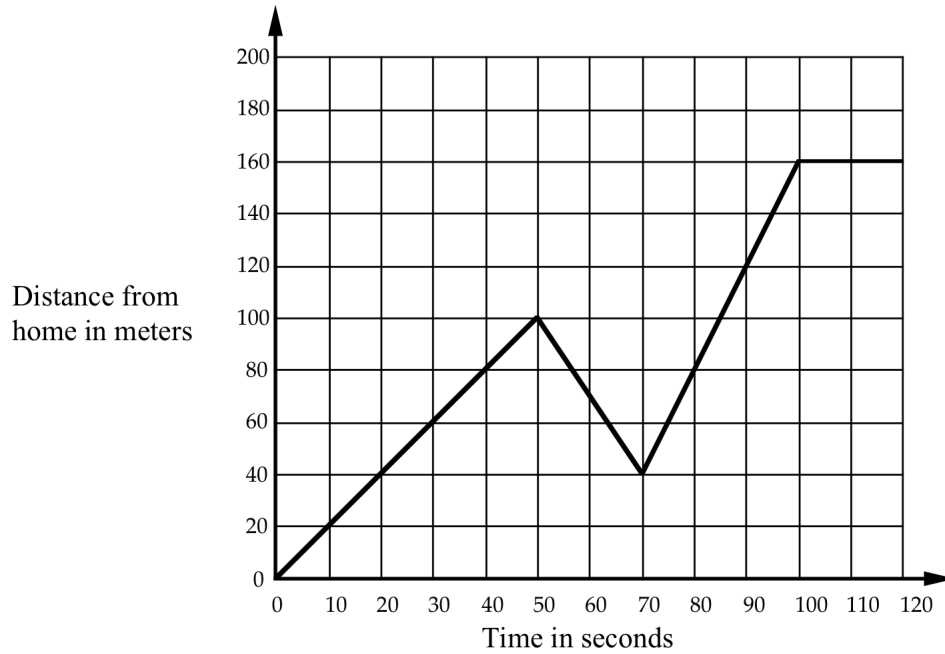
X

Time	Distance
0	120
1	96
2	72
3	48
4	24
5	0

9 After the party, Tom walked all the way home.

Journey to the Bus Stop

Every morning Tom walks along a straight road from his home to a bus stop, a distance of 160 meters. The graph shows his journey on one particular day.



1. Describe what may have happened. You should include details like how fast he walked.

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2. Are all sections of the graph realistic? Fully explain your answer.

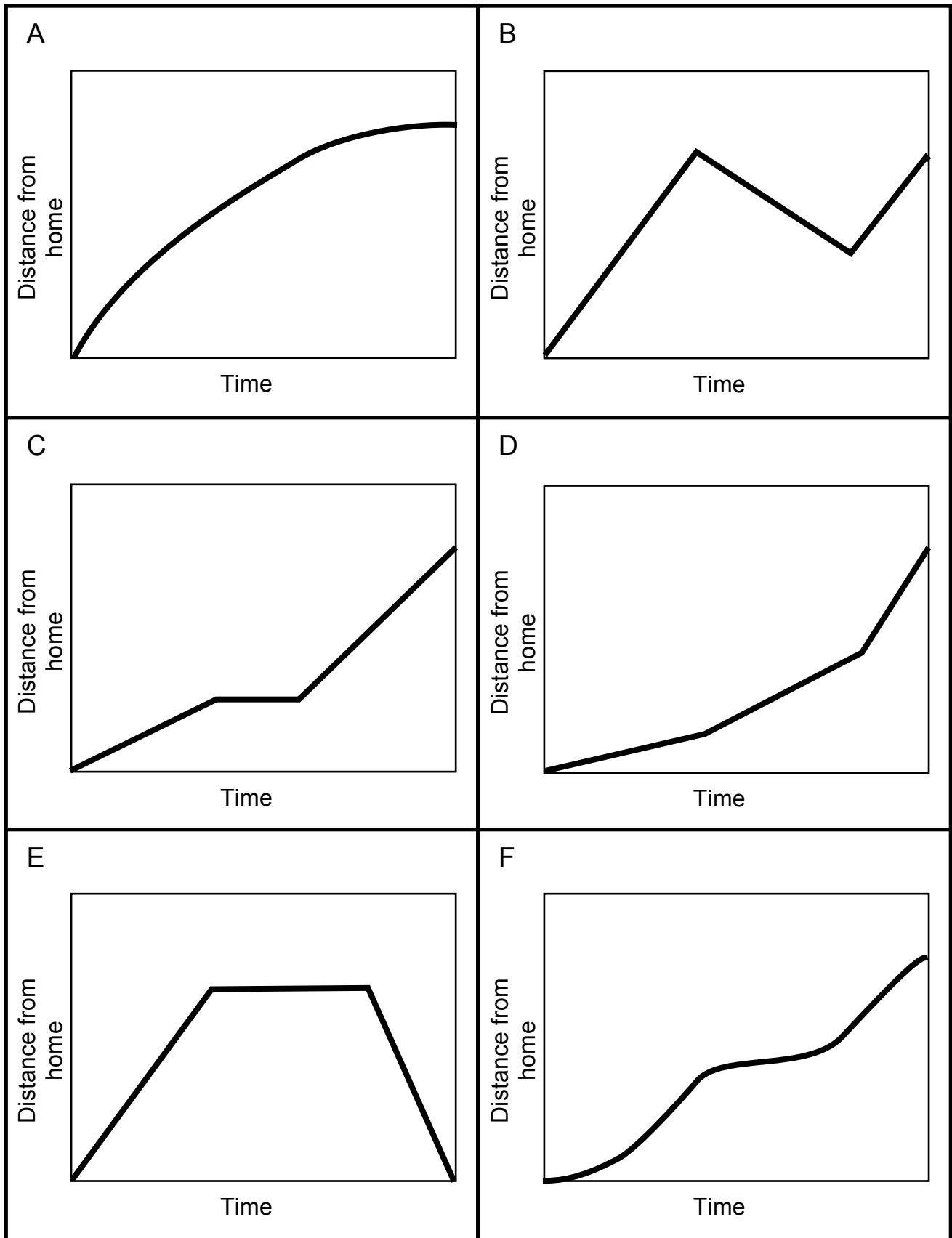
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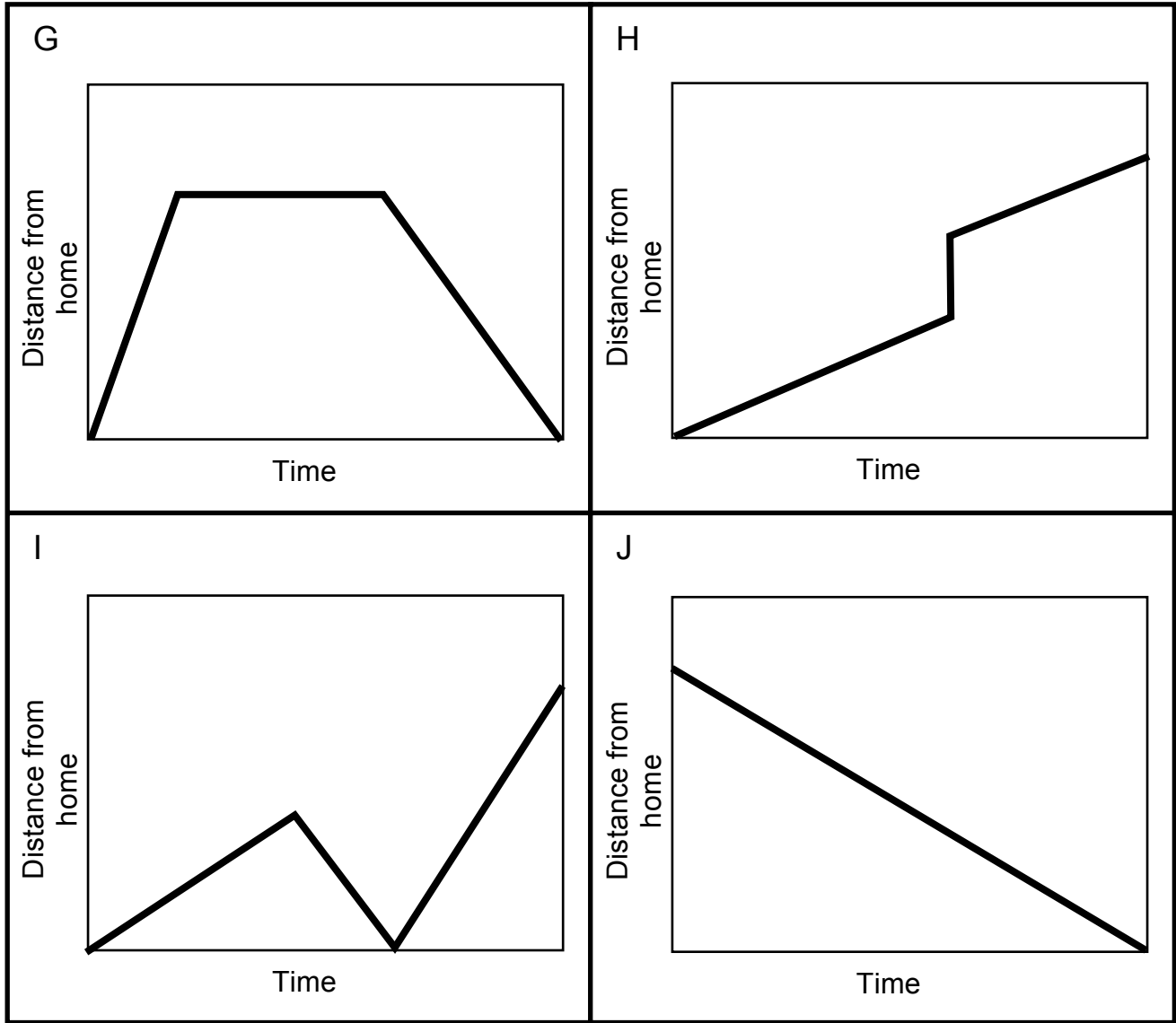
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Card Set A: Distance–Time Graphs



Card Set A: Distance–Time Graphs (continued)



Card Set B: Interpretations

<p>1 Tom ran from his home to the bus stop and waited. He realized that he had missed the bus so he walked home.</p>	<p>2 Opposite Tom's home is a hill. Tom climbed slowly up the hill, walked across the top, and then ran quickly down the other side.</p>
<p>3 Tom skateboarded from his house, gradually building up speed. He slowed down to avoid some rough ground, but then speeded up again.</p>	<p>4 Tom walked slowly along the road, stopped to look at his watch, realized he was late, and then started running.</p>
<p>5 Tom left his home for a run, but he was unfit and gradually came to a stop!</p>	<p>6 Tom walked to the store at the end of his street, bought a newspaper, and then ran all the way back.</p>
<p>7 Tom went out for a walk with some friends. He suddenly realized he had left his wallet behind. He ran home to get it and then had to run to catch up with the others.</p>	<p>8 This graph is just plain wrong. How can Tom be in two places at once?</p>
<p>9 After the party, Tom walked slowly all the way home.</p>	<p>10 Make up your own story!</p>

Card Set C: Tables of Data

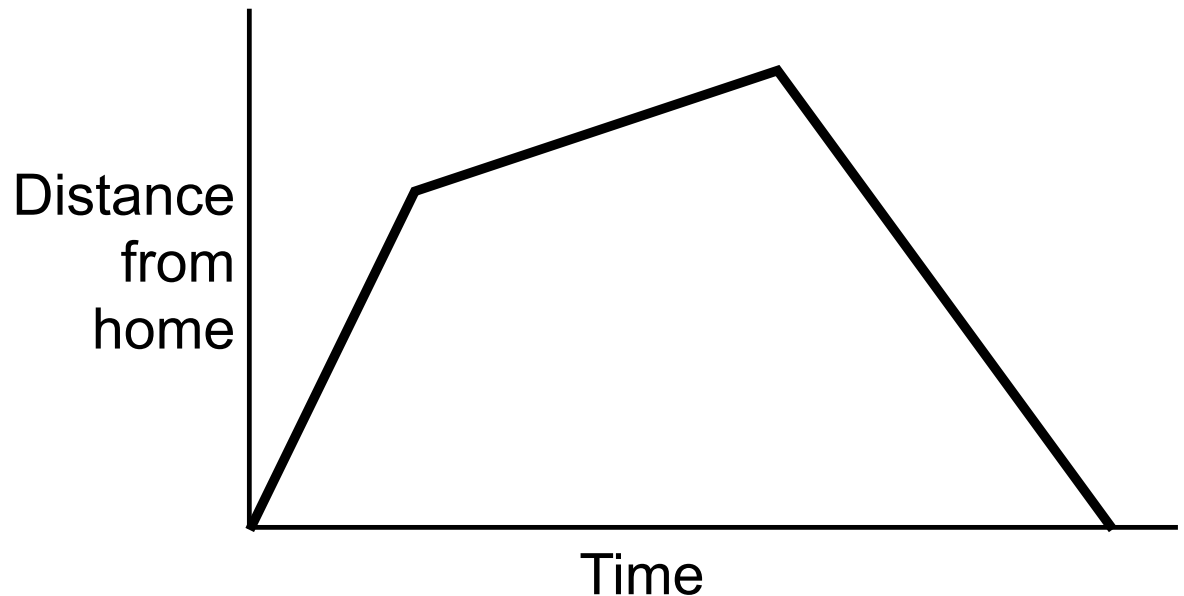
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Matching a Graph to a Story

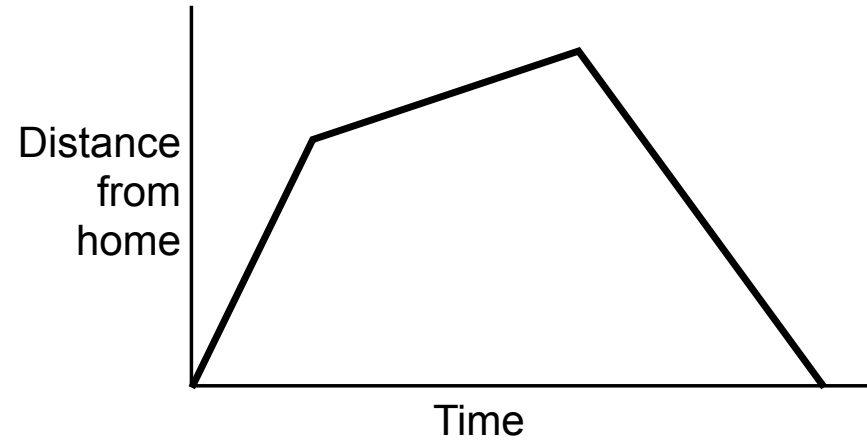
A. Tom took his dog for a walk to the park. He set off slowly and then increased his pace. At the park Tom turned around and walked slowly back home.

B. Tom rode his bike east from his home up a steep hill. After a while the slope eased off. At the top he raced down the other side.

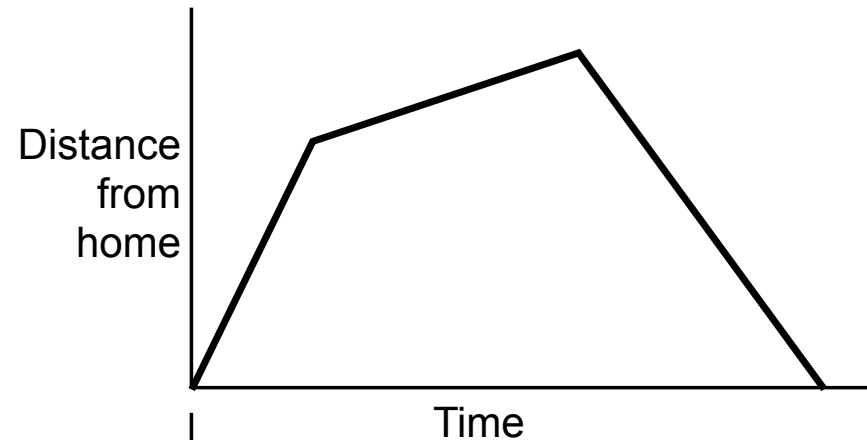
C. Tom went for a jog. At the end of his road he bumped into a friend and his pace slowed. When Tom left his friend he walked quickly back home.



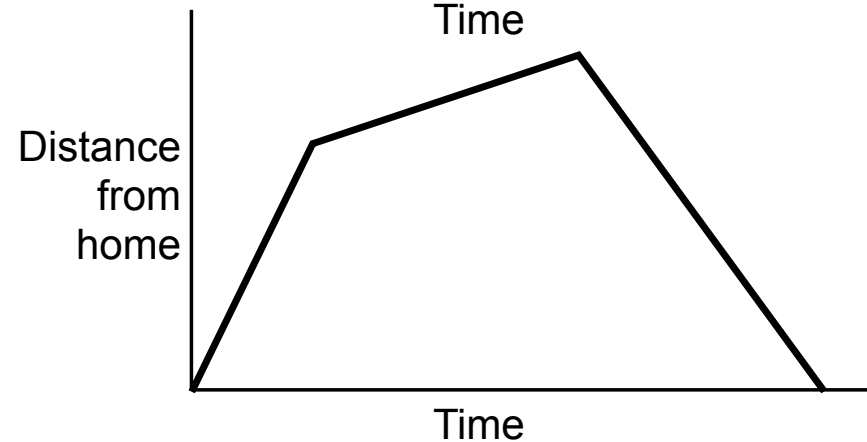
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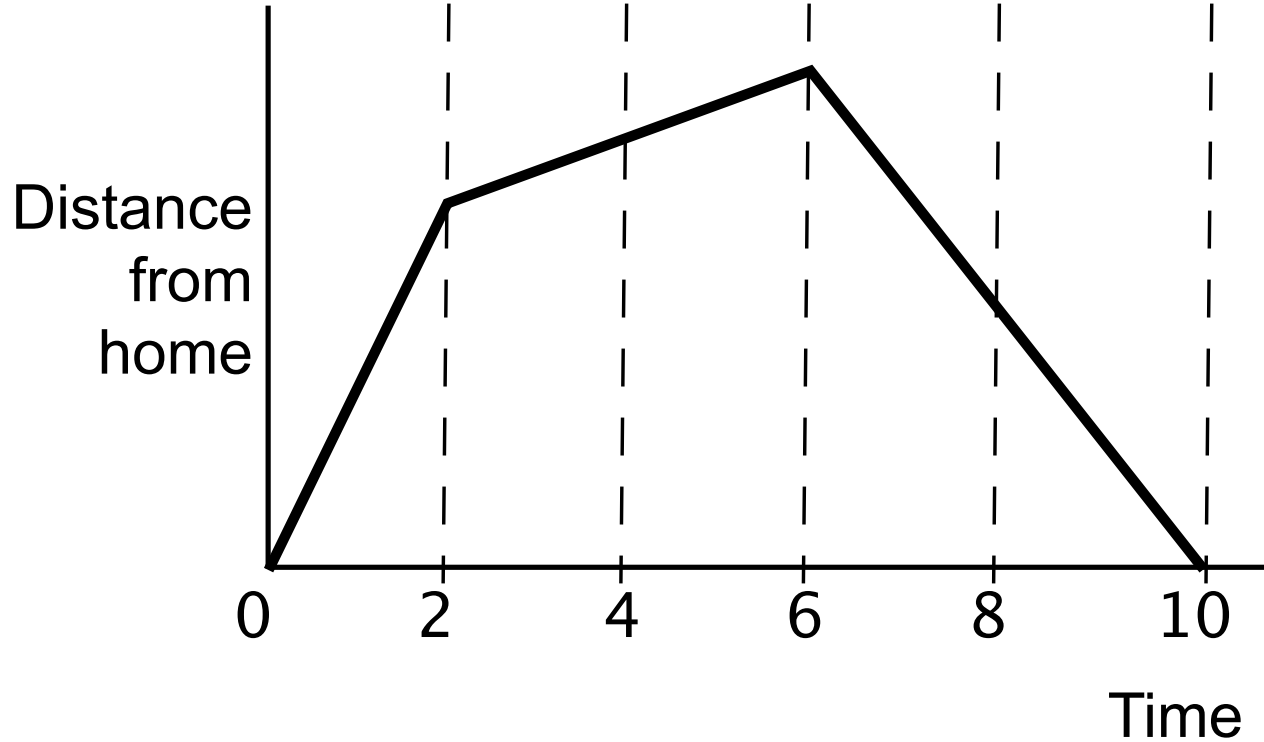
Matching Cards

- Take turns at matching pairs of cards. You may want to take a graph and find a story that matches it. Alternatively, you may prefer to take a story and find a graph that matches it.
- Each time you do this, explain your thinking clearly and carefully. If you think there is no suitable card that matches, write one of your own.
- Place your cards side by side on your large sheet of paper, not on top of one another, so that everyone can see them.
- Write your reasons for the match on the cards or the poster just as we did with the example in class. Give explanations for each line segment.
- Make sure you leave plenty of space around the cards as, eventually, you will be adding another card to each matched pair.

Sharing Work

- One student from each group is to visit another group's poster.
- If you are staying at your desk, be ready to explain the reasons for your group's matches.
- If you are visiting another group:
 - Write your card placements on a piece of paper.
 - Go to another group's desk and check to see which matches are different from your own.
 - If there are differences, ask for an explanation. If you still don't agree, explain your own thinking.
 - When you return to your own desk, you need to consider as a group whether to make any changes to your own poster.

Making Up Data for a Graph



Time	Distance
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2	
4	
6	
8	
10	

Mathematics Assessment Project
CLASSROOM CHALLENGES

This lesson was designed and developed by the
Shell Center Team
at the
University of Nottingham
Malcolm Swan, Nichola Clarke, Clare Dawson, Sheila Evans
with
Hugh Burkhardt, Rita Crust, Andy Noyes, and Daniel Pead

It was refined on the basis of reports from teams of observers led by
David Foster, Mary Bouck, and Diane Schaefer
based on their observation of trials in US classrooms
along with comments from teachers and other users.

This project was conceived and directed for
MARS: Mathematics Assessment Resource Service
by
Alan Schoenfeld, Hugh Burkhardt, Daniel Pead, and Malcolm Swan
and based at the University of California, Berkeley

We are grateful to the many teachers, in the UK and the US, who trialed earlier versions
of these materials in their classrooms, to their students, and to
Judith Mills, Carol Hill, and Alvaro Villanueva who contributed to the design.

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We are particularly grateful to
Carina Wong, Melissa Chabran, and Jamie McKee

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