

Lesson 3 Reteach

Equations in $y = mx$ Form

When the ratio of two variable quantities is constant, their relationship is called a **direct variation**.

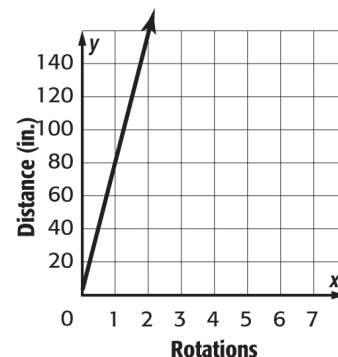
Example 1

The distance that a bicycle travels varies directly with the number of rotations that its tires make. Determine the distance that the bicycle travels for each rotation.

Since the graph of the data forms a line, the rate of change is constant. Use the graph to find the constant ratio.

$$\frac{\text{distance traveled}}{\text{\# of rotations}} \longrightarrow \frac{80}{1} \quad \frac{160}{2} \text{ OR } \frac{80}{1} \quad \frac{240}{3} \text{ OR } \frac{80}{1} \quad \frac{320}{4} \text{ OR } \frac{80}{1}$$

The bicycle travels 80 inches for each rotation of the tires.



Example 2

The number of trading cards varies directly as the number of packages. If there are 84 cards in 7 packages, how many cards are in 12 packages?

Let x = the number of packages and y = the total number of cards.

$$y = mx \quad \text{Direct variation equation}$$

$$84 = m(7) \quad y = 84, x = 7$$

$$12 = m \quad \text{Simplify.}$$

$$y = 12x \quad \text{Substitute for } m = 12.$$

Use the equation to find y when $x = 12$.

$$y = 12x$$

$$y = 12(12) \quad x = 12$$

$$y = 144 \quad \text{Multiply.}$$

There are 144 cards in 12 packages.

Exercises

Write an equation and solve the given situation.

1. **TICKETS** Four friends bought movie tickets for \$41. The next day seven friends bought movie tickets for \$71.75. What is the price of one ticket?

2. **JOBS** Barney earns \$24.75 in three hours. If the amount that he earns varies directly with the number of hours, how much would he earn in 20 hours?

Lesson 3 Skills Practice

Equations in $y = mx$ Form

For Exercises 1–3, determine whether each linear function is a direct variation. If so, state the constant of variation.

1.

Price, x	\$5	\$10	\$15	\$20
Tax, y	\$0.41	\$0.82	\$1.23	\$1.64

2.

Hours, x	11	12	13	14
Distance, y (miles)	154	167	180	193

3.

Age, x	8	9	10	11
Grade, y	3	4	5	6

For Exercises 4–12, y varies directly with x . Write an equation for the direct variation. Then find each value.

4. If $y = 8$ when $x = 3$, find y when $x = 45$.

5. If $y = -4$ when $x = 10$, find y when $x = 2$.

6. If $y = 27$ when $x = 8$, find y when $x = 11$.

7. Find y when $x = 12$, if $y = 2$ when $x = 5$.

8. Find y when $x = 3$, if $y = -4$ when $x = -9$.

9. Find y when $x = -6$, if $y = 15$ when $x = -5$.

10. If $y = 20$ when $x = 8$, what is the value of x when $y = -2$?

11. If $y = -30$ when $x = 15$, what is the value of x when $y = 60$?

12. If $y = 42$ when $x = 15$, what is the value of x when $y = 70$?

Lesson 4 Reteach

Slope-Intercept Form

Linear equations are often written in the form $y = mx + b$. This is called the **slope-intercept form**. When an equation is written in this form, m is the slope and b is the y -intercept.

Example 1

State the slope and the y -intercept of the graph of $y = x - 3$.

$$y = x - 3$$

Write the original equation.

$$y = 1x + (-3)$$

Write the equation in the form $y = mx + b$.

$$\begin{array}{c} \uparrow \quad \uparrow \\ y = mx + b \end{array}$$

$$m = 1, b = -3$$

The slope of the graph is 1, and the y -intercept is -3 .

You can use the slope intercept form of an equation to graph the equation.

Example 2

Graph $y = 2x + 1$ using the slope and y -intercept.

Step 1 Find the slope and y -intercept.

$$y = 2x + 1 \quad \text{slope} = 2, \text{ } y\text{-intercept} = 1$$

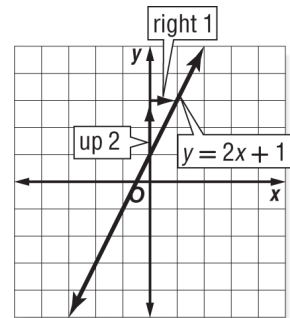
Step 2 Graph the y -intercept 1.

Step 3 Write the slope 2 as $\frac{2}{1}$. Use it to locate a second point on the line.

$$m = \frac{2}{1} \quad \leftarrow \text{change in } y : \text{ up 2 units}$$

$$\quad \quad \quad \leftarrow \text{change in } x : \text{ right 1 unit}$$

Step 4 Draw a line through the two points.



Exercises

State the slope and the y -intercept for the graph of each equation.

1. $y = x + 1$

2. $y = 2x - 4$

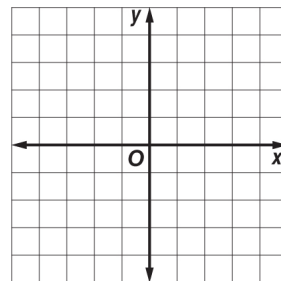
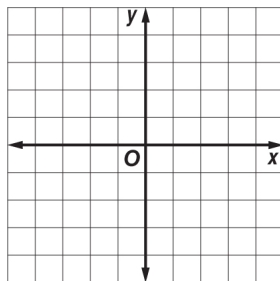
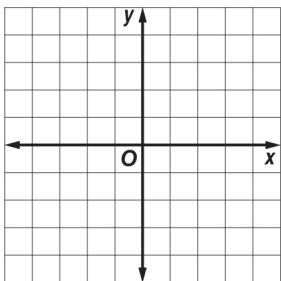
3. $y = \frac{1}{2}x - 1$

Graph each equation using the slope and the y -intercept.

4. $y = 2x + 2$

5. $y = x - 1$

6. $y = \frac{1}{2}x + 2$



Lesson 4 Skills Practice

Slope-Intercept Form

State the slope and the y -intercept for the graph of each equation.

1. $y = x + 4$

2. $y = 2x - 2$

3. $y = 3x - 1$

4. $y = -x + 3$

5. $y = \frac{1}{2}x - 5$

6. $y = -\frac{1}{3}x + 4$

7. $y - 2x = -1$

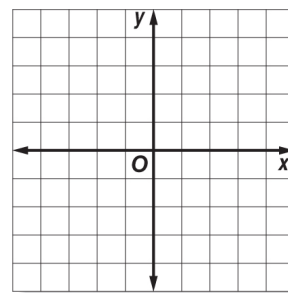
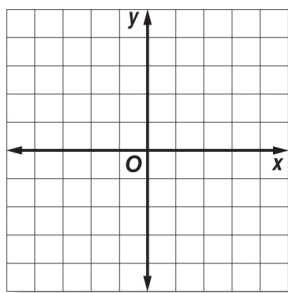
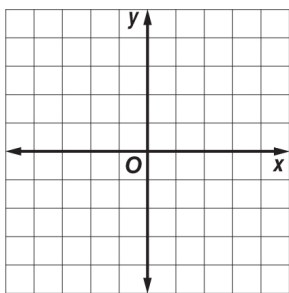
8. $y + 4x = 2$

9. $y = -\frac{3}{2}x - 3$

10. Graph a line with a slope of 1 and a y -intercept of -4 .

11. Graph a line with a slope of 2 and a y -intercept of -3 .

12. Graph a line with a slope of $\frac{1}{3}$ and a y -intercept of 1.

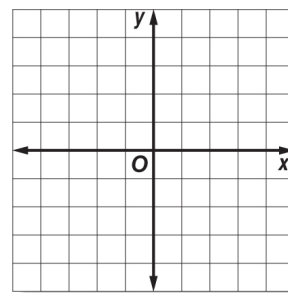
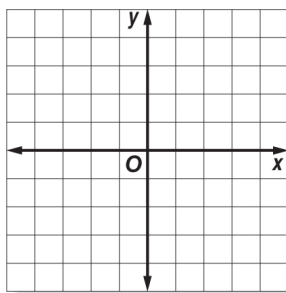
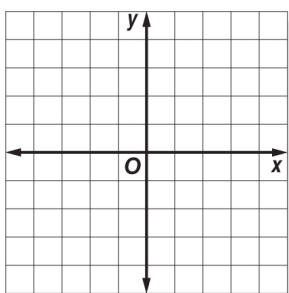


Graph each equation using the slope and the y -intercept.

13. $y = 3x - 3$

14. $y = -x + 1$

15. $y = \frac{1}{2}x - 2$



16. $y = 4x - 2$

17. $y = -\frac{3}{2}x + 1$

18. $y = \frac{2}{3}x - 3$

