

## Exercise 8.1

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**1. The angles of quadrilateral are in the ratio 3 : 5 : 9 : 13. Find all the angles of the quadrilateral.**

**Solution:**

Let the common ratio between the angles be = x.

We know that the sum of the interior angles of the quadrilateral =  $360^\circ$

Now,

$$3x + 5x + 9x + 13x = 360^\circ$$

$$\Rightarrow 30x = 360^\circ$$

$$\Rightarrow x = 12^\circ$$

$\therefore$ , Angles of the quadrilateral are:

$$3x = 3 \times 12^\circ = 36^\circ$$

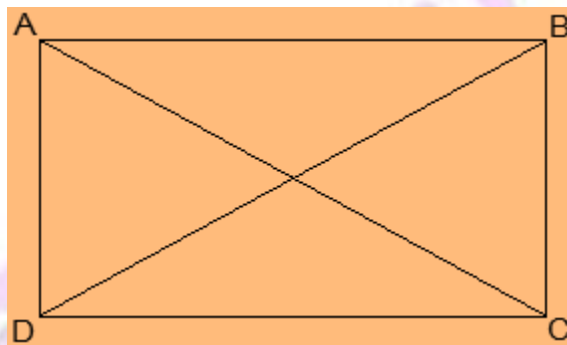
$$5x = 5 \times 12^\circ = 60^\circ$$

$$9x = 9 \times 12^\circ = 108^\circ$$

$$13x = 13 \times 12^\circ = 156^\circ$$

**2. If the diagonals of a parallelogram are equal, then show that it is a rectangle.**

**Solution:**



Given that,

$$AC = BD$$

To show that, ABCD is a rectangle if the diagonals of a parallelogram are equal

To show ABCD is a rectangle we have to prove that one of its interior angles is right angled.

**Proof,**

In  $\triangle ABC$  and  $\triangle BAD$ ,

$$AB = BA \text{ (Common)}$$

$$BC = AD \text{ (Opposite sides of a parallelogram are equal)}$$

$$AC = BD \text{ (Given)}$$

Therefore,  $\triangle ABC \cong \triangle BAD$

[SSS congruency]

$$\angle A = \angle B$$

[Corresponding parts of Congruent Triangles]

also,

$$\angle A + \angle B = 180^\circ \text{ (Sum of the angles on the same side of the transversal)}$$

$$\Rightarrow 2\angle A = 180^\circ$$

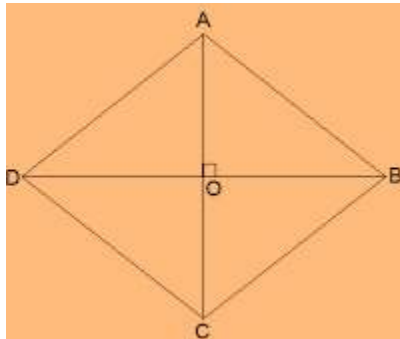
$$\Rightarrow \angle A = 90^\circ = \angle B$$

$\therefore$ , ABCD is a rectangle.

Hence Proved.

**3. Show that if the diagonals of a quadrilateral bisect each other at right angles, then it is a rhombus.**

**Solution:**



Let ABCD be a quadrilateral whose diagonals bisect each other at right angles.

Given that,

$$OA = OC$$

$$OB = OD$$

$$\text{and } \angle AOB = \angle BOC = \angle OCD = \angle ODA = 90^\circ$$

To show that,

if the diagonals of a quadrilateral bisect each other at right angles, then it is a rhombus.

i.e., we have to prove that ABCD is parallelogram and  $AB = BC = CD = AD$

**Proof,**

In  $\triangle AOB$  and  $\triangle COB$ ,

$$OA = OC \text{ (Given)}$$

$$\angle AOB = \angle COB \text{ (Opposite sides of a parallelogram are equal)}$$

$$OB = OB \text{ (Common)}$$

Therefore,  $\triangle AOB \cong \triangle COB$  [SAS congruency]

Thus,  $AB = BC$  [CPCT]

Similarly we can prove,

$$BC = CD$$

$$CD = AD$$

$$AD = AB$$

$$\therefore, AB = BC = CD = AD$$

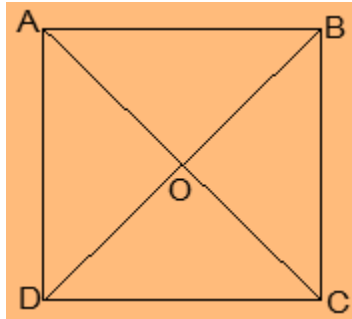
Opposites sides of a quadrilateral are equal hence ABCD is a parallelogram.

$\therefore$ , ABCD is rhombus as it is a parallelogram whose diagonals intersect at right angle.

Hence Proved.

**4. Show that the diagonals of a square are equal and bisect each other at right angles.**

**Solution:**



Let ABCD be a square and its diagonals AC and BD intersect each other at O.

To show that,

$$AC = BD$$

$$AO = OC$$

and  $\angle AOB = 90^\circ$

Proof,

In  $\triangle ABC$  and  $\triangle BAD$ ,

$$BC = BA \text{ (Common)}$$

$$\angle ABC = \angle BAD = 90^\circ$$

$$AC = AD \text{ (Given)}$$

$$\therefore \triangle ABC \cong \triangle BAD \quad [\text{SAS congruency}]$$

Thus,

$$AC = BD \quad [\text{CPCT}]$$

diagonals are equal.

Now,

In  $\triangle AOB$  and  $\triangle COD$ ,

$$\angle BAO = \angle DCO \text{ (Alternate interior angles)}$$

$$\angle AOB = \angle COD \text{ (Vertically opposite)}$$

$$AB = CD \text{ (Given)}$$

$$\therefore \triangle AOB \cong \triangle COD \quad [\text{AAS congruency}]$$

Thus,

$$AO = CO \quad [\text{CPCT}].$$

$\therefore$ , Diagonal bisect each other.

Now,

In  $\triangle AOB$  and  $\triangle COB$ ,

$$OB = OB \text{ (Given)}$$

$$AO = CO \text{ (diagonals are bisected)}$$

$$AB = CB \text{ (Sides of the square)}$$

$$\therefore \triangle AOB \cong \triangle COB \quad [\text{SSS congruency}]$$

also,  $\angle AOB = \angle COB$

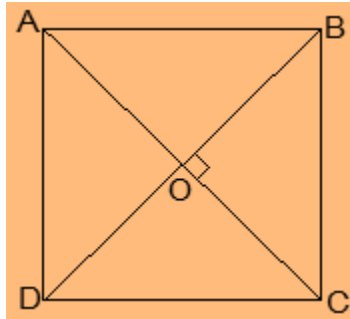
$$\angle AOB + \angle COB = 180^\circ \text{ (Linear pair)}$$

Thus,  $\angle AOB = \angle COB = 90^\circ$

$\therefore$ , Diagonals bisect each other at right angles

**5. Show that if the diagonals of a quadrilateral are equal and bisect each other at right angles, then it is a square.**

**Solution:**



Given that,

Let ABCD be a quadrilateral and its diagonals AC and BD bisect each other at right angle at O.

To prove that,

The Quadrilateral ABCD is a square.

Proof,

In  $\triangle AOB$  and  $\triangle COD$ ,

$AO = CO$  (Diagonals bisect each other)

$\angle AOB = \angle COD$  (Vertically opposite)

$OB = OD$  (Diagonals bisect each other)

$\therefore \triangle AOB \cong \triangle COD$  [SAS congruency]

Thus,

$AB = CD$  [CPCT] --- (i)

also,

$\angle OAB = \angle OCD$  (Alternate interior angles)

$\Rightarrow AB \parallel CD$

Now,

In  $\triangle AOD$  and  $\triangle COB$ ,

$AO = CO$  (Diagonals bisect each other)

$\angle AOD = \angle COB$  (Vertically opposite)

$OD = OB$  (Common)

$\therefore \triangle AOD \cong \triangle COB$  [SAS congruency]

Thus,

$AD = CB$  [CPCT] --- (ii)

also,

$AD = BC$  and  $AD = CD$

$\Rightarrow AD = BC = CD = AB$  --- (ii)

also,  $\angle ADC = \angle BCD$  [CPCT]

and  $\angle ADC + \angle BCD = 180^\circ$  (co-interior angles)

$\Rightarrow 2\angle ADC = 180^\circ$

$\Rightarrow \angle ADC = 90^\circ$  --- (iii)

One of the interior angles is right angle.

Thus, from (i), (ii) and (iii) given quadrilateral ABCD is a square.

Hence Proved.

**6. Diagonal AC of a parallelogram ABCD bisects  $\angle A$  (see Fig. 8.19). Show that**

**(i) it bisects  $\angle C$  also,**

**(ii) ABCD is a rhombus.**

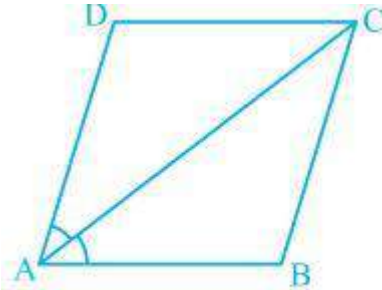


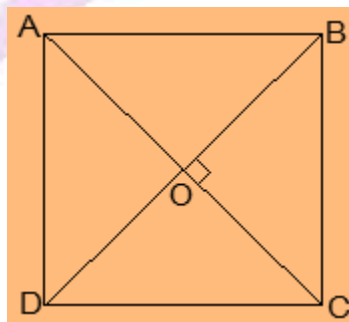
Fig. 8.19

Solution:

- (i) In  $\triangle ADC$  and  $\triangle CBA$ ,  
 $AD = CB$  (Opposite sides of a parallelogram)  
 $DC = BA$  (Opposite sides of a parallelogram)  
 $AC = CA$  (Common Side)  
 $\therefore \triangle ADC \cong \triangle CBA$  [SSS congruency]  
 Thus,  
 $\angle ACD = \angle CAB$  by CPCT  
 and  $\angle CAB = \angle CAD$  (Given)  
 $\Rightarrow \angle ACD = \angle BCA$   
 Thus,  
 $AC$  bisects  $\angle C$  also.
- (ii)  $\angle ACD = \angle CAD$  (Proved above)  
 $\Rightarrow AD = CD$  (Opposite sides of equal angles of a triangle are equal)  
 Also,  $AB = BC = CD = DA$  (Opposite sides of a parallelogram)  
 Thus,  
 $ABCD$  is a rhombus.

7.  $ABCD$  is a rhombus. Show that diagonal  $AC$  bisects  $\angle A$  as well as  $\angle C$  and diagonal  $BD$  bisects  $\angle B$  as well as  $\angle D$ .

Solution:



Given that,

$ABCD$  is a rhombus.  
 $AC$  and  $BD$  are its diagonals.

Proof,

$AD = CD$  (Sides of a rhombus)  
 $\angle DAC = \angle DCA$  (Angles opposite of equal sides of a triangle are equal.)

also,  $AB \parallel CD$

$\Rightarrow \angle DAC = \angle BCA$  (Alternate interior angles)

$$\Rightarrow \angle DCA = \angle BCA$$

$\therefore$ , AC bisects  $\angle C$ .

Similarly,

We can prove that diagonal AC bisects  $\angle A$ .

Following the same method,

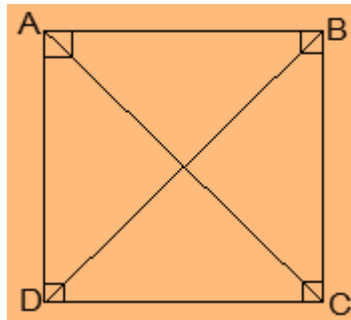
We can prove that the diagonal BD bisects  $\angle B$  and  $\angle D$ .

**8. ABCD is a rectangle in which diagonal AC bisects  $\angle A$  as well as  $\angle C$ . Show that:**

(i) ABCD is a square

(ii) Diagonal BD bisects  $\angle B$  as well as  $\angle D$ .

Solution:



- (i)  $\angle DAC = \angle DCA$  (AC bisects  $\angle A$  as well as  $\angle C$ )  
 $\Rightarrow AD = CD$  (Sides opposite to equal angles of a triangle are equal)  
 also,  $CD = AB$  (Opposite sides of a rectangle)  
 $\therefore AB = BC = CD = AD$   
 Thus, ABCD is a square.

- (ii) In  $\triangle BCD$ ,  
 $BC = CD$   
 $\Rightarrow \angle CDB = \angle CBD$  (Angles opposite to equal sides are equal)  
 also,  $\angle CDB = \angle ABD$  (Alternate interior angles)  
 $\Rightarrow \angle CBD = \angle ABD$   
 Thus, BD bisects  $\angle B$   
 Now,  
 $\angle CBD = \angle ADB$   
 $\Rightarrow \angle CDB = \angle ADB$   
 Thus, BD bisects  $\angle D$

**9. In parallelogram ABCD, two points P and Q are taken on diagonal BD such that  $DP = BQ$  (see Fig. 8.20). Show that:**

- (i)  $\triangle APD \cong \triangle CQB$   
 (ii)  $AP = CQ$   
 (iii)  $\triangle AQB \cong \triangle CPD$   
 (iv)  $AQ = CP$   
 (v) APCQ is a parallelogram

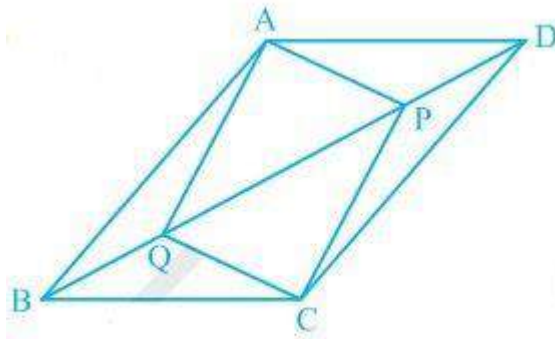


Fig. 8.20

Solution:

- (i) In  $\triangle APD$  and  $\triangle CQB$ ,  
 $DP = BQ$  (Given)  
 $\angle ADP = \angle CBQ$  (Alternate interior angles)  
 $AD = BC$  (Opposite sides of a parallelogram)  
 Thus,  $\triangle APD \cong \triangle CQB$  [SAS congruency]
- (ii)  $AP = CQ$  by CPCT as  $\triangle APD \cong \triangle CQB$ .
- (iii) In  $\triangle AQB$  and  $\triangle CPD$ ,  
 $BQ = DP$  (Given)  
 $\angle ABQ = \angle CDP$  (Alternate interior angles)  
 $AB = CD$  (Opposite sides of a parallelogram)  
 Thus,  $\triangle AQB \cong \triangle CPD$  [SAS congruency]
- (iv) As  $\triangle AQB \cong \triangle CPD$   
 $AQ = CP$  [CPCT]
- (v) From the questions (ii) and (iv), it is clear that APCQ has equal opposite sides and also has equal and opposite angles.  $\therefore$ , APCQ is a parallelogram.

**10. ABCD is a parallelogram and AP and CQ are perpendiculars from vertices A and C on diagonal BD (see Fig. 8.21). Show that**

- (i)  $\triangle APB \cong \triangle CQD$
- (ii)  $AP = CQ$

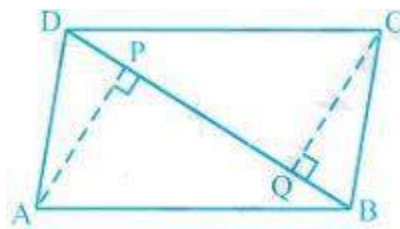


Fig. 8.21

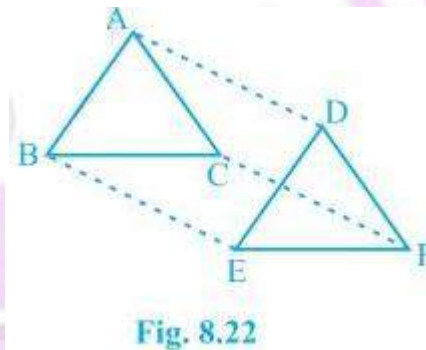
Solution:

- (i) In  $\triangle APB$  and  $\triangle CQD$ ,  
 $\angle ABP = \angle CDQ$  (Alternate interior angles)  
 $\angle APB = \angle CQD (= 90^\circ)$  as AP and CQ are perpendiculars  
 $AB = CD$  (ABCD is a parallelogram)  
 $\therefore \triangle APB \cong \triangle CQD$  [AAS congruency]
- (ii) As  $\triangle APB \cong \triangle CQD$ .  
 $\therefore AP = CQ$  [CPCT]

11. In  $\triangle ABC$  and  $\triangle DEF$ ,  $AB = DE$ ,  $AB \parallel DE$ ,  $BC = EF$  and  $BC \parallel EF$ . Vertices A, B and C are joined to vertices D, E and F respectively (see Fig. 8.22).

Show that

- (i) quadrilateral ABED is a parallelogram  
 (ii) quadrilateral BEFC is a parallelogram  
 (iii)  $AD \parallel CF$  and  $AD = CF$   
 (iv) quadrilateral ACFD is a parallelogram  
 (v)  $AC = DF$   
 (vi)  $\triangle ABC \cong \triangle DEF$ .



Solution:

- (i)  $AB = DE$  and  $AB \parallel DE$  (Given)  
 Two opposite sides of a quadrilateral are equal and parallel to each other.  
 Thus, quadrilateral ABED is a parallelogram
- (ii) Again  $BC = EF$  and  $BC \parallel EF$ .  
 Thus, quadrilateral BEFC is a parallelogram.
- (iii) Since ABED and BEFC are parallelograms.  
 $\Rightarrow AD = BE$  and  $BE = CF$  (Opposite sides of a parallelogram are equal)  
 $\therefore AD = CF$ .  
 Also,  $AD \parallel BE$  and  $BE \parallel CF$  (Opposite sides of a parallelogram are parallel)  
 $\therefore AD \parallel CF$
- (iv) AD and CF are opposite sides of quadrilateral ACFD which are equal and parallel to each other. Thus, it is a parallelogram.
- (v) Since ACFD is a parallelogram  
 $AC \parallel DF$  and  $AC = DF$
- (vi) In  $\triangle ABC$  and  $\triangle DEF$ ,



$$\begin{aligned} AB &= DE \text{ (Given)} \\ BC &= EF \text{ (Given)} \\ AC &= DF \text{ (Opposite sides of a parallelogram)} \\ \therefore, \Delta ABC &\cong \Delta DEF \quad \text{[SSS congruency]} \end{aligned}$$

12. ABCD is a trapezium in which  $AB \parallel CD$  and  $AD = BC$  (see Fig. 8.23). Show that

- (i)  $\angle A = \angle B$
- (ii)  $\angle C = \angle D$
- (iii)  $\Delta ABC \cong \Delta BAD$
- (iv) diagonal  $AC =$  diagonal  $BD$

[Hint : Extend AB and draw a line through C parallel to DA intersecting AB produced at E.]

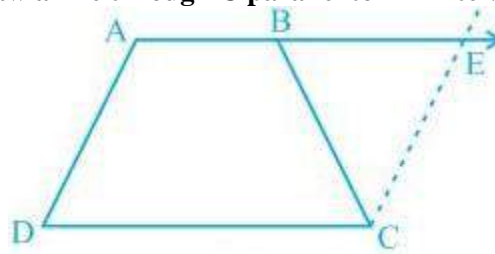


Fig. 8.23

**Solution:**

To Construct: Draw a line through C parallel to DA intersecting AB produced at E.

- (i)  $CE = AD$  (Opposite sides of a parallelogram)

$$AD = BC \text{ (Given)}$$

$$\therefore, BC = CE$$

$$\Rightarrow \angle CBE = \angle CEB$$

also,

$$\angle A + \angle CBE = 180^\circ \text{ (Angles on the same side of transversal and } \angle CBE = \angle CEB)$$

$$\angle B + \angle CBE = 180^\circ \text{ ( As Linear pair)}$$

$$\Rightarrow \angle A = \angle B$$

- (ii)  $\angle A + \angle D = \angle B + \angle C = 180^\circ$  (Angles on the same side of transversal)

$$\Rightarrow \angle A + \angle D = \angle A + \angle C \text{ (} \angle A = \angle B)$$

$$\Rightarrow \angle D = \angle C$$

- (iii) In  $\Delta ABC$  and  $\Delta BAD$ ,

$$AB = AB \text{ (Common)}$$

$$\angle DBA = \angle CBA$$

$$AD = BC \text{ (Given)}$$

$$\therefore, \Delta ABC \cong \Delta BAD \quad \text{[SAS congruency]}$$

- (iv) Diagonal  $AC =$  diagonal  $BD$  by CPCT as  $\Delta ABC \cong \Delta BAD$ .

Exercise 8.2

1. ABCD is a quadrilateral in which P, Q, R and S are mid-points of the sides AB, BC, CD and DA (see Fig 8.29). AC is a diagonal. Show that:

- (i)  $SR \parallel AC$  and  $SR = \frac{1}{2} AC$
- (ii)  $PQ = SR$
- (iii) PQRS is a parallelogram.

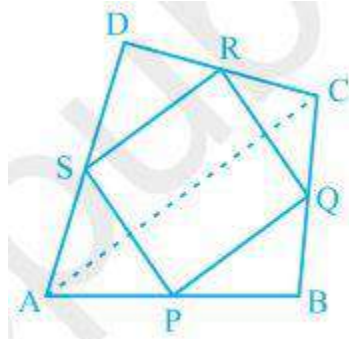


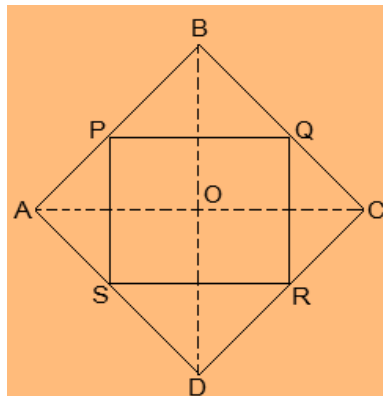
Fig. 8.29

Solution:

- (i) In  $\triangle DAC$ ,  
R is the mid point of DC and S is the mid point of DA.  
Thus by mid point theorem,  $SR \parallel AC$  and  $SR = \frac{1}{2} AC$
- (ii) In  $\triangle BAC$ ,  
P is the mid point of AB and Q is the mid point of BC.  
Thus by mid point theorem,  $PQ \parallel AC$  and  $PQ = \frac{1}{2} AC$   
also,  $SR = \frac{1}{2} AC$   
 $\therefore PQ = SR$
- (iii)  $SR \parallel AC$  ----- from question (i)  
and,  $PQ \parallel AC$  ----- from question (ii)  
 $\Rightarrow SR \parallel PQ$  - from (i) and (ii)  
also,  $PQ = SR$   
 $\therefore$  PQRS is a parallelogram.

2. ABCD is a rhombus and P, Q, R and S are the mid-points of the sides AB, BC, CD and DA respectively. Show that the quadrilateral PQRS is a rectangle.

Solution:



Given in the question,

ABCD is a rhombus and P, Q, R and S are the mid-points of the sides AB, BC, CD and DA respectively.

To Prove,

PQRS is a rectangle.

Construction,

Join AC and BD.

Proof:

In  $\triangle DRS$  and  $\triangle BPQ$ ,

$DS = BQ$  (Halves of the opposite sides of the rhombus)

$\angle SDR = \angle QBP$  (Opposite angles of the rhombus)

$DR = BP$  (Halves of the opposite sides of the rhombus)

$\therefore \triangle DRS \cong \triangle BPQ$  [SAS congruency]

$RS = PQ$  [CPCT]----- (i)

In  $\triangle QCR$  and  $\triangle SAP$ ,

$RC = PA$  (Halves of the opposite sides of the rhombus)

$\angle RCQ = \angle PAS$  (Opposite angles of the rhombus)

$CQ = AS$  (Halves of the opposite sides of the rhombus)

$\therefore \triangle QCR \cong \triangle SAP$  [SAS congruency]

$RQ = SP$  [CPCT]----- (ii)

Now,

In  $\triangle CDB$ ,

R and Q are the mid points of CD and BC respectively.

$\Rightarrow QR \parallel BD$

also,

P and S are the mid points of AD and AB respectively.

$\Rightarrow PS \parallel BD$

$\Rightarrow QR \parallel PS$

$\therefore$  PQRS is a parallelogram.

also,  $\angle PQR = 90^\circ$

Now,

In PQRS,

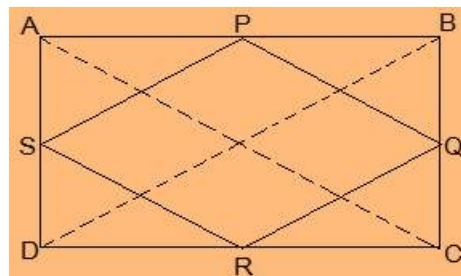
$RS = PQ$  and  $RQ = SP$  from (i) and (ii)

$\angle Q = 90^\circ$

$\therefore$  PQRS is a rectangle.

**3. ABCD is a rectangle and P, Q, R and S are mid-points of the sides AB, BC, CD and DA respectively. Show that the quadrilateral PQRS is a rhombus.**

Solution:



Given in the question,

ABCD is a rectangle and P, Q, R and S are mid-points of the sides AB, BC, CD and DA respectively.

Construction,

Join AC and BD.

To Prove,

PQRS is a rhombus.

Proof:

In  $\triangle ABC$

P and Q are the mid-points of AB and BC respectively

$\therefore$ ,  $PQ \parallel AC$  and  $PQ = \frac{1}{2} AC$  (Midpoint theorem) --- (i)

In  $\triangle ADC$ ,

$SR \parallel AC$  and  $SR = \frac{1}{2} AC$  (Midpoint theorem) --- (ii)

So,  $PQ \parallel SR$  and  $PQ = SR$

As in quadrilateral PQRS one pair of opposite sides is equal and parallel to each other, so, it is a parallelogram.

$\therefore$ ,  $PS \parallel QR$  and  $PS = QR$  (Opposite sides of parallelogram) --- (iii)

Now,

In  $\triangle BCD$ ,

Q and R are mid points of side BC and CD respectively.

$\therefore$ ,  $QR \parallel BD$  and  $QR = \frac{1}{2} BD$  (Midpoint theorem) --- (iv)

$AC = BD$  (Diagonals of a rectangle are equal) --- (v)

From equations (i), (ii), (iii), (iv) and (v),

$PQ = QR = SR = PS$

So, PQRS is a rhombus.

Hence Proved

4. ABCD is a trapezium in which  $AB \parallel DC$ , BD is a diagonal and E is the mid-point of AD. A line is drawn through E parallel to AB intersecting BC at F (see Fig. 8.30). Show that F is the mid-point of BC.

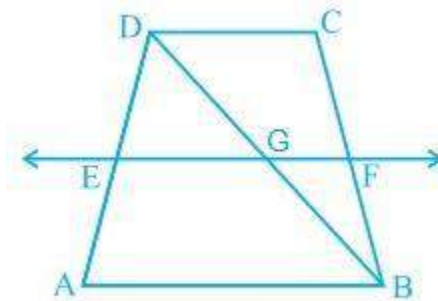


Fig. 8.30

Solution:

Given that,

ABCD is a trapezium in which  $AB \parallel DC$ , BD is a diagonal and E is the mid-point of AD.

To prove,

F is the mid-point of BC.

Proof,

BD intersected EF at G.

In  $\triangle BAD$ ,

E is the mid point of AD and also  $EG \parallel AB$ .

Thus, G is the mid point of BD (Converse of mid point theorem)

Now,

In  $\triangle BDC$ ,

G is the mid point of BD and also  $GF \parallel AB \parallel DC$ .

Thus, F is the mid point of BC (Converse of mid point theorem)

**5. In a parallelogram ABCD, E and F are the mid-points of sides AB and CD respectively (see Fig. 8.31). Show that the line segments AF and EC trisect the diagonal BD.**

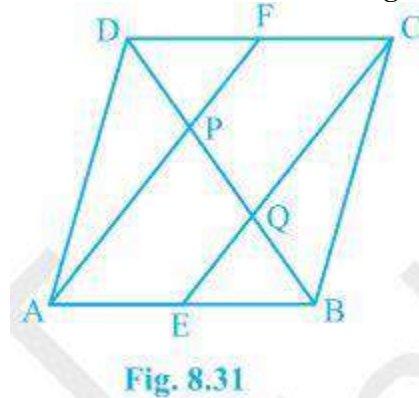


Fig. 8.31

**Solution:**

Given that,

ABCD is a parallelogram. E and F are the mid-points of sides AB and CD respectively.

To show,

AF and EC trisect the diagonal BD.

Proof,

ABCD is a parallelogram

$\therefore$ ,  $AB \parallel CD$

also,  $AE \parallel FC$

Now,

$AB = CD$  (Opposite sides of parallelogram ABCD)

$\Rightarrow \frac{1}{2} AB = \frac{1}{2} CD$

$\Rightarrow AE = FC$  (E and F are midpoints of side AB and CD)

AECF is a parallelogram (AE and CF are parallel and equal to each other)

$AF \parallel EC$  (Opposite sides of a parallelogram)

Now,

In  $\triangle DQC$ ,

F is mid point of side DC and  $FP \parallel CQ$  (as  $AF \parallel EC$ ).

P is the mid-point of DQ (Converse of mid-point theorem)

$\Rightarrow DP = PQ$  --- (i)

Similarly,

In  $\triangle APB$ ,

E is midpoint of side AB and  $EQ \parallel AP$  (as  $AF \parallel EC$ ).

Q is the mid-point of PB (Converse of mid-point theorem)

$\Rightarrow PQ = QB$  --- (ii)

From equations (i) and (ii),

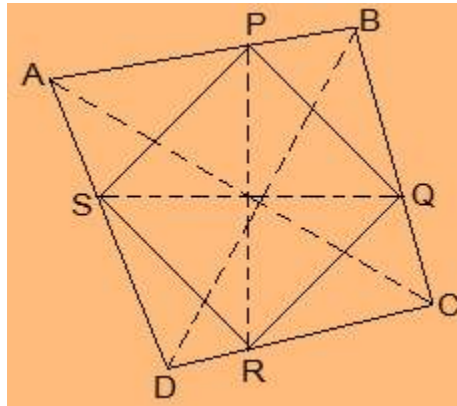
$DP = PQ = BQ$

Hence, the line segments AF and EC trisect the diagonal BD.

Hence Proved.

**6. Show that the line segments joining the mid-points of the opposite sides of a quadrilateral bisect each other.**

**Solution:**



Let ABCD be a quadrilateral and P, Q, R and S are the mid points of AB, BC, CD and DA respectively.

Now,

In  $\triangle ACD$ ,

R and S are the mid points of CD and DA respectively.

$\therefore SR \parallel AC$ .

Similarly we can show that,

$PQ \parallel AC$ ,

$PS \parallel BD$  and

$QR \parallel BD$

$\therefore$  PQRS is parallelogram.

PR and QS are the diagonals of the parallelogram PQRS. So, they will bisect each other.

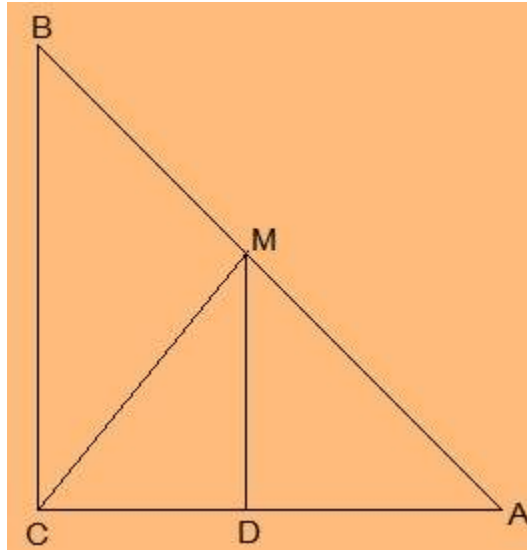
**7. ABC is a triangle right angled at C. A line through the mid-point M of hypotenuse AB and parallel to BC intersects AC at D. Show that**

**(i) D is the mid-point of AC**

**(ii)  $MD \perp AC$**

**(iii)  $CM = MA = \frac{1}{2} AB$**

**Solution:**



- (i) In  $\triangle ACB$ ,  
M is the midpoint of AB and  $MD \parallel BC$   
 $\therefore$  D is the midpoint of AC (Converse of mid point theorem)
- (ii)  $\angle ACB = \angle ADM$  (Corresponding angles)  
also,  $\angle ACB = 90^\circ$   
 $\therefore$ ,  $\angle ADM = 90^\circ$  and  $MD \perp AC$
- (iii) In  $\triangle AMD$  and  $\triangle CMD$ ,  
 $AD = CD$  (D is the midpoint of side AC)  
 $\angle ADM = \angle CDM$  (Each  $90^\circ$ )  
 $DM = DM$  (common)  
 $\therefore$ ,  $\triangle AMD \cong \triangle CMD$  [SAS congruency]  
 $AM = CM$  [CPCT]  
also,  $AM = \frac{1}{2} AB$  (M is midpoint of AB)  
Hence,  $CM = MA = \frac{1}{2} AB$