## XV. Mathematics, Grade 10

## Grade 10 Mathematics Test

The spring 2019 grade 10 Mathematics test was a next-generation assessment that was administered in two primary formats: a computer-based version and a paper-based version. The vast majority of students took the computer-based test. The paper-based test was offered as an accommodation for students with disabilities who are unable to use a computer, as well as for English learners who are new to the country and are unfamiliar with technology.

Most of the operational items on the grade 10 Mathematics test were the same, regardless of whether a student took the computerbased version or the paper-based version. In places where a technology-enhanced item was used on the computer-based test, an adapted version of the item was created for use on the paper test. These adapted paper items were multiple-choice, multiple-select, or short-answer items that tested the same Mathematics content and assessed the same standard as the technology-enhanced item.

This document displays released items from the paper-based test. Released items from the computer-based test are available on the MCAS Resource Center website at mcas.pearsonsupport.com/released-items.

## Test Sessions and Content Overview

The grade 10 Mathematics test was made up of two separate test sessions. Each session included selected-response, short-answer, and constructed-response questions. On the paper-based test, the selected-response questions were multiple-choice items and multiple-select items, in which students select the correct answer(s) from among several answer options.

## Standards and Reporting Categories

The grade 10 Mathematics test was based on high school standards in the Massachusetts Curriculum Framework for Mathematics (2017). The standards in the 2017 framework are organized under the five major conceptual categories listed below.

- Number and Quantity
- Algebra
- Functions
- Geometry
- Statistics and Probability

The grade 10 test assessed standards that overlap between the Model Algebra I/Model Geometry and Model Mathematics I/Model Mathematics II courses. The Massachusetts Curriculum Framework for Mathematics is available on the Department website at www.doe.mass.edu/frameworks/current.html.

Mathematics test results for grade 10 are reported under four MCAS reporting categories, which are based on the five framework conceptual categories listed above.

The table at the conclusion of this chapter provides the following information about each released operational item: reporting category, standard covered, item type, and item description. The correct answers for selected-response and short-answer questions are also displayed in the table.

## Reference Materials and Tools

Each student taking the grade 10 Mathematics test was provided with a grade 10 Mathematics Reference Sheet. A copy of the reference sheet follows the final question in this chapter.

During Session 2, each student had sole access to a calculator. Calculator use was not allowed during Session 1.
During both Mathematics test sessions, the use of bilingual word-to-word dictionaries was allowed for current and former English learner students only. No other reference tools or materials were allowed.

# Grade 10 Mathematics <br> SESSION 1 

This session contains 21 questions.

You may use your reference sheet during this session. You may not use a calculator during this session.

## Directions

Read each question carefully and then answer it as well as you can. You must record all answers in this Test \& Answer Booklet.

For some questions, you will mark your answers by filling in the circles in your Test \& Answer Booklet. Make sure you darken the circles completely. Do not make any marks outside of the circles. If you need to change an answer, be sure to erase your first answer completely.

For other questions, you will need to fill in an answer grid. Directions for completing questions with answer grids are provided on the next page.

If a question asks you to show or explain your work, you must do so to receive full credit. Write your response in the space provided in this Test \& Answer Booklet. Only responses written within the provided space will be scored.

## Directions for Completing Questions with Answer Grids

1. Work the question and find an answer.
2. Enter your answer in the answer boxes at the top of the answer grid.
3. Print only one number or symbol in each box. Do not leave a blank box in the middle of an answer.
4. Under each answer box, fill in the circle that matches the number or symbol you wrote above. Make a solid mark that completely fills the circle.
5. Do not fill in a circle under an unused answer box.
6. Fractions cannot be entered into an answer grid and will not be scored. Enter fractions as decimals.
7. If you need to change an answer, be sure to erase your first answer completely.
8. See below for examples of how to correctly complete an answer grid.

## EXAMPLES


(1) Which of the following is equivalent to this expression?

$$
-5 x\left(-6 x^{2}+1\right)
$$

(A) $30 x^{3}-4 x$
(B) $30 x^{3}-5 x$
(C) $-11 x^{3}-4 x$
(D) $-11 x^{3}-5 x$

2 Consider this function.

$$
f(x)=x(18-x)
$$

What are the values of $f(0), f(5)$, and $f(18)$ ?
(A) $f(0)=-18$
(B) $f(0)=0$
$f(5)=90$
$f(5)=90$
$f(18)=-36$
$f(18)=-324$
(C) $f(0)=0$
$f(5)=65$
$f(18)=0$
(D) $f(0)=18$
$f(5)=-450$
$f(18)=-36$

3 This diagram shows a circle with an inscribed right triangle and some of its measurements, in units.


Based on the diagram, what is the circumference, in units, of the circle?
(A) $5 \pi$
(B) $10 \pi$
(C) $14 \pi$
(D) $25 \pi$
4. On a coordinate plane, a single transformation will be performed on square RSTU.

Select three transformations of square RSTU that would result in a congruent figure.
(A) a translation 3 units up and 8 units to the right
(B) a rotation of $270^{\circ}$ counterclockwise about the origin
(C) a dilation by a scale factor of 1 with respect to the origin
(D) a dilation by a scale factor of 1.5 with respect to the origin
(E) a dilation by a scale factor of -2 with respect to the origin
(5) Consider this system of equations.

$$
\begin{aligned}
& h+c=2.25 \\
& h-c=1.75
\end{aligned}
$$

What value of $h$ makes the system of equations true?
Enter your answer in the answer boxes at the top of the answer grid and completely fill the matching circles.


6 Which of the following is equivalent to this expression?

$$
4 k^{4}+16 k^{3}+10 k^{2}
$$

(A) $4 k^{2}\left(k^{2}+4 k+2\right)$
(B) $2 k^{2}\left(2 k^{2}+8 k+5\right)$
(C) $2\left(2 k^{4}+14 k^{3}+8 k^{2}\right)$
(D) $2 k^{2}\left(2 k^{2}+16 k+10\right)$
(7) Consider this inequality.

$$
y \geq x-4
$$

Which of the following graphs represents the solution set of the inequality?
(A)

(B)

(C)

(D)


8 Line $w$ is represented by this equation.

$$
y=5 x+3
$$

Which of the following equations represents a line that is perpendicular to line $w$ ?
(A) $y=-\frac{1}{5} x+1$
(B) $y=-5 x+1$
(C) $y=\frac{1}{5} x+1$
(D) $y=5 x+1$

## This question has four parts. Be sure to label each part of your response.

9 A line and a parabola are graphed on a coordinate plane. The equation of the line and the equation of the parabola are shown in this table.

| Graph | Equation |
| :---: | :---: |
| Line | $y=-3 x+5$ |
| Parabola | $y=-x^{2}+2 x+1$ |

A. What is the value of $y$ for the line when $x=-4$ ? Show or explain how you got your answer.
B. What is the value of $y$ for the parabola when $x=-4$ ? Show or explain how you got your answer.
C. The line and the parabola intersect at two points. The distance, in units, between the two points is represented by this expression.

$$
\sqrt{(4-1)^{2}+(-7-2)^{2}}
$$

Simplify the expression to determine the distance, in units, between the two points. Show or explain how you got your answer.
D. The area, in square units, of the region on the coordinate plane enclosed by the parabola and the line is represented by this expression.

$$
-\frac{4^{3}}{3}+\frac{5(4)^{2}}{2}-4(4)-\left(-\frac{1^{3}}{3}+\frac{5(1)^{2}}{2}-4(1)\right)
$$

Simplify the expression to determine the area, in square units, of the enclosed region. Show or explain how you got your answer.

## 9

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10 A waiter recorded the amount of money he earned in tips each weekday for a two-week period. His data are shown in this table.

## Money Earned in Tips

| Week | Monday | Tuesday | Wednesday | Thursday | Friday |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\$ 25$ | $\$ 44$ | $\$ 48$ | $\$ 63$ | $\$ 75$ |
| 2 | $\$ 35$ | $\$ 35$ | $\$ 48$ | $\$ 62$ | $\$ 75$ |

Which statement about the data in the table is true?
(A) The median and the range for week 1 are equal to the median and the range for week 2 .
(B) The median and the mode for week 1 are equal to the median and the mode for week 2.
(C) The mean and the median for week 1 are equal to the mean and the median for week 2.
(D) The mean and the range for week 1 are equal to the mean and the range for week 2 .

11 Line segment $K L$ is shown on this coordinate plane.


What are the coordinates of the midpoint of line segment $K L$ ?
(A) $\left(-1, \frac{1}{2}\right)$
(B) $\left(-\frac{1}{2}, 1\right)$
(C) $\left(\frac{1}{2},-1\right)$
(D) $\left(1,-\frac{1}{2}\right)$

## This question has two parts.

12 Shayla and Carlos each have a bag that contains 5 green marbles, 5 red marbles, and 10 yellow marbles. The marbles are all the same size and shape.

## Part A

Shayla will select two marbles from her bag at random. She will not return the first marble to the bag before selecting the second marble.

Which expression represents the probability that Shayla will select two red marbles?
(A) $\frac{5}{20} \cdot \frac{4}{19}$
(B) $\frac{5}{20} \cdot \frac{4}{20}$
(C) $\frac{5}{20} \cdot \frac{5}{19}$
(D) $\frac{5}{20} \cdot \frac{5}{20}$

## Part B

Carlos will select two marbles from his bag at random. He will not return the first marble to the bag before selecting the second marble.

The first marble Carlos selects will not be yellow. What is the probability that the second marble he selects will be yellow?
(A) $\frac{9}{20}$
(B) $\frac{9}{19}$
(C) $\frac{10}{20}$
(D) $\frac{10}{19}$

13 What are the solutions of this equation?

$$
x^{2}+7 x+12=0
$$

(A) $x=-3 ; x=-4$
(B) $x=-2 ; x=-6$
(C) $x=2 ; x=6$
(D) $x=3 ; x=4$

## This question has four parts. Be sure to label each part of your response.

14 This double bar graph shows the amounts of time, in minutes, an athlete spent on aerobic training and strength training each day for 5 days.

Aerobic and Strength Training


Day of the Week

| $\square$ |
| :--- |
| Aerobic training |
| $\square$ |

A. On what day did the athlete spend the longest total amount of time training? Show or explain how you got your answer.
B. What is the median total number of minutes the athlete spent training each day? Show or explain how you got your answer.
C. What percent of the total number of minutes the athlete spent training for the 5 days was spent on strength training? Show or explain how you got your answer.
D. Determine whether the sum of the mean number of minutes spent on aerobic training and the mean number of minutes spent on strength training is equal to the mean total number of minutes spent training. Show or explain how you got your answer.
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(15) A rectangular garden that is $16 \frac{1}{4}$ feet wide and $11 \frac{3}{4}$ feet long will be covered with soil. If a bag of soil covers an area of 20 square feet, which of the following is closest to the number of bags of soil needed to cover the garden?
(A) 2
(B) 3
(C) 8
(D) 10

## This question has two parts.

## 16 Part A

Four triangles and some of their angle measures are shown.


Based on the angle measures, which of the following similarity statements is true?
(A) $\triangle F G E \sim \triangle T U S$
(B) $\triangle G E F \sim \triangle Q P R$
(C) $\triangle L M N \sim \triangle P Q R$
(D) $\triangle N M L \sim \triangle T S U$

## Part B

These two triangles are similar.


Which of the following similarity statements about the triangles are true?
Select the two true statements.
(A) $\triangle E F G \sim \triangle Z Y X$
(B) $\triangle E G F \sim \triangle X Y Z$
(C) $\triangle F E G \sim \triangle X Z Y$
(D) $\triangle F G E \sim \triangle Y Z X$
(E) $\triangle G F E \sim \triangle Y X Z$

11 Which of the following is equivalent to this expression?

$$
x^{2}+5 x-84
$$

(A) $(x+6)(x-14)$
(B) $(x-6)(x+14)$
(C) $(x+7)(x-12)$
(D) $(x-7)(x+12)$

18 Triangle $K L M$, shown on this coordinate plane, will be dilated by a scale factor of $\frac{1}{2}$ with respect to the origin.


What are the ordered pairs that represent the vertices of the image of triangle $K L M$ after the dilation?

Select the three ordered pairs.
(A) $(-3,-1)$
(B) $(-2,3)$
(C) $(-1,-3)$
(D) $(1,3)$
(E) $(2,-2)$
(F) $(3,-2)$

## This question has two parts.

## (19) Part A

Which of the following statements is true?
(A) The sum of two rational numbers is rational.
(B) The product of two rational numbers is irrational.
(C) The sum of a rational number and an irrational number is rational.
(D) The product of a non-zero rational number and an irrational number is rational.

## Part B

Which of the following statements is true?
(A) The sum of $\frac{\pi}{2}$ and $\frac{\pi}{2}$ is rational, and the product of $\frac{1}{2}$ and $\pi$ is rational.
(B) The sum of $\frac{\pi}{2}$ and $\frac{\pi}{2}$ is rational, and the product of $\frac{1}{2}$ and $\pi$ is irrational.
(C) The sum of $\frac{\pi}{2}$ and $\frac{\pi}{2}$ is irrational, and the product of $\frac{1}{2}$ and $\pi$ is rational.
(D) The sum of $\frac{\pi}{2}$ and $\frac{\pi}{2}$ is irrational, and the product of $\frac{1}{2}$ and $\pi$ is irrational.

20 Which of the following is the solution set of this inequality?

$$
2-4 y>14
$$

(A) $y>-3$
(B) $y<-3$
(C) $y>3$
(D) $y<3$

21 A right triangle and some of its measurements are shown in this diagram.


Based on the measurements shown in the diagram, what is $t$ ?
(A) 6 mm
(B) $4 \sqrt{3} \mathrm{~mm}$
(C) $6 \sqrt{3} \mathrm{~mm}$
(D) 8 mm

# Grade 10 Mathematics SESSION 2 

This session contains 21 questions.

You may use your reference sheet during this session. You may use a calculator during this session.

## Directions

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## EXAMPLES



22 This diagram shows a right square pyramid and some of its dimensions.


What is the volume of the pyramid?
(A) 48 cubic inches
(B) 60 cubic inches
(C) 144 cubic inches
(D) 180 cubic inches

23 A travel agent surveyed people in two age groups about whether or not they like traveling. Which two-way table shows the possible results of the survey?
(A)
Travel Survey

|  | Likes <br> Traveling | Dislikes <br> Traveling | Totals |
| :---: | :---: | :---: | :---: |
| Ages <br> $\mathbf{1 8 - 3 0}$ | 40 | 10 | 50 |
| Ages <br> 31-60 | 20 | 30 | 50 |
| Totals | 60 | 40 | 100 |

(B)
Travel Survey

|  | Likes <br> Traveling | Dislikes <br> Traveling | Totals |
| :---: | :---: | :---: | :---: |
| Ages <br> $\mathbf{1 8 - 3 0}$ | 30 | 10 | 50 |
| Ages <br> $\mathbf{3 1 - 6 0}$ | 30 | 10 | 50 |
| Totals | 60 | 40 | 100 |

(C)

| Travel Survey |  |  |  |
| :---: | :---: | :---: | :---: |
|  | Likes <br> Traveling | Dislikes <br> Traveling | Totals |
| Ages <br> $\mathbf{1 8 - 3 0}$ | 40 | 10 | 50 |
| Ages <br> $\mathbf{3 1 - 6 0}$ | 10 | 30 | 50 |
| Totals | 60 | 40 | 100 |

(D)

| Travel Survey |  |  |  |
| :---: | :---: | :---: | :---: |
|  | Likes <br> Traveling | Dislikes <br> Traveling | Totals |
| Ages <br> $\mathbf{1 8 - 3 0}$ | 30 | 10 | 50 |
| Ages <br> $\mathbf{3 1 - 6 0}$ | 40 | 10 | 50 |
| Totals | 60 | 40 | 100 |

(24) Which of the following graphs does not represent $y$ as a function of $x$ ?
(A)

(C)

(B)

(D)


25 Consider square $E F G H$, shown on this coordinate plane.


Square $E F G H$ will be reflected over the $y$-axis. Which graph correctly shows the image of square $E F G H$ after the reflection?
(A)

(B)

(C)

(D)


26 A parallelogram is shown on this coordinate plane.


What is the perimeter, in units, of the parallelogram?
(A) 24
(B) 36
(C) 48
(D) 64
27) A sphere and one of its dimensions are shown in this diagram.


Which of the following is closest to the volume of the sphere?
(A) 9203 in. ${ }^{3}$
(B) $1150 \mathrm{in}^{3}{ }^{3}$
(C) $163 \mathrm{in}^{3}$
(D) 82 in. ${ }^{3}$

28 This table shows the values of the linear function $f(x)$ for different values of $x$.

| $x$ | $f(x)$ |
| :---: | :---: |
| 0 | 120 |
| 20 | 90 |
| 40 | 60 |
| 60 | 30 |

The function $g(x)$ is represented by this equation.

$$
g(x)=10 x+40
$$

Which statement correctly compares the rates of change and $y$-intercepts of $f(x)$ and $g(x)$ ?
(A) Function $f(x)$ has a greater rate of change and a greater $y$-intercept than function $g(x)$.
(B) Function $g(x)$ has a greater rate of change and a greater $y$-intercept than function $f(x)$.
(C) Function $f(x)$ has a greater rate of change than function $g(x)$, and function $g(x)$ has a greater $y$-intercept than function $f(x)$.
(D) Function $g(x)$ has a greater rate of change than function $f(x)$, and function $f(x)$ has a greater $y$-intercept than function $g(x)$.

29 A factory worker loaded some boxes onto a cart. Each box has the same weight. This expression represents the total weight, in pounds, of the cart and $n$ boxes.

$$
10 n+25
$$

Based on the expression, what is the weight, in pounds, of the cart?
Enter your answer in the answer boxes at the top of the answer grid and completely fill the matching circles.


This question has four parts. Be sure to label each part of your response.
30 A student graphed $\triangle P Q R$ on a coordinate plane, as shown.

A. The student reflected $\triangle P Q R$ over the $x$-axis to create $\triangle E F G$. What are the coordinates of vertex $E$ ? Show or explain how you got your answer.
B. The student performed a different single transformation on $\triangle P Q R$ to create $\triangle J K L$. The coordinates of vertex $K$ are $(4,1)$. What could be the single transformation the student performed?
C. Describe a single transformation the student can perform on $\triangle P Q R$ so that its image, $\triangle U V W$, is similar to, but not congruent to, $\triangle P Q R$. Show or explain how you got your answer.
D. What will be the coordinates of vertex $W$ after the student performs the transformation described in Part C? Show or explain how you got your answer.

30
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31 Marvin solved this equation.

$$
4(x+5)=88
$$

Marvin created a table showing each step he used to solve the equation. The table also showed the correct explanation for each step.

Which of the following tables shows the correct explanation for each step in Marvin's solution?

(A) \begin{tabular}{c|l|}
\hline $4(x+5)=88$ \& Given <br>

\hline $4 x+20=88$ \& | He multiplied |
| :--- |
| both sides |
| by 4. | <br>


\hline $4 x=68$ \& | He added 20 |
| :--- |
| to both sides. | <br>


\hline$x=17$ \& | He multiplied |
| :--- |
| both sides |
| by 4. | <br>

\hline
\end{tabular}

(B)

| $4(x+5)=88$ | Given |
| :---: | :--- |
| $4 x+20=88$ | He used the <br> distributive <br> property. |
| $4 x=68$ | He subtracted <br> 20 from both <br> sides. |
| $x=17$ | He divided <br> both sides <br> by 4. |

(C)

| $4(x+5)=88$ | Given |
| :---: | :--- |
| $4 x+20=88$ | He used the <br> distributive <br> property. |
| $4 x=68$ | He divided <br> both sides <br> by 20. |
| $x=17$ | He subtracted <br> 4 from both <br> sides. |

(D)

| $4(x+5)=88$ | Given |
| :---: | :--- |
| $4 x+20=88$ | He added 4 <br> to both sides. |
| $4 x=68$ | He multiplied <br> both sides <br> by 20. |
| $x=17$ | He divided <br> both sides <br> by 4. |

32 Each exterior angle of a regular polygon has a measure of $30^{\circ}$. What is the total number of sides of the polygon?
(A) 6
(B) 9
(C) 12
(D) 15

This question has two parts.
33 On a map, 1 inch equals 0.75 mile.

## Part A

The distance between a museum and a library on the map is 2 inches.
What is the actual distance, in miles, between the museum and the library?
Enter your answer in the answer boxes at the top of the answer grid and completely fill the matching circles.


## Part B

The actual distance between the library and a bus stop is 3 miles.
What is the distance, in inches, between the library and the bus stop on the map?
Enter your answer in the answer boxes at the top of the answer grid and completely fill the matching circles.


34 Triangle $L M N$ is similar to triangle $X Y Z$. This diagram shows some of the dimensions, in units, of the triangles.


Based on the diagram, what is the length, in units, of $\overline{X Z}$ ?
(A) 13.5
(B) 22.5
(C) 24
(D) 28

This question has four parts. Be sure to label each part of your response.
35 At the beginning of the year, Samantha deposits $\$ 1000$ into a savings account that pays $2.5 \%$ interest. She does not deposit money into or withdraw money from the account for 1 year.
A. What is the interest rate expressed as a decimal?
B. This formula can be used to calculate the total amount of money, including interest, in an account over time for a deposit of $\$ 1000$.

$$
A=1000\left(1+\frac{r}{n}\right)^{n t}
$$

In the formula, the variables $A, r, t$, and $n$ are defined as follows:

- $A=$ the amount of money in the savings account after $t$ years
- $r=$ the interest rate as a decimal
- $t=$ the amount of time, in years, the money is invested
- $n=$ the number of times the interest is compounded in 1 year

What is the amount of money, in dollars, in Samantha's savings account at the end of 1 year if the interest is compounded annually (once per year)? Show or explain how you got your answer.
C. Samantha deposits $\$ 1000$ into a new savings account. The new savings account pays $3 \%$ interest, compounded semiannually (twice per year). She does not deposit money into or withdraw money from the account for $1 \frac{1}{2}$ years.

Write an equation that can be used to determine the amount of money, in dollars, in the new savings account at the end of $1 \frac{1}{2}$ years.
D. Use the equation you wrote in Part C to determine the amount of money, in dollars, in Samantha's new savings account at the end of $1 \frac{1}{2}$ years. Show or explain how you got your answer.
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36 A storage rack has two wires that help support the sides of the rack. Each wire connects the top of one side to the base of the rack. The sides form right angles with the base of the rack. The rack and its interior dimensions are shown in this diagram.


Which of the following is closest to the length, in feet, of each wire?
(A) 9
(B) 10.4
(C) 13.4
(D) 18

## This question has two parts.

## 37 Part A

This table shows the value of linear function $f(x)$ for different values of $x$.

| $\boldsymbol{x}$ | 2 | 4 | 5 | 7 |
| :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{f}(\boldsymbol{x})$ | 223 | 206 | 197.5 | 180.5 |

A student graphed the line that represents $f(x)$ on a coordinate plane. Which statement about the graph of $f(x)$ is true?
(A) The slope of the line is negative, and the $y$-intercept of the line is negative.
(B) The slope of the line is negative, and the $y$-intercept of the line is positive.
(C) The slope of the line is positive, and the $y$-intercept of the line is negative.
(D) The slope of the line is positive, and the $y$-intercept of the line is positive.

## Part B

The student also graphed linear function $g(x)$ on a coordinate plane, as shown.


Which of the following equations models $g(x)$ ?
(A) $g(x)=-6 x+228$
(B) $g(x)=-3 x+38$
(C) $g(x)=3 x+228$
(D) $g(x)=6 x+38$

33 A student has two part-time jobs: babysitting and tutoring. The student earns an hourly wage at each job.

- On Monday, the student earned a total of $\$ 130$ for 4 hours of babysitting and 2 hours of tutoring.
- On Tuesday, the student earned a total of $\$ 80$ for 3 hours of babysitting and 1 hour of tutoring.

Which of the following systems of equations can be used to find $x$, the student's hourly wage for babysitting, and $y$, the student's hourly wage for tutoring?
(A) $2 x+4 y=130$
$x+3 y=80$
(B) $3 x+y=130$
$4 x+2 y=80$
(C) $4 x+3 y=130$
(D) $4 x+2 y=130$
$2 x+y=80$
$3 x+y=80$

39 Figure $R$ is shown on this coordinate plane.


Which of the following transformations would carry Figure $R$ onto itself?
(A) a reflection over the line $y=1$
(B) a reflection over the line $x=1$
(C) a $90^{\circ}$ clockwise rotation about the point $(1,1)$
(D) a $180^{\circ}$ clockwise rotation about the point $(1,1)$

## This question has two parts.

40 The population of each of four towns is predicted to increase or decrease at a constant rate. The equations shown in this table can be used to predict the population, $P$, of each town $t$ years from today.

## Population Predictions

| Town | Equation |
| :---: | :---: |
| Pinehill | $P=800-20 t$ |
| Rye | $P=500+15 t$ |
| Smithfield | $P=10 t+950$ |
| Troy | $P=-50 t+600$ |

## Part A

Based on the equations in the table, which statements about the populations of these towns are true?

Select two true statements.
(A) The population of Troy is decreasing.
(B) The population of Pinehill is increasing.
(C) The populations of Rye and Smithfield are each increasing.
(D) The populations of Smithfield and Troy are each decreasing.
(E) The populations of all four of the towns are each increasing.

## Part B

Which of the following lists the towns, based on their populations today, from least to greatest population?
(A) Pinehill, Rye, Smithfield, Troy
(B) Rye, Troy, Pinehill, Smithfield
(C) Smithfield, Pinehill, Rye, Troy
(D) Troy, Pinehill, Smithfield, Rye

41 A student shaded part of circle $V$, as shown.


Which of the following is closest to the area of the shaded part of circle $V$ ?
(A) $78.5 \mathrm{~cm}^{2}$
(B) $31.4 \mathrm{~cm}^{2}$
(C) $25.0 \mathrm{~cm}^{2}$
(D) $15.7 \mathrm{~cm}^{2}$

42 A student will draw the line of best fit for the set of data shown in this scatter plot.


Which of the following best describes how to draw the line of best fit for the set of data?
(A) The line of best fit should pass through the origin.
(B) The line of best fit should connect all of the data points.
(C) The line of best fit should come as close as possible to every data point.
(D) The line of best fit should contain the points with the highest and lowest $y$-values.

CONVERSIONS
1 cup $=8$ fluid ounces
1 pint $=2$ cups
1 quart $=2$ pints
1 gallon $=4$ quarts
1 gallon $\approx 3.785$ liters
1 liter $\approx 0.264$ gallon
1 liter $=1000$ cubic centimeters

1 inch $=2.54$ centimeters
1 meter $\approx 39.37$ inches
1 mile $=5280$ feet
1 mile $=1760$ yards
1 mile $\approx 1.609$ kilometers
1 kilometer $\approx 0.62$ mile

1 pound = 16 ounces
1 pound $\approx 0.454$ kilogram
1 kilogram $\approx 2.2$ pounds
1 ton $=2000$ pounds

## AREA (A) FORMULAS

square......... $A=s^{2}$
rectangle . . . . . . . . $A=I w$
parallelogram . . . . . $A=b h$
triangle ......... $A=\frac{1}{2} b h$
trapezoid . . . . . . . A $A=\frac{1}{2} h\left(b_{1}+b_{2}\right)$
circle

$$
A=\pi r^{2}
$$

## TOTAL SURFACE AREA (SA) FORMULAS

cube
$S A=6 s^{2}$
right square pyramid... $S A=s^{2}+2 s \ell$
( $\ell=$ slant height $)$
right rectangular prism . . SA $=2(/ w)+2(h w)+2(I h)$

## CIRCLE FORMULAS

pi . . . . . . . . . . . $\pi \approx 3.14$
circumference ... . $C=2 \pi r$ OR $C=\pi d$ area $A=\pi r^{2}$

## RIGHT TRIANGLES



Pythagorean Theorem

$$
a^{2}+b^{2}=c^{2}
$$

Trigonometric Ratios
$\sin \theta=\frac{a}{c}$
$\cos \theta=\frac{b}{c}$
$\tan \theta=\frac{a}{b}$

## VOLUME (V) FORMULAS

cube $\qquad$ $V=s^{3}$
( $s$ = length of an edge)
prism $\qquad$ $V=B h$
cylinder

$$
V=\pi r^{2} h
$$

cone $V=\frac{1}{3} \pi r^{2} h$
pyramid......... . V $=\frac{1}{3} B h$
sphere
$V=\frac{4}{3} \pi r^{3}$

## SPECIAL RIGHT TRIANGLES



Spring 2019 Released Operational Items

| $\begin{gathered} \hline \text { PBT } \\ \text { Item } \\ \text { No. } \\ \hline \end{gathered}$ | Page No. | Reporting Category | Standard | Item Type* | Item Description | Correct Answer** |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 354 | Algebra and <br> Functions | A-APR.A. 1 | SR | Multiply two polynomial expressions. | B |
| 2 | 354 | Algebra and Functions | F-IF.A. 2 | SR | Evaluate a quadratic function for different input values. | C |
| 3 | 355 | Geometry | G-C.A. 2 | SR | Use an inscribed right triangle to determine the circumference of a circle. | B |
| 4 | 355 | Geometry | G-CO.B. 6 | SR | Identify transformations that would produce a congruent figure. | A,B,C |
| 5 | 356 | Algebra and <br> Functions | A-REI.C. 6 | SA | Solve for one variable in a system of linear equations algebraically. | 2 |
| 6 | 356 | Algebra and Functions | A-SSE.A. 2 | SR | Factor a trinomial expression. | B |
| 7 | 357 | Algebra and <br> Functions | A-REI.D. 12 | SR | Identify the graph of the solution set of a linear inequality in two variables. | D |
| 8 | 358 | Geometry | G-GPE.B. 5 | SR | Identify an equation of a line perpendicular to a given line. | A |
| 9 | 359 | Number and Quantity | N-RN.A. 2 | CR | Evaluate expressions involving radicals and rational exponents. |  |
| 10 | 361 | Statistics and Probability | S-ID.A. 2 | SR | Compare measures of center and spread of two data sets. | C |
| 11 | 362 | Geometry | G-GPE.B. 6 | SR | Find the midpoint of a line segment graphed on a coordinate plane. | B |
| 12 | 363 | Statistics and Probability | S-CP.B. 6 | SR | Calculate conditional probabilities of real-world events from a description. | A;D |
| 13 | 364 | Algebra and Functions | A-REI.B. 4 | SR | Find the solutions of a quadratic equation in one variable. | A |
| 14 | 365 | Statistics and Probability | S-ID.A. 2 | CR | Interpret data in a data display and compare the measures of center of the data sets. |  |
| 15 | 367 | Number and Quantity | N-Q.A. 2 | SR | Estimate the solution of a real-world problem using units. | D |
| 16 | 368 | Geometry | G-SRT.A. 3 | SR | Use similarity criteria to identify and name similar triangles. | A;C,E |
| 17 | 369 | Algebra and <br> Functions | A-SSE.B. 3 | SR | Factor a quadratic trinomial expression. | D |
| 18 | 370 | Geometry | G-SRT.A. 1 | SR | Identify the graph of a figure on a coordinate plane after a dilation. | A,D,F |
| 19 | 371 | Number and Quantity | N-RN.B. 3 | SR | Identify correct statements about operations with rational and irrational numbers. | A;D |
| 20 | 372 | Algebra and <br> Functions | A-REI.B. 3 | SR | Determine the solution set of a linear inequality in one variable. | B |
| 21 | 373 | Geometry | G-SRT.C. 6 | SR | Use a trigonometric ratio to determine a missing side length in a right triangle. | C |
| 22 | 376 | Geometry | G-GMD.A. 3 | SR | Calculate the volume of a right square pyramid. | A |
| 23 | 377 | Statistics and Probability | S-ID.B. 5 | SR | Identify a two-way table that represents a real-world situation. | A |


| PBT <br> Item <br> No. | Page <br> No. | Reporting <br> Category | Standard | Item <br> Type* | Item Description | Correct <br> Answer** |
| :---: | :---: | :--- | :--- | :--- | :--- | :--- |
| 24 | 378 | Algebra and <br> Functions | F-IF.A.1 | SR | Identify a graph that does not represent a functional <br> relationship. | D |
| 25 | 379 | Geometry | G-CO.A.5 | SR | Identify the graph of a figure on a coordinate plane after a <br> reflection. | C |
| 26 | 380 | Geometry | G-GPE.B.7 | SR | Calculate the perimeter of a parallelogram shown on a <br> coordinate plane. | B |
| 27 | 381 | Geometry | G-GMD.A.3 | SR | Calculate the volume of a sphere. | B |
| 28 | 382 | Algebra and <br> Functions | F-IF.C.9 | SR | Compare the properties of linear functions represented in <br> different ways. | D |
| 30 | 384 | Algebra and <br> Functions | A-SSE.A.1 | SA | Interpret part of an expression that represents a real-world <br> Situation. | 25 |
| 31 | 386 | Glgebra and <br> Functions | A-REI.A.1 | SR | Describe transformations that create congruent and non- <br> congruent images and determine the coordinates of the <br> vertices of transformed figures. | Sustify each step in the solution of a linear equation. |

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[^0]:    * Mathematics item types are: selected-response (SR), short-answer (SA), and constructed-response (CR).
    ** Answers are provided here for selected-response and short-answer items only. Sample responses and scoring guidelines for constructedresponse items will be posted to the Department's website later this year.

