

Correlation Coefficient Critical Values for 0.05 and 0.01 Significance Levels

Sample Size n	0.05 Critical Value	0.01 Critical Value	Sample Size n	0.05 Critical Value	0.01 Critical Value
4	0.950	0.990	21	0.433	0.549
5	0.878	0.959	22	0.423	0.537
6	0.811	0.917	23	0.413	0.526
7	0.754	0.875	24	0.404	0.515
8	0.707	0.834	25	0.396	0.505
9	0.666	0.798	26	0.388	0.496
10	0.632	0.765	27	0.381	0.487
11	0.602	0.735	28	0.374	0.479
12	0.576	0.708	29	0.367	0.471
13	0.553	0.684	30	0.361	0.463
14	0.532	0.661	35	0.335	0.430
15	0.514	0.641	40	0.312	0.403
16	0.497	0.623	45	0.294	0.380
17	0.482	0.606	50	0.279	0.361
18	0.468	0.590	60	0.254	0.330
19	0.456	0.575	70	0.236	0.305
20	0.444	0.561	80	0.220	0.286

Interpreting the correlation coefficient r and the coefficient of determination r^2

For sample sizes $n \geq 4$, r is statistically significant if $|r| >$ the critical value.

Example 1: $n = 20$ and $r = 0.587$

With $n = 20$ and $r = 0.587$, we can say there is a statically significant linear relationship between the explanatory variable and the response variable at the 0.01 level of significance. There is at most a 1% chance that this apparent relationship is due to chance or other unknown factors.

The coefficient of determination $r^2 = 0.3446$. This tells us about 34% of the variation or change in the response variable can be explained by variation or change in the explanatory variable. The remaining 66 % of the variation in the response variable is unexplained and is due to chance or other unknown factors.

Example 2: $n = 9$ and $r = -0.758$

With $n = 9$ and $r = -0.758$, we can say there is a statically significant linear relationship between the explanatory variable and the response variable at the 0.05 level of significance. There is at most a 5% chance that this apparent relationship is due to chance or other unknown factors.

The coefficient of determination $r^2 = 0.5746$. This tells us about 57% of the variation or change in the response variable can be explained by variation or change in the explanatory variable. The remaining 43 % of the variation in the response variable is unexplained and is due to chance or other unknown factors.

Example 3: $n = 16$ and $r = 0.478$

With $n = 9$ and $r = 0.478$, we can say there is no statistically significant linear relationship between the explanatory variable and the response variable at the 0.01 or 0.05 level of significance .