## Significant Figures

## Nature of Measurement

Measurement - quantitative observation consisting of 2 parts

$$
\begin{aligned}
& \text { Part } 1 \text { - number } \\
& \text { Part } 2 \text { - scale (unitit) }
\end{aligned}
$$

Examples:

> 20 grams
> $6.63 \times 10^{-34}$ Joule seconds

## Significant Figures

## *All of the known digits + 1 estimated digit



## Uncertainty of Measurement

The last digit on any physical measurement is always an approximation.
-Significant figures are the number of digits that can be accurately measured and the first uncertain digit.

## Rule \#1

*All non-zero numbers are significant
*3.89 = 3 significant figures
*938.3 = 4 significant figures

## Rule \#2

Sandwich rule: all zero's between non-zero or significant numbers are significant
a.) $202=3$ significant figures

## Rule \#2

$$
\begin{aligned}
& \text { b.) } 67000045=\frac{8}{\text { significant figures }}
\end{aligned}
$$

## c.) $150098=6$ significant

 figures
## Rule \#3

* leading zeros are never significant


## Rule \#3 Leading zeros are NEVER significant

$\gtrdot 0.91=2$ significant figures
$* 0.0089=2$ significant figures

## Rule \#4

# - Trailing zeros are only 

 significant if there is a decimal place in the number-202.00 = 5 significant figures

## Practice the zero rules:

$$
10.0098=\text { 6 sig digs }
$$

$$
9800=2 \text { sig digs }
$$

$$
0.009800=4 \text { sig digs }
$$

## Sig Fig Practice \#1

How many significant figures in each of the following?
$1.0070 \mathrm{~m} \rightarrow 5$ sig figs
$17.10 \mathrm{~kg} \rightarrow 4$ sig figs
$100,890 L \rightarrow 5$ sig figs
$\underline{3.29} \times 10^{3} s \rightarrow 3$ sig figs
$0.0054 \mathrm{~cm} \rightarrow 2$ sig figs
$3,200,000 \rightarrow 2$ sig figs

## Rule \#5

* Numbers obtained through counting or are defined have unlimited significant figures
- 24 people in the class
- 60 minutes $=1$ hour
bboth have unlimited


# Significant Figures in Calculations 

*An answer cannot be more precise than the least precise measurement in the calculation

## Rounding

-Look at the digit to the right of the one you need to round. - If is is < 5 - leave it alone

- If it is $\geq 5$ - round up

$$
\begin{aligned}
& \text { 56.312 } \mathrm{m}=\square(4 \mathrm{sig} . \\
& \text { figs.) } \\
& 56.31 \mathrm{~m}
\end{aligned}
$$

## Rounding

* 0.001775 m =
(2 sig. figs.)
$\$ 0.0018$ m
- 8792 m =
(2 sig. figs.)
-8800 m


## Addition and Subtraction

- Answers should be rounded to the same number of decimal places as the least (lowest) number of decimal places in the calculation


## Using significant figures when adding and subtracting

892.542

20.629
0.18 $\qquad$
$+\quad 4.20$


### 917.551

The least amount of significant figures to the right of the decimal in the numbers is 2 ; therefore, the answer should only have 2 significant figures to the right of the decimal.

### 917.55

## Examples

\$12.52 m + $349.0 m=$

- $361.52 \mathrm{~m}=361.5 \mathrm{~m}$
* $74.626 m-28.34 m=$
- $46.286 \mathrm{~m}=46.29 \mathrm{~m}$


## Sig Fig Practice \#2

| Calculation | Calculator says: |  | Answer |
| :--- | :--- | :--- | :--- |
| $3.24 \mathrm{~m}+7.0 \mathrm{~m}$ | 10.24 m |  | 10.2 m |
| $100.0 \mathrm{~g}-23.73 \mathrm{~g}$ | 76.27 g |  | 76.3 g |
| $0.02 \mathrm{~cm}+2.371 \mathrm{~cm}$ | 2.391 cm |  | 2.39 cm |
| $713.1 \mathrm{~L}-3.872 \mathrm{~L}$ | 709.228 L | 709.2 L |  |
| $1818.2 \mathrm{lb}+3.37 \mathrm{lb}$ | 1821.57 lb | 1821.6 lb |  |
| $2.030 \mathrm{~mL}-1.870 \mathrm{~mL}$ | 0.16 mL | 0.160 mL |  |

## Multiplication and Division

-The answer should be rounded to the same number of significant figures as the least number of significant figures in the calculation

## Examples

$7.55 \mathrm{~m} \times 0.34 \mathrm{~m}=$

- $2.567 \mathrm{~m}^{2}=2.6 \mathrm{~m}^{2}$
\$. $20 \mathrm{~m} \times 0.70 \mathrm{~m}=$
$1.47 \mathrm{~m}^{2}=1.5 \mathrm{~m}^{2}$


## Examples

- $2.4526 \mathrm{~m} / 8.4 \mathrm{~m}=$
$-0.2922=0.29 \mathrm{~m}^{2}$
- $0.365 \mathrm{~m} / 0.0200 \mathrm{~m}=$
- $18.25=18.3 \mathrm{~m}^{2}$


## Sig Fig Practice \#3

Calculation
$3.24 \mathrm{~m} \times 7.0 \mathrm{~m}$
Calculator says: $22.68 \mathrm{~m}^{2}$

## Answer

$23 \mathrm{~m}^{2}$ $100.0 \mathrm{~g} \div 23.7 \mathrm{~cm}^{3} \quad 4.219409283 \mathrm{~g} / \mathrm{cm}^{3} \quad 4.22 \mathrm{~g} / \mathrm{cm}^{3}$ $0.02 \mathrm{~cm} \times 2.371 \mathrm{~cm} \quad 0.04742 \mathrm{~cm}^{2}$ $0.05 \mathrm{~cm}^{2}$
$710 \mathrm{~m} \div 3.0 \mathrm{~s}$
$236.6666667 \mathrm{~m} / \mathrm{s}$
$1818.2 \mathrm{lb} \times 3.23 \mathrm{ft} \quad 5872.786 \mathrm{lb} \cdot \mathrm{ft}$ $1.030 \mathrm{~g} \div 2.87 \mathrm{~mL} \quad 2.9561 \mathrm{~g} / \mathrm{mL}$
$240 \mathrm{~m} / \mathrm{s}$
$5870 \mathrm{lb} \cdot f t$
$2.96 \mathrm{~g} / \mathrm{mL}$

## Precision and Accuracy

Accuracy refers to the agreement of a particular value with the true value.

Precision refers to the degree of agreement among several measurements made in the same manner.


Neither accurate nor precise


Precise but not accurate


Precise AND
accurate

